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Flexible Pavement Design Developments

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Contents

Compaction Requirements for Flexible Pavements

R. FOSTER aad R.G. AHLVIN, respectively, Coordinator of Research, National Jituminous Concrete Association, and Chief, Special Projects Section, Flexible Pavelent Branch, Soils Division, U.S. Army Engineer, Waterways Experiment Station; Icksburg, Mississippi

> **This paper presents the results of an analytical study made to develop criteria for determining the degree of compaction required at different depths in soils beneath flexible pavements to prevent consolidation of the soil under wheel loads and consequent deformation of the pavement.**

Data obtained from observations of airfield pavements in actual service and from reports of accelerated traffic tests on carefully controlled test sections were tabulated, and from these tabulations correlations were developed between the compaction effort applied to flexible pavements by aircraft traffic and the densities resulting from this compaction effort at various depths.

The established CBR relations were used to integrate the effects of wheel load, tire pressure, assembly configuration, and depth below pavement surface into a compaction index, C_i, **for purposes of this study. Correlations between Cj and the densities required to prevent further compaction are presented.**

IN 1942, when the Corps of Engineers adopted the California Bearing Ratio method i : use in designing flexible pavements for airfields, the CBR procedures specified Loratory compaction of soil samples under a 2,000-psi static load. This compacl)n gives densities of the same order as those obtained by AASHO Method T99 for ^ndy and gravelly soils, but much higher densities for clayey soils. The CBR methalso specified a field compaction test using a tamper that imparted a compaction **:ort considerably greater than imparted by AASHO T99 compaction. Personnel of ; Corps of Engineers and consultants to the Corps anticipated that higher densities uld be needed in soil components of airfield pavements than were produced by the SHO T99 compaction test, but did not consider the CBR procedures entirely suit** le for this purpose. From laboratory tests performed in the Corps' Flexible Pave**snt Laboratory, Soils Division, at the Waterways Experiment Station, Vicksburg, ssissippi, it was determined that a modification of AASHO T99 would be better suitto the Corps' problems and would require less new test equipment. The Corps' de- ;n manual published in June 1942 specified a laboratory compaction test similar to SHO T99, but with modifications which increased the weight of the hammer from 5 10 lb, the height of fall from 12 to 18 in., and the number of layers compacted from) 5. These changes increased the compaction effort almost fivefold.**

Also, based primarily on judgment of Corps personnel and consultants, compaction luirements were specified in 1942 as 95 percent of modified AASHO maximum density all base courses, subbases, and for the top 6 in. of subgrades. In most soils 95 perit of modified AASHO density is equal to or higher than 100 percent of AASHO T99 Kdmum density; therefore, these specifications represented a definite upgrading of ^paction requirements from those used for highways, which were normally 95 per-It of AASHO T99. Compaction of fill was specified to be 90 percent of modified K HO compaction, but no specifications were established for cut sections except in •top 6 in.

1945, a study was made of the degrees of compaction existing in certain accelertraffic test sections. These studies showed a definite relation between degree of

compaction, wheel load, and depth from the surface of the pavement to the layer being studied. It was assumed that if this density had been built into the structure during construction of the test sections, no appreciable densification would have occurred under traffic. As a result of these studies, the Corps has established in a sense, a "design" of the ultimate compaction necessary. For the "design," the compaction that will be induced in each layer by the airplane traffic is determined, and this degree of compaction is required to be obtained during construction.

Unfortunately, the studies which led to these developments were documented only in letter reports between the Waterways Experiment Station and the Office, Chief of Engi neers, and thus the test data have not been generally available. However, in 1959, the Corps published a report (24) which contains all the data collected by the Corps on the subject. The authors of this paper were directly connected with the studies. This pa per summarizes data (24) and shows how the procedures developed by the Corps can b applied to civil airfields and highways.

Early Studies

Figure 1, taken from a 1945 unpublished letter report, shows plots of the degree of compaction that developed in several accelerated-traffic tests at various depths below

Figure 1. Compaction study data.

the pavement surface. It is apparent that the density developed by traffic decreased with depth in a logical manner when the densities were expressed as a percentage of the maximum densities obtained in the laboratory compaction test. This pattern appeared in all the accelerated-traffic tests (Fig. 1A-H) and in the airfield pavement u der actual traffic (Fig. 2). Another feature indicated by these results is that the col sionless sands appear to plot about 5 points higher (in percentage of compaction) that the other soils. Figures 1J and 1K are summary plots obtained by reading the dept

at which 90, 95, 100, and 105 percent compaction were measured and plotting the depth against wheel load. The lines of equal percentage of compaction were fitted to the plotted points visually. These summary plots were used to establish the following compaction requirements which appeared in the Corps of Engineers' engineering design manual published in 1946.

Through the succeeding four years, personnel of the Flexible Pavement Laboratory were engaged in producing CBR versus thickness design curves for multiple-wheel gears and for higher tire pressures by theoretical resolution of the single-wheel curves. These same concepts were applied to the compaction requirements, and it was found that a definite relation existed between the required degree of compaction and the maximum shear stress (T max) as computed by the theory of elasticity. Figure 2 shows the relation. In 1950, the relation shown in Figure 2 was used to translate the compaction requirements for single wheels (Table 1) into compaction requirements for a range of single, dual, and twin-tandem assemblies. Although tire pressure was not

hdicated in the 1946 requirements, the tire pressures for the various loads were approximately those shown in the legend of Figure 2, and these values were used for the translations. ranslations were produced for 100- and 200-psi tire pressures for single-wheel loads. For e dual and twin-tandem assemblies, the tire pressure was varied to give a contact area of 7sqin. for each tire. Figure 3 shows the compaction requirements produced by theoret-

TABLE 1

1946 COMPACTION REQUIREMENTS

1 resolution of the 1946 criteria. These requirements appeared in the Corps' engi- !ring design manual in 1951.

In the period following 1951, it was necessary to produce plots such as those shown Figure 3 for many different gear loadings. In the course of this work, ample evice was found that the compaction that will be produced in a given layer by traffic is (unction of the total load, arrangement of tires, tire pressure, number of repetitions, d depth to the given layer. Theoretically, the characteristics of the material between the surface and the given layer should also influence the compaction, but apparently the differences in the materials in the average flexible pavement are not enough to significantly influence compaction.

The determination of the exact relations between the compaction induced in the give layer and each of the variables listed above would require a multiplicity of carefully controlled test sections. A major discovery by personnel of the Flexible Pavement

Figure 3. Subgrade and base course compaction requirements.

Laboratory was that the design CBR could be used as a compaction index to combine the parameters listed. In preparing compaction requirements for the various gear loads it was found that an almost constant relation exists between the degree of compaction required in a given layer by the Corps and the design CBR indicated by the Corps' CBR design curves for that layer. Table 2 illustrates the constancy of th relation. The values shown in Table 2 were obtained by selecting a range of loads

TABLE 2

REQUIRED CBR VALUES FOR VARIOUS WHEEL LOADS'

		Single Wheels		Multiple Wheels					
	Wheel		CBR for Indicated	Assembly Load	CBR for Dual Wheel	Assembly	CBR for Twin-Tandem		
ASHO	Load	Tire Pressure				Load			
Density	(kips)	100 psi	200 psi	(kips)	Loads	(kips)	Wheel Loads		
				(a) Cohesionless Sands					
00%	10	8.1	7.1	50	9.2	100	9.5		
Mod.	20	8.1	7.2	75	8.6	125	8.9		
	30	8.0	7.7	100	8.5	150	9.4		
	40	8.0	7.5	125	8.5	175	8.9		
	50	8.0	7.4	-		200	9.2		
	60	8.0	7.5						
95%	10	3.7	3.3	50	4.1	100	4. 7		
Mod.	20	3.6	3.4	75	4.0	125	4.6		
	30	3.6	3.3	100	3.7	150	4.5		
	40	3.5	3.3	125	3.6	175	4.2		
	50	3.6	3.3			200	4. 1		
	60	3.6	3.6						
			(b)	Other Soils					
0%	10	15	13	50	16	100	16		
Mod.	20	15.5	13.5	75	14.5	125	15		
	30	16	14	100	15	150	15		
	40	15.5	14	125	15	175	15.5		
	50	16	13.5			200	16		
	60	16	13.5						
5%	10	8.1	7.1	50	9.2	100	9.5		
Mod.	20	8.1	7.2	75	8.6	125	8.9		
	30	8.0	7.7	100	8.5	150	9.4		
	40	8.0	7.5	125	8.5	175	8.9		
	50	8.0	7.4			200	9.2		
	60	8.0	7.5						

verage CBR: (a) Cohesionless Sands, 100% Mod. AASHO Density = 8.3; 95% = 3.8; (b) her Soils, 100% Mod. AASHO Density = 15.0 ; 95% = 8.3 .

Id gear configurations, reading the depth at which 95 and 100 percent compaction ^ d be required from Figure 3, and then reading from the respective CBR curve the R that would be required at that thickness. For example. Figure 3 indicates that any material other than cohesionless sand, 100 percent compaction would be rered at a depth of 7 in. for a 10,000-lb, single-wheel load, 100-psi tire pressure. Corps' CBR design curves (Fig. 2 of Appendix, (2)) indicate that a design CBR 15 would be required for the 10,000-lb wheel load at a depth of 7 in. The other ues shown in Table 2 were obtained in the same manner. This over-all factor ch combines the parameters of load, tire arrangement, tire pressure, number of etitions, and depth to the layer under consideration was labeled "Compaction Index," to avoid the confusion that would exist if the initials CBR were used. With this fnbination factor the variables are reduced to two, percentage of compaction and ipaction index, and all pertinent data can be plotted in one plot and brought to bear Ithe problem even though the data from individual tests do not cover the full range U e variables.

•Following this discovery, a review was made of all available data (4 - 25). Data re considered pertinent only where information was available on the density, depth,

TABLE 3

ACCELERATED TRAFFIC TEST COMPACTION RESULTS

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TIELD COMPACTION DATA FOR FLEXIBLE AIRFIELD PAVEMENTS

* The compaction index is the design CBR value for the corresponding load and depth.

TABLE 4 (Continued)

* Classification given where Atterberg limits are unknown.

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TABLE 4 (Continued)

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TABLE 4 (Continued)

igure 4. Compaction requirements of cohesive (plastic) soils for flexible airfield pavements, Table 1 data.

lid plasticity of the soil, and on the load, tire arrangement, tire pressure, and volume traffic. Table 3 summarizes the data from certain carefully controlled test sections; ese were considered of primary reliability. Table 4 summarizes data from airfields, hich were considered of secondary reliability.

The data from Table 3 are plotted as diagrams of percent compaction versus com- .ction index in Figures 4 and 5. Since tolerable amounts of settlement from compac-*Wpn* have not been established, the points shown in Figures 4 and 5 cannot be separated to "acceptable" and "nonacceptable" categories with a dividing line drawn between
em. The points in Figures 4 and 5 that plot toward the lower densities (for a given The points in Figures 4 and 5 that plot toward the lower densities (for a given impaction index) represent cases where the amount of densification that occurred was hall. This could easily be due to a low volume of traffic or a moisture content conderably dry (or wet) of optimum. The points that plot toward the higher densities, wever, represent those cases where the volume of traffic was high and the moisture nditions were proper for compaction to occur. A limiting line, set high enough so It all points would fall below it, would be a completely safe limit; however, due to a inaccuracies involved in density sampling and in determining the proper reference nsity (modified AASHO), it is felt that such a limiti inaccuracies involved in density sampling and in determining the proper reference 3ity (modified AASHO), it is felt that such a limiting line would be unduly conservae. Also, some of the points lying in high positions may be due to unusually high denies developed during construction, or to naturally high densities, rather than to traf-

. The lines shown in Figures 4 and 5 are intended to exclude the majority of the internal control of the curves was influenced to some degree by the pattern of degree μ The shape of the curves was influenced to some degree by the pattern of deny-depth-load relations which was in use prior to the time this study was made. In Figure 4, which treats cohesive soils, the material strength requirements and sultant normal design practices affect the values at high compaction indexes. Loadis applied to a test section or airfield that would plot in the high C_i range would prote failure unless the materials involved had unusually high strengths (CBR values). hesive materials at or near optimum moisture content do not normally have these sually high strengths, but may have them at moisture contents well below optimum, ollows that the data which were obtained for cohesive materials at high values of C_i ^Id not have been in the proper moisture condition to give maximum compaction.

Figure 5. Compaction requirements of cohesionless (NP) soils for flexible airfield pavements, Table 1 data.

Therefore, data above a C_i of 50 have not been plotted, and some of the points immedi ately below a C_i of 50 must remain in question.

Figures 6 and 7 are plots of percent compaction versus compaction index for all the

Figure 6. Compaction requirements of cohesive (plastic) soils for flexible airfie pavements, all data.

Figure 7. Compaction requirements of cohesionless (NP) soils for flexible airfield pavements, all data.

ata. The curves on these figures are the same as those shown in Figures 4 and 5. While at first glance it may appear that Figures 6 and 7 are an unrelated scatter of oints, the plots have meaning if it is accepted that the required degree of compaction ecreases with decreasing compaction index. On this basis the uppermost points in he right-hand portion in Figures 6 and 7 (the high C_i range) are considered to have relulted from compaction by aircraft traffic. On the other hand, densities indicated by he uppermost points to the left were not necessarily the result of compaction by air-|raft traffic. For instance, 90 to 95 percent of modified AASHO maximum compaction s commonly required throughout fill sections, with 95 to 100 percent required in the bp 6 in. of the subgrade. Also it is possible in some cases for cut sections to be at gher densities than those that will be produced by aircraft using the overlying pavehent. For these reasons, less importance should be attached to the high plotted points the left-hand portions of Figures 6 and 7. The absence of points indicating high denities in the very high C_i range in Figure 6 is due to the inability of cohesive materials exhibit these unusually high strengths at optimum moisture contents, as discussed reviously.

It was first thought that soil type as expressed by the plasticity index (PI) would be sufficiently critical parameter that it might be treated in a number of ranges, such

Figure 8. Compaction requirements for flexible airfield pavements.

TABLE 5

Depth of Compaction fbr Select Ifaterials and Subgrades

 $\overline{5}$

as nonplastic, 0-5 PI, 5-10 PI, 10-25 PI, etc. On analysis, however, it was found that distinctions could not be made between the various ranges of plasticity, and that only the separation into cohesive and colesionless (plasticity index zero or NP) *was* warranted. This finding was partly lue to the small differences between ranges and partly to the data being insuficient to establish such small differences. $\frac{w}{2}$
The percent compaction versus com-

The percent compaction versus comaction index curves (shown for both soil
ypes in Fig. 8) are the basis of the com-
action requirements shown in Table 5. ypes in Fig. 8) are the basis of the com- \ action requirements shown in Table 5. $\frac{1}{2}$
These are the requirements contained in $\frac{3}{2}$
he current (Aug. 1958) Corps of Figure These are the requirements contained in he current (Aug. 1958) Corps of Engieers' design manual for pavement areas ubject to normal traffic distribution. The lompaction indexes from Figure 8 were sed with the respective CBR design curve) determine the depth to which the various agrees of compaction should be specified tr subgrades with design CBR values less an 20. The depths are rounded off to te nearest half foot. As in previous isthe manual, the minimum compactures of the manual, the minimum compactor requirements for fills are specified on requirements for fills are specified 95 percent for cohesionless materials

Figure **9.** CBR design curves.

hd 90 percent for other soils. These are relatively moderate compaction requirements, he values shown in Table 5 for 80 and 85 percent compaction are intended for use in eluating the adequacy of the natural density in cut sections. Where the natural density less than the requirements, the soil must be compacted to the required density by Uing from the surface of the cut (not effective unless the moisture content at the time

gure 10. Example of density requirements .

of rolling is proper) or by removal and replacement in lifts.

As shown in Figure 8, indicated percentage of compaction for a compaction index of 20 and above (design CBR of 20 and above) is in excess of 100 percent. Compaction requirements for materials with design CBR values in excess of 20 (base courses, subbases, and high-strength subgrades) are given in Table 5 in a narrative form, rather than as a table, to emphasize the necessity for high degrees of compaction for these materials.

The compaction requirements indicated by the compaction index apply only to the problem of densification by traffic. The problem of the consolidation produced in subgrades and foundations by high fills is a soil mechanics problem.

Application to Civil Airfields and Highways

Figure 8 can be used to establish compaction requirements for civil airfields and for highways when CBR design curves are available. The procedures are illustrated by the following examples. Figure 9 shows CBR design curves for an 18,000-lb, single-axle load (from Fig. IV-2, very heavy traffic class, (3)), and for a Douglas DC-8 plane at 300,000 lb (from Fig. 4, (1)). The compaction index in Table 6 was read from Figure 8, and the corresponding thickness from Figure 9. For example, the compaction index for 95 percent of modified AASHO maximum density from Figure 3 is 3.5 for cohesionless soils and 8.6 for other soils. The compaction index is converted directly to design CBR (compaction index of 3.5, design CBR of 3.5) and the thicknesses read from the proper curve in Figure 9. For example for the 18,000-lb axle load, the thicknesses indicated from Figure 9 are 17 in. for cohesionless soils and 10 in. for other soils.

		Cohesionless Soils ¹		Cohesive Soils			
Compac-	Compaction	Thickness (in.		Compaction	Thickness (in.		
% tion,	Index	18.000-lb Axle	$DC-8$	Index	18,000-lb Axle	$DC-8$	
105	42		9				
100	9	10	32	19	6		
95	3.5	17	61	8.6	10	33	
90	1.8	27	92	5.0	14	49	
85		-		3.2	18	63	
80				2.4	22	79	

TABLE 6

 $1_{PI} = 0.$

Figure 10 is a plot of the percent compaction versus depth given in Table 6. Norm| ly, the curves in Figure 10 would be used to establish a step-pattern of compaction re quirements. For example, for the 18,000-lb axle load, 95 percent of modified AASH^ maximum density would be required to a depth of 14 in. from the finished surface of pavement, and 90 percent to a depth of 18 in., in cohesive soils. In cohesionless soi 100 percent of modified AASHO maximum density would be required to a depth of 15 i from the finished surface of the pavement, 95 percent to a depth of 27 in. The depth would probably be shifted an inch or two to coincide with a lift. Also, 95 percent wou probably be specified for all cohesionless fills, and 90 percent for other fills.

SUMMARY

The design CBR, termed the "Compaction Index," C_i , provides a means of combin ing into a single parameter the variables of load, tire arrangement, tire pressure, volume of traffic, and depth from the surface to the layer being studied. The relatioj developed by the Corps of Engineers Flexible Pavement Laboratory, between compa tion index and the required percentage of modified AASHO maximum density are pre-l sented. These relations can be used to develop compaction requirements for civil a' field and highway loadings. Examples of the procedures are given.

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EDWARD A. ABDUN-NUR, Consulting Engineer, Denver, Colorado-In developing design compaction requirements from the actual observations on compaction of the various layers in airfields subjected to actual and to accelerated traffic, the authors have given the profession a very realistic approach to design criteria-badly needed in this field. They are to be highly commended for such a fine piece of work.

Figures 4 and 5 are most interesting in that they form the basis of the relationship between compaction requirements and compaction index, from which the requirements at different depths for different wheel loads, arrangements and tire pressures are later derived. Figures 6 and 7 are still more interesting in that they contain a much larger population, even though part of it may not be as reliable as that in Figures 4 and 5. These figures represent, in essence, the basic data from which all the final relationships and conclusions in the paper are drawn.

The authors have very carefully and capably given various reasons and explanations for the scatter of the data exhibited in these figures. Additional reasons and explanations that have also been factors in this scatter, can no doubt be enumerated. Howeve irrespective of any reasons and explanations, this scatter must be accepted as a norm physical picture of any universe being studied. The very orderliness that the authors have implied must exist in the data, and which their explanations tried to justify, simp does not exist in nature or on any project.

With this in mind, the writer questions plotting the curves in these figures at what appears to be the 85 to 95 percentile of the universe. The effect of using such a high $\frac{1}{2}$ level for a basis of design is to inject a factor of safety that is not needed and the universe the cost of facilities designed to such standards. If to that will unjustifiably increase the cost of facilities designed to such standards. this is added the fact that such levels obtained from 85 or 95 percentile points are further used as minima, then the additional factors of safety interjected by this mechanis lose their practical justification.

It seems to the writer that a realistic approach would be to fit a curve around the average or mean of the data. This automatically allows for the scatter which is bound to result in the compaction on any construction job. If the ultra-conservative curves shown in these figures and the resulting increased cost are justified by other consider ations, then at least, the average requirement of compaction should be used instead of ations, the attention show $\frac{1}{2}$ is the average requirement of compaction show $\frac{1}{2}$ is the used instead of $\frac{1}{$

Control of c cal, and nearly impossible of attainment on a construction project. The reasons for this have been developed by the writer for portland cement concrete in a paper delive. ed at the 1961 Convention of the American Concrete Institute. They are just as applicable to soils, base courses, and bituminous concrete, except that the variations are of a different magnitude in each case. Control by maintaining an average compaction requirement that will assure a predetermined probability that no more than a predete mined percentage of the universe will fall below a given design figure is much more practical, represents the actual physical conditions on the job more realistically, and is obtainable. Such an approach has been used by the writer for several years, and h been recommended recently for compaction, as a result of the AASHO Road Test by W. N. Carey, Jr., J. F. Shook, and J. F. Reynolds in a paper presented at the 1960 Annual Meeting of the American Society for Testing Materials.

If such an average requirement is tied to the uniformity of a given contractor oper ation, a motivation can result that will improve the uniformity of the work far beyond that obtained by any degree of inspection.

that obtained by any degree of inspection.

W. H. CAMPEN, Manager, Omaha Testing Laboratories—Apparently the densities which are sufficient to produce required CBR values in subgrades, subbases and bases are not high enough to prevent further densification in the field by loaded tires. The authors therefore are proposing a method whereby the necessary degree of density can authors therefore are proposing a method whereby the necessary degree of density can
be specified for various depths of the lavered systems under different wheel loads and tire pressures.

Based on the usual relationship between density and CBR the procedure recommended will result in higher values of CBR. Theoretically the thicknesses should therefore be reduced. Has this point been given consideration?

The writer notices also that the sandy or cohesionless subbases attain much higher densities, in respect to designed densities, than other types of subbases. In the writer's opinion the results are to be expected because it is well known now that the impact method used in the laboratory in making the moisture-density test gives low results on cohesionless materials. A comparison of the results obtained with the impact method with hose obtained by the inundation-vibration method on ordinary sand may show the forme \sim 0 be only 92 of the latter.

C.R. FOSTER and R.G. AHLVIN, Closure-The authors agree that Mr. Abdun-Nur's proposal to use statistical quality control methods in the control of compaction is a good bne. The Waterways Experiment Station has made limited use of such methods in reis earch work involving repetitive density sampling. The Corps of Engineers, however, is not geared to use of such methods in connection with specification compliance deters not geared to use of such methods in connection with specification compliance deter-
pinations, and it will be some time before adequate service test trials and advanting inations, and it will be some time before adequate service test trials and education
If field personnel will permit their use f field personnel will permit their use.
In regard to the analysis in the paper

In regard to the analysis in the paper being discussed, it is doubtful that the methods
. Abdun-Nur proposes should be applied. As My Abdun Nunnaints and south in Ir. Abdun-Nur proposes should be applied. As Mr. Abdun-Nur points out, scatter is ound to occur in the compaction on any construction job. The data being analyzed, owever, are for a multitude of jobs and not just one. Essentially, each plotted point 1 the figures to which Mr. Abdun-Nur refers (4-7), represents a separate job and lerefore a separate universe in regard to the type of control proposed. An attempt to pply the same methods to the universe of universes represented by the data involves random treatment of unknowns and uncontrolled variables of such magnitude that the ariability is greater than the significant range in parameters. Also, such an attempt ould result in an average which would apply to a collection of subsequent constructions ich that half of these constructions would be satisfactory with a degree of conservatism mging upward from none, whereas the other would be unsatisfactory, ranging from ightly to greatly unsatisfactory.

Although the authors do not believe the methods proposed by Mr. Abdun-Nur apply to eir analysis, this in no way detracts from the merits of the methods, and one cannot il to recognize their advantages in regard to construction control.

Mr. Campen's question hews directly to the practical aspects of the interrelation of rength (CBR) and density, and reflects his intimate knowledge of the subject. A degn CBR value must be determined for each material used in a pavement structure, d design values necessarily depend on the density to be attained. It is, or has been, mmon practice to select design values from laboratory CBR test results based on a ven percentage of a standard density—frequently 90 or 95 percent of modified AASHO aximum density. Mr. Campen points out that where a higher density is required, a gher design CBR value may be selected.

Corps of Engineers' procedures specify a determination and plotting of CBR test re-Its for a range of moisture contents, densities, and compactive efforts from which sign CBR values are selected. Plots of data of this type permit selection of CBR de- ;n values for any pertinent values of moisture content and density.

The authors are glad to have Mr. Campen's comment on the agreement of his experice with theirs in regard to the ready attainment of higher densities in cohesionless .terials.

An Analysis of Hybla Valley Rigid Plate Bearing Data

G. RAGNAR INGIMARSSON, Research Assistant, Soil Mechanics Laboratory, University of Michigan, Ann Arbor

> This paper presents an analysis of some 89 rigid plate bearing tests, on 26 different flexible pavement sections at the experimental test track at Hybla Valley, Va. The test data are those reported by Benkelman and Williams (1_, Tables 4 and 7). The linear equation developed by W.S. Housel (2) is used in the analysis. Statistical results indicating the accuracy with which this linear equation reproduces the results of bearing capacity tests on different sizes of plates are presented. The analysis is carried to the point of determining the stress reactions developed by the flexible surfaces and the supporting subgrade; these results are presented graphically. Bearing capacity and resistance factors for different thicknesses of base and surface are compared. Use of a high-speed digital computer in this analysis is described. Also presented are methods of programming and a cost analysis.

HRB Special Report 46 *(})* contains data from rigid plate bearing tests carried out all the experimental test track at Hybla Valley, Va. Four different test procedures were employed; namely, the incremental, the incremental repetitional, the accelerated, ' and the repetitional.

The following analysis has been limited to the accelerated tests only. The data froi this test procedure were chosen because they provide a larger variety of pavement sed tions, subjected to a wider range of loadings, than do the other test data. Furthermol this test series is the only one in which a uniform rate of loading was maintained through out the series, permitting a valid comparison between load and settlement of differenti plate sizes and pavement thickness.

The symbols and abbreviations used in this paper are as follows:

- A = area of plates in square inches:
- B = thickness of stabilized aggregate base in inches;
- $D =$ diameter of plates in inches;
- K_1 = settlement coefficient ($\frac{A}{D}$);
- K_2 = stress reaction coefficient ($\frac{m}{n}$);
- m = perimeter shear in pounds per inch (pi);
- n = developed pressure in pounds per square inch (psi);
- $P = perimeter in inches;$
- p = unit load or bearing capacity in pounds per square inch (psi);
- t = total pavement thickness in inches;
- W = total load in pounds;
- Δ = deflection or settlement in inches;
- A.C. = thickness of asphaltic concrete in inches; and

Rem. = removed.

The accelerated test procedure consists of two parts, designated as the increment portion and the accelerated portion. The first part provides for application and release portion. of three individual loads of increasing magnitude, the period of application or releas being maintained until the rate of movement slows down to 0.001 in. in 15 sec. Foll

Figure 1. Load-deflection graph.

ng the release of the third load, the accelerated portion is carried out, providing for rate of vertical movement of the surface under a load applied at a settlement rate of 5 in. per min.

Figure 1 shows a typical load-deflection graph from the accelerated tests. As exected, there is a definite discontinuity in the graph at 0.4-in. deflection, due to the hange in rate of loading.

THE LINEAR EQUATION

In Housel's perimeter-shear theory (3), the bearing capacity or intensity of load is kpressed by the following straight line equation for a given amount of deflection:

> P $- A$ $-$

^I which

 $p =$ unit load or bearing capacity;

- m = perimeter shear, load per unit length;
- n = developed pressure, load per unit area;

 $P = perimeter;$ and

 $A = area$.

Figure 2 shows how a soil mass devels resistance to applied load in terms of rimeter shear, m, and developed presre, $n_1 + n_2$. It will be noted that all the id applied to the surface of the soil o- ;inates within the plate area. Below the frface some of the load is then distribulaterally as perimeter shear and the mainder transmitted directly down the itral column as developed pressure. Previous investigations of plate loading

Figure 2. Stress reactions in cohesive soil .

tests have shown that the magnitude and sequence in which these stress reactions are developed varies widely, depending on the relative rigidity of the bearing plate and supporting elements of the soil mass. In the normal case the perimeter shear and developed pressure are mobilized simultaneously, with both having positive magnitudes throughout the entire range of load and settlement. In relatively compressible materials the perimeter shear reaches limiting values first and developed pressure, indicated by concentration of pressure in the central column, follows as the final limit of supporting capacity.

Figure 3. Pressure transmission pavement, through

In layered systems, such as a flexible pavement, it has been found that the sequence in which the two basic stress reactions are developed is the same, but that the rates at which they are mobilized are controlled by the relative rigidity of the bearing plates and supporting elements of the pavement structure and subgrade (4). As the load is applied, an elastic depression forms under the bearing area; rigid plates tend to bridge this depression (Fig. 3) where the transmission of pressure concentration at the edge of the plate through granular paving mixtures has been visualized in terms of arching action. Similar pressure distribution takes place through cohesive mixtures where shearing resistance is the basic

Figure 4. Deflection of pavement under various sizes of plates .

reaction.

Pressure transmission through a flexible pavement structure is also influenced by the size and rigidity of the bearing plate (Fig. 4). In larger plates where pressure transmission from the perimete: is limited in magnitude or angle of pressure transmission from affecting the central zone, direct transmission of pressure down the central column becomes a factor These variations in pressure transmissioj must be included in the dimensional effect in plate loading tests and in their analysis^ in terms of the linear equation for bearing capacity.

The first question is whether or not it | is possible to express the bearing capacity of flexible pavements by this linear e-

quation. The second question is whether or not the stress reactions in this type of an alysis will reveal the significant structural behavior of flexible pavements, in spite of the variations which may occur in the sequence and magnitude of these reactions.

ANALYSIS OF DATA

As a first step in the analysis of the test data, it was decided to investigate how well the linear equation represented the relationship between the bearing pressures on the various plate sizes at a constant settlement.

In reviewing the typical load-deflection graph (Fig. 1), involving two different rate of loading, it was obvious that it would be necessary to treat the two portions of each load-deflection curve separately. To do this, it was necessary to estimate the no-lo deflection value for the two portions of each curve. Inasmuch as the primary objecti of loading tests is to determine the ultimate supporting capacity of the flexible pavements, further analysis was concentrated on the higher ranges of load and the initial

COMBINATIONS OF PLATE SIZES TO WHICH THE LINEAR EQUATION WAS APPLIED

25

Figure 6. Values of m and n for 3-in. A.C. surface.

Figure 7. Values of m and n for 3-in. A.C. removed.

Figure 8. Values of m and n for 6-in. A.C. surface.

Figure 9. Values of m and n for 6-in. A.C. removed.

Figure 10. Values of m and n for 9-in. A.C. surface.

Figure 11. Values of m and n for 9-in. A.C. removed.

repetitive loading cycle of the accelerated test procedure was considered as a seating process for the accelerated loading which followed.

The no-load deflections for the second portion of the curves could be decided on, either by extending the upper part of the curves graphically down to the abscissa or by ::onsidering the permanent settlement of the pavement after release of the last repetitive load as the no-load deflection.

Values obtained by the second method were used throughout the analysis; but, in nost cases, both methods gave practically identical values.

In Figure 5 the load-deflection diagrams for the accelerated loading from Figure 1 ave been reproduced with a common origin, hereafter referred to as zero deflection.

When all the test data given in Table 4 and Table 7 of HRB Special Report 46 had een treated as explained previously, the linear equation was tested for its capability J express the bearing capacity for various plate sizes at constant deflection. The lethod of least squares was used to determine the constants, m and n, in the linear quation.

It was realized in the beginning of the analysis that it would be advantageous to use high-speed computer to carry out the numerical work. For this purpose, the author Tote a program for the IBM 704 high-speed digital computer. Details of the proram are explained in the Appendix.

The linear equation was applied to three or four plates according to the available ita for each pavement section. Table 1 gives all the pavement sections and plate zes analyzed together as indicated.

The values for the stress reactions, m and n, obtained from the foregoing analyses •e plotted in Figures 6 through 12 for base course thicknesses shown on each curve, some cases, the values of m and n were obtained from three plates only, as indi- .ted on the graphs. Values of m and n for the same thickness of asphaltic concrete irface but with varying base thickness are grouped together, except in Figure 12 here results are shown from three pavement sections with varying thickness of as**laltic concrete laid on the subgrade with no base course.**

When the values of m and n in all test series had been obtained, the bearing capacity expressed by the linear equation was computed and compared to the measured values, tviations of the computed bearing capacity were expressed as percentages of the sasured values, and are presented in Figure 13 with percent of deviation as the abissa and the percentage of almost 2,000 cases as the ordinate.

DISCUSSION OF TEST RESULTS

As summarized in Figure 13, the agreement between the test results and bearing $\frac{A}{p}$ **icity at constant settlement computed by the linear equation is remarkably good, combinations of plate size and pavement thickness are represented in the statistianalysis; and, without exception, fall within the narrow range of experimental ershown. Ninety-two percent of all values fall within + 5 percent, and 99.6 percent** t
Lipped
Lipped **within the limits of** *t* **10 percent. Considering normal variations in construction .ctice, such results also demonstrate the excellent quality control exercised in the cing and placement of paving materials and in subgrade preparation.**

jThe data speak for themselves in answer to the first question, the validity of the fcar equation as a measure of the variation in bearing capacity with the size of load areas in the case of flexible pavements. The second question, whether or not the ess reactions in this equation can be broken down into factors which reflect signifi**t variations in the structural behavior of flexible pavements, is much more involved. \ review of the data in Figures 6 through 12 brings out several strong trends which consistent throughout the entire test series. Nevertheless, the complete interprelon of these stress reactions has proved to be peculiarly complex. In all cases, ^e is a large increase in the perimeter shear, m, as the pavement thickness is inised. This is perhaps quite obvious and could be anticipated. However, the mag-Jde of this increase is surprising and leads to other variations more difficult to ex- |n.**

TYPICAL LINEAR EQUATIONS

Figure 14 shows a set of linear equations for a typical test series for deflections of 0.2, $\bar{0}$.78, and 1.2 in. The plotted points show the accuracy with which the linear equation for bearing capacity reproduces the test results, illustrative of the data in Figure 13 for the entire series of tests. At the lowest deflection, 0.2 in., the bearing capacity is negative for the larger sizes of plates. This indicates that the larger plates will not develop positive supporting capacity until the pavement deflection or settlement exceeds that amount. Intercepts on the vertical axis give the values of developed pressure, n, at the indicated settlements. Negative values of n in the lower settlement

Figure 13. Percentage deviation of computed and observed bearing capacity.

range show that in this range the pressure is not being transmitted directly to the sub grade over the entire bearing plate. Such negative values of n are associated with hip values of perimeter shear, m, represented by the steeper slope of the straight lines Figure 14.

This variation in the stress reactions, m and n, shows that applied loads in the lo er range of settlement are being carried by pressure concentration at the edge of the bearing plates. This pressure concentration is then transmitted through the flexible ' pavement to the subgrade, where a substantial part of the perimeter shear will have been converted into developed pressure over the central column. Such results are no new, having been reported previously with partial explanations offered (4). Factors ' believed to produce these results have been shown in Figures 3 and 4 and discussed i a preliminary way. However, it is the quantitative evaluation of these reactions thati presents the difficult problem that has yet to be resolved.

The relation between load, settlement, and size of bearing area has been formula! in more general terms involving two soil resistance coefficients, K_1 and K_2 (3). settlement coefficient, K₁, has been defined as the ratio of settlement, Δ , divided by developed pressure, n $(K_1 = \Delta/n)$. This coefficient is analogous to the conventional

Figure 14. Typical linear equations.

pefficient of compressibility. The stress reaction coefficient, K_2 , has been defined s the ratio of perimeter shear, m, divided by developed pressure, n $(K_2 = m/n)$. K_2 ves the relative magnitude of these two types of resistance at any specified settlelent.

Maximum and minimum values of the soil resistance coefficients, K_1 and K_2 , have een identified as measures of the bearing capacity limit of supporting masses in terms static resistance. As shown in Figure 15, such maximum and minimum values ocir in tests on flexible surfaces when the developed pressure, n, is equal to zero. hen encountered in previous tests, another method of identifying the static resistance mit was available for confirmation. This confirmation was provided by extrapolating tes of settlement for various loads to obtain the yield value or load at which progresve settlement was zero. Incremental loading at constant time intervals was not used the Hybla Valley tests, hence this demonstrated procedure is not available.

In passing, it may be noted that the ultimate capacity of these surfaces is such that e total loads employed in the investigation provided only a limited range of pavement flection which was not sufficient to reach limiting values of the variables involved. ttlement for the 24-in. pavement thickness seldom exceeded 0.4 in., and most of e tests for the 18-in. pavement are also limited in the settlement range. Several ts on the 24-in. base thickness have been omitted as there were only one or two ints on the load-settlement diagrams, not enough to justify plotting.

The present tests produce the largest volume of comprehensive data confirming se more complex variations that has yet been available for study; the factual na-

ture of these data cannot be passed over lightly. The extended range over which nega **tive values of developed pressure occur is surprising and this, too, is a consistent** *rm* sult in all test series. In only a limited number of the tests has the loading been sufficient to produce a zero value of n, previously identified as the limit of static resistance in the pavement structure. However, there are a sufficient number of tests cap **ried to and beyond this critical range to provide a fairly adequate basis for further at alysis.**

It is hoped that such further study may throw some light on the source and characi

of these secondary effects. One possible approach that might be helpful is the nondimensional analysis presented by Kondner and Krizek (5). It is hoped that these investigators may follow up this suggestion and see what their analysis might contribute
to a solution of the problem. Housel has been following the author's work on the analysis of the loading tests from Hybla Valley, and presents a written discussion hereinafter. Perhaps others may come forward with other methods of analyzing these tests. The volume of data made available and the care with which it has been gathered have not been achieved in any previous investigation. Furthermore, the consistent variation in the stress reactions developed certainly justifies much more study on such an important problem in the design of a flexible pavement, the structural action of which is still quantitatively indeterminate in terms of the mechanics involved.

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Appendi x

USE OF HIGH-SPEED DIGITAL COMPUTERS

It may be assumed that in the near future there will be a very substantial increase **the use of high-speed digital computers in practically every field of engineering.** roblems involving time-consuming computations, which are repeated over and over Igain, are particularly adaptable to the use of high-speed computers.

Because the analysis of plate load bearing tests is at least partly this type of probim, the author took advantage of this opportunity and wrote a program which would ermit the use of a digital computer in carrying out the bulk of the numerical work.

 $\begin{bmatrix} 1 \\ 1 \\ 2 \end{bmatrix}$ A simplified flow-diagram which could be used for the evaluation of the stress retions, m and n from a set of data is shown in Figure 16. The flow-diagram is a aphical representation of the sequence of operations required to solve the problem question. It is absolutely independent of the computer or computer language used, It serves as a guide when one wishes to write a detailed program for a computer,
or those not acquainted with this representation, it may be helpful if the two symbols
"and "=" are defined. The symbol ":" means "Compare th it serves as a guide when one wishes to write a detailed program for a computer, " and "=" are defined. The symbol ":" means "Compare the variable on the left to le one on the right and choose between greater than $(>)$ or less than $(<)$, as indited. " The symbol "=" means "Make the value of the variable on the left equal to e current values of the terms on the right."

The IBM 704 computer which was available is a large-scale computer which em oys a special user's language called MAD, the Michigan Algorithm Decoder. The ogram was written in such a manner that it would be required only to feed the comter with the very minimum of information necessary to carry out the computations; d, when completed, the results would be printed or plotted in the most convenient :m.

Figure 17 shows a part of a data-deck which was used in this program. The first tu
DO
Tat
N 'd contains a title to be printed with the results. This may be any phrase the user loses, containing no more than 80 letters and blanks. The second card contains ne information pertaining to the computations themselves. The word "ROUND" inates that the plates used are round, and could be replaced by "SQUARE" or "REC- .NGLE." "DIMENSIONS" tells that the size of each plate is given in terms of dileter or sides, rather than "AREA." The next three numbers indicate the number

A **= Deflection**

- **PO** = Unit Load Observed **D** = Diameter of Plates
-

NO = Number of Plates Used PA = Perimeter-Area Ratio

Figure 16. Flow diagram for solution of stress reactions m and n.

of plates used, the number of deflection points to be computed, and the thickness of flexible pavement, respectively. "NO" means that it is not desired to call in the plot routine to produce a graphical representation of the results. The last two words indi cate the units used. The third card gives the plate sizes, and the observed data are ' listed on the following cards. The data are listed as the value of deflection followed by the unit pressure for each plate; for example, at 0.1-in. deflection, 63 psi, 42 psi, and 31 psi, for the 12-, 18-, and 24-in. plates, respectively. If the next test

Figure 17. Example of input deck.

eries in the deck were for the same sizes of plates, the word "ROUND" could be relaced by "SAME" which would prevent unnecessary duplication of computations aleady carried out for the preceding test series.

Figure 18 shows a typical page of printed output. Although an example of the ploted output is not available, this system includes a plot-routine which is capable of reparing graphs and plotting results at the rate of 400 points in a full-page graph in bout 2.5 sec.

It is not intended to list the complete program here. It is felt, however, that some arts of the program should be reproduced to indicate how the MAD language and other imilar languages are being developed to make the use of digital computers more acessible to a person who is not in a position to spend the time and energy to study the etails of the internal functions of the computer. It may be said today that learning
write programs in the MAD language (that is, learning to use the computer) is anlogous to learning to drive an automobile. One may perfect the former technique ithout acquiring much knowledge of computers themselves.

A very powerful statement in the MAD language is the "WHENEVER-Statement." p demonstrate this, reference is made to the input cards shown in Figure 17. De-Inding on the first and second words on Card 2, it is possible to deduce the P/A tio in various ways. For round and square plates, this may be as follows:

WHENEVER SHAPE .E. \$ SQUARE \$. .AND. SIZE .E. \$ AREAS \$ PERARE $(J) = 4. / SQRT$. (TEMP (I)) OR WHENEVER SHAPE .E. \$ ROUND \$. .AND. SIZE .E. \$ AREAS \$ PERARE (J) = 2. / SQRT. (TEMP (I) / 3.14) **OTHERWISE** PERARE (J) = 4. / TEMP (I) END OF CONDITIONAL

Most of the abbreviations used in the above sequence are self-explanatory. "TEMP

TEST SERIES 3 IN. AC REMOVED B = 6 IN., PLATE DIAMETERS = 12, 18, 24 IN.

Figure 18. Example of printed output.

(I)" is a location in the memory of the computer where "AREAS" or "DIMENS" are stored. ".E." means "same as."

Another very interesting statement is the "THROUGH-Statement." An example of this follows:

THROUGH D, FOR PLATE = 1,1, PLATE .G. PLNUMB SHEAR (SET, PLATE) = M (SET) PERARE (PLATE) COMPPR (SET, PLATE) = SHEAR (SET, PLATE) + N (SET) DIFFER (SET, PLATE) = (DEPRES (SET, PLATE + 1) - COMPPR $(SET, PLATE)$ D PERCT (SET, PLATE) = DIFFER (SET, PLATE) 100. / (DEPRES $(SET, PLATE + 1))$

The first instruction would sound like this in plain English: "Go through all computations up to and including those in Line D; first, by putting the parameter "PLAT! = 1," then, next time, by putting "PLATE = $1 + 1$," and so on until "PLATE" is great er than "PLNUMB"."

The parameter "SET" stands for the deflection point being computed; that is, first, second, and so on. "M (SET)" and "N (SET)" are the constants m and n in Housel's linear equation. "COMPPR (SET, PLATE)" stands for computed pressure or bearing capacity, and "DEPRES (SET, PLATE + 1)" for observed bearing capacity. "(DEPRES **capacity, and "DEPRES (SET, PLATE + 1)" for observed bearing capacity. "(DEPRES** (Set) $\frac{1}{2}$ is the amount of deflection, and $\frac{1}{2}$ involved is the number of plates

Any equality can be written in practically the same way one would when carrying out computations by hand. For example, if the stress coefficient **K**₁ referred to in this paper is to be computed, it is required only to add one instruction to the progra **this paper is to be computed, it is required only to add one instruction to the program.**

$$
K_1 \quad (SET) = DEPRES \quad (SET, 1) / N \quad (SET)
$$

It should be clear from this that programming in MAD is not a very difficult task. Input and output instructions can, however, be tedious; but, by no means hard to un-**Iderstand.**

The reader may be interested in getting an idea of the cost of carrying out the computations in this *prograna.*

Once the program has been written, the only requirement for processing data is to junch the data on cards, as shown in Figure 17. The punching is comparable to typewriting; hence, it would be difficult to give any definite figures as to how many cards me could expect to finish in a given time. This, however, would never be a very cost- " operation.

As an example of the cost of using the computer, it was found that the completion |>f 20 pages of output, as shown in Figure 18, took 1. 6 min. The computer charges '.re \$5,00 per min, and the foregoing would thus be about \$8.00.

The time consumed in writing and testing the program itself was, in this case, the hajor factor. However, if it were found desirable to use it for substantial computa-Uons, the cost of programming would eventually be negligible.

' One great advantage of the computer program is that it becomes easy and inexpenive to test out new theories and formulas which might be applicable to the program in uestion. Changes in the program itself are easy to make because instructions can be dded or removed as required without changing the output and input to any great extent.

This example of the use of a high-speed digital computer has been included here for lie reader who is not well acquainted with this powerful tool and who might be able to enefit from its use. It may be emphasized that it is not necessary to know the me-**Ihanical details of the computer itself to be able to use it, but merely to learn a rela- ^vely straightforward set of instructions such as those illustrated.**

Discussion

'.S. HOUSEL, Professor of Civil Engineering, University of Michigan, and Research lonsultant, Michigan State Highway Department—The writer has spent some time in an •tempt to interpret the stress reactions developed in the Hybla Valley tests in the antitative terms of the linear equation for bearing capacity used by the author, with**it coming to a final conclusion. This discussion will consequently be devoted to raisg several questions yet to be answered and commenting on certain aspects of the wuctural behavior of flexible pavements.**

^I **Statistically, the linear equation reproduces the measured results of all the tests wolved within a very narrow range of experimental error. Satisfying this test of %ldity does not reveal, in terms of structural behavior of the pavement structures, i of the factors which contribute to the surprisingly high values of perimeter shear,** *m* **inability of rigid plates to transmit direct pressure over the contact area, and the normally high deflections at which the full supporting capacity of the pavement struc- |:e is developed.**

The fact that the maximum and minimum values of soil resistance coefficients deed from the linear equation for bearing capacity do determine the upper limit of ,tic resistance or bearing capacity of the entire system has been demonstrated a nber of times in the design of building foundations (1^, 2). This relation has been

confirmed in previous rigid plate bearing tests on flexible pavements $(3, 4)$. If this principle is applied to the Hybla Valley tests, the limit of supporting capacity is not **reached until the deflection is much higher than the range of thousandths of an inch normally considered in current practice. For example, in Figure 15 the critical deflection at a developed pressure of n = 0 is reached at approximately 0.8 in. for a total pavement thickness of 9 in. As shown in Figure 6, the same limits are not even reached in the Hybla Valley tests and would be at deflections considerably greater than 1 in.**

Determining the source of these abnormally high deflections and correspondingly high values of perimeter shear is peculiarly perplexing. One may surmise that one possible source is in the permanent deformation due to yielding at the edges of the plate under the high pressure concentration along these edges. The increase in the **critical deflection with increased thickness of base course suggests that consolidation or stress conditioning of the base courses is another potential source. Similar permanent deformation in the subgrade is another possible source that cannot be neglected** If the high deflections originate from these sources rather than in shearing displace**ment, it is important to recognize that the pavement structures will improve with time and load applications in service and that this greater range of available supporting capacity may eventually be mobilized. Either that or the sources of permanent deformation must be eliminated by greater initial compaction or the pavement must be designed with greater flexibility in order to develop this supporting capacity more effectively**

In this respect, current pavement design in this country may be penalizing itself by **continued use of design criteria based on the elastic properties of rigid solids in which the assumed proportionality between total load and deflection takes precedence over th relationship between applied pressure and subgrade bearing capacity in plastic support ing media to which the linear equation for bearing capacity applies.**

Rigidity and strength under the conditions of pavement performance are not synonymous. Rigidity carries with it susceptibility to fracture and the weakness of brittle failures. The objective of pavement design should be to build flexible strength or controlled flexibility into pavement structures. For most efficient performance, relative rigidity of the pavement components should be reduced to a minimum. Rigid pavement **surfaces should be made more flexible or the supporting elements of base and subgrad** made more rigid. Flexible pavements have the advantage of mobilizing available sub**grade support more effectively. There should be no prejudice against larger deflections as long as the yield value of the supporting subgrade or other pavement components is not exceeded and the structural continuity and riding quality of the pavement itself is not impaired.**

This design philosophy calls for a rather definite reorientation of the current design practice which relies on proportionality between total load and deflection and relationships developed from the concept of a rigid pavement. It might be remarked tha one seldom sees steel wheels on a tea wagon; if there were, it might be as damaging **to polished floors of hardwood and tile as the pinpoint heels of current ladies' shoes '**

are to bituminous surfaces. ing tests may be in their relative rigidity and the secondary dimensional effects which ing tests may be in their relative rigidity and the secondary dimensional effects which
If you induce a **These offects annoy to mask the basic supporting capacity which the** they induce. These effects appear to mask the basic supporting capacity which the '
tasks attempt to mongure.

tests attempt to measure. bearing areas more nearly comparable to pneumatic tires. This procedure has been given some previous attention but has not yet supplanted the more common use of rigid plates adapted from foundation practice (5). Insofar as the writer is concerned, the attempt to unscramble the dimensional factors involved in perimeter shear and negative values of developed pressure has not been abandoned. There are some pron **negative values of developed pressure has not been abandoned. There are some promission ising possibilities not completely explored, but any further progress in this direction**

must await further study. ment design. By taking advantage of more liberal use of highly compacted granular ment design. By taking advantage of more inclusion of m_{ore} compacted gramming
cubbages and structural continuity sunnlied by prestressing and hydraulic compressi **subbases and structural continuity supplied by prestressing and hydraulic compressi** **units installed in the pavement base, surprising results are being obtained. In this connection, it has been reported that concrete pavements 3.5 to 7 in. thick are being generally built. One such pavement in Switzerland was reported to have been in ser**vice for several years under heavy traffic without having developed any cracks in **some miles of pavement. These are practical accomplishments to which pavement designers in this country should be alert if they wish to keep abreast of the continued developments in pavement design.**

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Comparative Studies of Combinations of Treated and Untreated Bases and Subbases for Flexible Pavements

CHARLES W. JOHNSON, Materials and Testing Engineer, New Mexico State Highway Department

> **New Mexico's experimental Project No. F-051-1 (8) was constructed to compare "upside down" stabilization with other base construction. The term was applied to the design because It called for the subbase material to be treated with cement.**

> **Nine experimental sections were constructed. The objective was to determine the effect of subbase stabilization compared to base course stabilization and the effect of a lower cement content in the base. Of particular interest is possible degradation of the mineral aggregates in all sections. The treated subbase sections should eliminate Intrusion of subgrade soils into the base.**

Through periodic inspections and check testing it Is hoped that better knowledge can be obtained to determine which design provides the best protection for future distortion and roughness. An attempt will be made to evaluate the various designs relative to costs and serviceability.

• THROUGHOUT NEW MEXICO there has been a growing conviction that a subbase treated to obtain greater stability will solve many road construction problems. New Mexico's experimental Project F-051-1 (8) was constructed to compare "upside down' stabilization with other base construction. The term was applied to the design because it called for the subbase material to be treated with cement. The concept of building with great strength directly over weak subgrade soils reverses the accepted principle of building stability gradually upward for flexible base construction.

The basic design feature of placing untreated base materials over a rigid subbase was incorporated into several projects rebuilt in 1954. Several old concrete pave**ments in the vicinity of Albuquerque had become so cracked and distorted that reconstruction was necessary. The old pavements were covered with 6 in. of untreated base material compacted and reshaped to typical section. Over the reshaped section** 2 in. of asphaltic hot plant mixed surfacing were placed. After six years of heavy traffic the surfaces remain in remarkably good condition. No reflective cracking has **developed and string line checks show little rutting or distortion. Prior to 1954, old concrete pavements were overlayed with asphaltic mixtures. The pavements continu to pump under traffic, and distortion rapidly developed. Usually within a year the crack patterns of the old concrete reflected through the asphaltic surface.**

In 1958, New Mexico commenced to use cement extensively to treat base course a **gregates. Pattern cracking which appeared in the surface course caused much concern among road builders.**

INTERSTATE 010-1 (8) 6, ROAD FORKS-EAST

On one New Mexico Project, I-OlO-l (8) 6, Road Forks—East, the contractor became alarmed when, after having completed approximately one-half the length of the project, pattern cracking appeared in the plant mixed surface course. He requested permission to change his operations and process the cement in the subbase aggregate He pointed out good reasons for the change: immediate protection of the subgrade fr **lurface moisture, better compaction of the untreated base because of a firmer founlation, reflective cracking in the surface course alleviated by a cushioning intermeliate layer, and in all probability a smoother-riding road. In New Mexico practically .11 cement treatments are processed by road mix methods. The time specified to rocess, compact, and shape the treated materials did not permit the necessary blade rork to obtain the smoothness desired for surface course placement.**

The New Mexico Highway Department had previously used variations of the upside own construction on urban projects where subgrade conditions were unfavorable to ood construction. Unstable subgrade soils caused by leaky water pipes and poor rainage were bridged by treating the subbase with cement. In all cases performance nder traffic appeared to be satisfactory. Because of the reasons stated *hy* **the con**ractor and the Department's previous experience, he was given permission to treat **le subbase instead of the base.**

Without any planning or much forethought all the features of an experimental proict were born. The contractor, in the interest of better flexible base construction, jreed to construct other variations of base and subbase stabilization at no additional)st to the state. Variations paired were (a) untreated base and subbase; (b) base)urse treated with *iVa* **percent cement and subbase treated with 3 percent cement; id (c) base course treated with** *lV»* **percent cement placed over an untreated subbase. hroughout the project 3 in. of asphaltic plant mixed surfacing were laid, except for** le section of the interstate connection where $1\frac{1}{2}$ in. of plant mix were placed over an **itreated base and a subbase treated with 3 percent cement.**

PRELIMINARY DISCUSSIONS, F-051-1 (8)

The materials and testing laboratory recommended the upside down design for seval projects. One of the projects so recommended was located on US 64 north of nta Fe, between Tesuque and Pojoaque. Samples taken from the subgrade soils ire found to be loaded with mica on which water acted rapidly and caused a greater ss of stability than normally expected for the soils encountered. It was thought that ment stabilization of the subbase would prevent any intrusion of the micaceous marials into the base.

Bureau of Public Roads engineers pointed out that the limited use of the design did t provide enough background for standard application. Following normal procedure 3y requested further justification and documentation before approval could be given r its use. Several conferences ensued and the facets of the design were discussed some detail.

The discussions disclosed opinions which differed on whether or not reflective icking was a forerunner of distress. Several engineers believed that cracking was iesirable but thought it could be alleviated by reducing the amount of cement used. Iiers thought that cement would be of little benefit unless slab strength were devel-Bd. Ideas about the upside down design centered on the untreated base course layer, e engineer felt strongly that the aggregates should be of top quality, well-graded, 1 the fines sandy and nonplastic. Samples tested from one of the Albuquerque prots, reconstructed in 1954, had plastic indexes ranging from five to seven. The ne engineer pointed out that the dynamic forces from moving loads were more or s confined within a granular layer and could be causing degradation of the aggrees which may have caused the material to be plastic. Project records showed le plasticity, but the issue was not clear.

Another engineer introduced the subject of asphalt. He believed that asphalticited materials would perform equally as well as cement-treated aggregates. Up-B down or right side up, reflective cracking would not be a problem. No one, so as is known, brought up the subject of lime. However, some conjecture developed ut the need of treating either base or subbase aggregates. Where was the proof any benefits existed? One thing was certain: Factual information supported by mtific data were not available for many of the ideas expressed.

INFORMATION ABOUT EXPER-IMENTAL SECTIONS

Eventually, treatment of the subbase with cement was chosen for the basic structural design of Project F-051-1 (8), but included were experimental sections each 2,000 ft long to make comparative studies of treated and untreated bases and subbases. The make-up of each experimental section was restricted to those discussed and about which the proponents seemed to have strong convictions. It might be said that the experimental Project F-051-1 (8) came about because of differences of opinion among engineers and a desire to know the truth.

It was agreed to construct each section to full stabilization, which in New Mexico is determined by the relationship between the traffic index and the California R. Values. Credit for gravel equivalent thickness of 1% times was taken for both the asphalt and cement stabiliza-

Figure 1. **Infonnation sign for Section H.**

Figure 2. Station 360+00, longitudinal cracking 1 ft in from inner edge of passin **lane, easttound roadway, August** 16, I96O.

ion where 4 percent additives were used and for the asphaltic surface course. No redit was taken for the Class C stabilization in the section using 2 percent cement.

The same company which built I-OlO-l (8) 6, **Road Forks—East, was awarded the ontract. The company tried earnestly to comply with each letter of the specifica**ions. R. L. Baker, project engineer, supervised the work. John Jaramillo, labor**tory technician from the central laboratory, inspected the work, lifted the samples, nd compiled the records. AU record samples were taken after the work was comleted and tested in the central laboratory. The top** 6 **in. of subgrade, the subbase, nd the base courses were specified to be compacted to a minimum of 95 percent modiied Proctor density. Density tests of the completed work show that compactions 'ell above the minimum requirements were generally obtained.**

Because of plastic and nonplastic requirements, two separate material pits were esignated for production of mineral aggregates for base, subbase, and surface contruction. One was located in the Pojoaque River, from which the nonplastic base nd surface course materials were obtained. The other was from a hill deposit which ontained natural fines compatible to obtain plastic indexes ranging from three to six.

To assist inspection of this project there are signs at the beginning and end of each esign change with information giving the stations and how each section is constructed *Tig.* **1). There are nine experimental test sections designated by letters A, B, C, D, , F, G, H, I. Section A is the control section and is typical of both right and left ines throughout the project, excepting the comparative experimental group B through All the comparative sections were constructed on the northbound lane.**

The contractor's superintendent was asked which of the experimental sections he id found the easiest to construct. He replied that he preferred either the asphalt-

Station 460+00, $\frac{1}{4}$ -in. rutting in outer wheel path of traffic lane, eastre 3. **bound roadway, August** l6, i960.

Figure *k.* **Cores taken fran experimental project Sections H and I .**

treated base or the upside down construction having a three to six plastic index in thel intermediate layer. The sandy nonplastic material was difficult to hold to the typical! section.

INSPECTION COMMENTS, F-051-1 (8)

On August 15, 1960, the first official examination of the completed experimental sections was made (Figs. 2 and 3). Observing the tests were W. L. Eager and L. H. Miller from the Bureau of Public Roads; and C.W. Johnson, and John J. Plese from **the New Mexico State Highway Department.**

Road roughnesses were measured with the Regional Bureau of Public Roads rough ness indicator through the experimental sections. It was desired to obtain initial **roughness readings before any change had occurred through traffic or natural conditions. All of the sections gave good readings, although there is some indication thatl** sections which have treated base course materials immediately under the mat are rougher than other sections. These results will be compared with future tests durin **the life of the experimental work. Tabulation of the results obtained are attached top the Appendices of this paper.**

String line checks were made on each section to determine if any rutting had devc oped from contractor's trucks hauling over the completed work. No rutting was fou^ *m* **any of the experimental sections on F-051-1 (8), Tesuque-Pojoaque.**

The only surface cracks found were in Sections Hand I, where the base was treated *f/ith* **cement immediately under the mat. Section H was treated with 4 percent cement md Section I was treated with 2 percent cement (Fig. 4). Transverse and pattern tracking were noted in both sections, but none were thought to be damaging as yet, rhe best indication of what to expect came from a previous survey of regularly-spaced ransverse shoulder cracks where the plant mix was laid** *1%* **in. thick. One hundred md thirty-six transverse cracks were found in Section H, where 4 percent cement was ised. One hundred and thirty-seven cracks were found in the shoulder of Section I, vhere 2 percent cement was used.**

On November 10, 1960, Benkelman beam deflections were measured at three sepa- 'ate locations of each experimental section. Using 10,800-lb wheel loads the average •esults ranged from 14. 4 to 24.0 thousandths of an inch, which was considered good. i.s could be expected, readings were high-

T for Sections E and F, where neither he base nor subbase were treated.

INSPECTION COMMENTS, I-OlO-l (8) 6

After one year of heavy traffic, rutting 1 the surface had developed to a depth of 4 in. on the Road Forks—East Project, -010-1 (8) 6. No pronounced differences ould be perceived in the upside down or onventional stabilizations. Longitudinal backs about 1 ft from the paved shoulder be pronounced in the passing lane from ation 326+15 to station 600+00, where e base was stabilized with 3 percent ceent. From station 600+00 to station 10+00, where the subbase was treated ith cement, the longitudinal cracks were cated in the paved shoulder about 2 ft er, relative to the other crack position.)ngitudinal cracks and rutting appear to more associated with soil and moisre conditions than with the design of se and subbase courses. The road from

Figure 5. Typical high shrinkage clay **soil in bed of dry lake, August** l6, i960.

ition 326+15 to station 800+00 traverses a shallow lake with alternately dry and wet Summer traffic seemed to have closed up most of the transverse re**ctive cracking from the cement-treated base. These cracks will no doubt tend to en up during colder weather. Roughness readings (tabulated in the Appendices) were newhat rougher than the initial readings recorded on F-051-1 (8). Inasmuch as ighness measurements were not taken immediately after construction on I-OlO-l (8) it is not known if traffic and weathering contribute to roughness.**

Information about design requirements and tests data covering compaction densities, Lghness measurements, and Benkelman beam readings for both I-OlO-l (8) 6 and F - • -1 (8), experimental projects is in the Appendices.

OBJECTIVES

jThe objectives of the comparative sections were to determine the effect of subbase bilization and the effects of other design variations.

Through periodic inspections and check testing it is hoped that better knowledge can •obtained to determine which design provides the best protection from future distor- 1 and roughness. Of particular interest is possible degradation of the mineral ag**gates in all sections. It is felt that the treated subbase sections should eliminate l-usion of subgrade soils into the base and therefore provide a good opportunity to**

determine if degradation is actually taking place. Assuming that it does take place, it would be desirable to know the rate and amount of degradation that can be expected before distress in the surface is indicated. Because reflective cracking has provoked so much discussion, the Department hopes to determine if this defect contributes to distortion and roughness developing in the riding surface.

Although economy was not considered in the original planning, everyone is interested in contract and maintenance costs. An attempt will be made to evaluate the various designs relative to costs and serviceability in the hope that a guide can be established to determine which is the best bargain for the money expended.

ACKNOWLEDGMENTS

The writer wishes to acknowledge the valuable assistance rendered by O. G. Betancourt, of the central laboratory, in the preparation of this paper.

Appendix A

F-058-1 (8) TESUQUE-POJOAQUE

EXPERIMENTAL PROJECT TEST SECTIONS

PROJECT F-051-1(8) TESUQUE - POJOAQUE

B . 0 . P. STA . 387+96 E.O.P . STA . 819+00 Test sections begin at Sta. 600+00 and end at Sta. 780+00

TEST *SECTIONS: A, B,* C, D, E, F , G, *H, I.*

Note: Section A is typical of both right and left lanes for the entire project, excluding test sections B through I.

*1 • Cement-treeted base course produced from Pit No. S8-126.S.

»2 . Untreoted bol e course and osphalt-treated base course produced from Pit No. 58-124.S (non-plostic materiel)

***3** . Untreated base course with P.I. from 3 to 6 produced from Pit. No. 58-126-S.

«4 - Subbase controlled gradation produced from Pit No. 58-124-S and Pit No. 58-126-S.

 \bullet , $\begin{array}{l} \sim \end{array}$) Plant mix and mineral aggregate for shoulder treatment produced from Pit No. 58-124-3.
#6)

AVERAGE DENSITIES OBTAINED DURING CONSTRUCTION New Mexico Project F-051-1 (8)

'cement-treated base

''asphalt-treated base; % theo. density

''asphalt-treated base; % lab. density

''subbase

Subgrade, subbase, untreated base, and cement-treated base: modified proctor density. Asphalt-treated base and plant mixed surfacing- Marshall hammer, 75 blows on each side.

SUMMARY OF SURFACE ROUGHNESS MEASUREMENTS New Mexico Project F-OS 1-1(8)

Tesuque-Pojoaque

August 15, 1960

NOTES: 3" Type One plant mix, 2 courses, on all sections

CTB = Cement Treated Base

ATB = Asphalt Treated Base

(1) = Outside or traffic lane

(2) = Inside or passing lane

Subbase = *2"* **maximum size, PI 6 or less**

BENKELMAN BEAM TEST RESULTS Project No. F-051-1(8) **Tesuque to Pojoaque**

All Tests Made in Driving Lane of North Bound Lane.

Appendix B

 $I-010-1$ (8) 6 ROAD FORKS-EAST

EXPERIMENTAL PROJECT TEST SECTIONS

PROJECT 1-010-1 (8)6

B.O.P. STA. 326+15.47

ROAD FORKS - EAST E.O.P. STA. 1088+28.4

TEST SECTIONS A, B, C, D, E, F, G, H.

Subbase Material produced from Pit No. 58-29-S. Base course, plant mix, and surface treatment aggregate produced from Pit No. 58-G2-S.

3" Plant Mix. Type I. l'Taper-10' Shoulder. It's Plant Mix. Type I 2 $\boldsymbol{\mathcal{A}}$ *naanaanaanaa* " Subbase . (Untreated) $STA.$ $326 + 15.47$ To 600+00 BO.P. Proj. I-010-1(8) 6 3" Plant Mix. Type Il'Taper-10° Shouldar. 142° Plant Mix. Type I 2 B^{\cdot} Base Course. (Untreated)
22222222222222222222 G" Jubbase. Cemant Treated. 3% dēt, 9" Subbase. (Untreated) End Anders navn av svenske geografis STA. 600+00 800+00 To 3" Plant Mix. Type I r Taper γ 10' Shoulder 1th" Plant Mix. Type I 2 $1.5%$ \mathcal{C} 1111111111 (Untrested) 14" Subbase STA. 800+00 820+00 To

3" Plant Mix. Type Il'Taper-10° Shouldar. 11/2" Plant Mix. Type I- \boldsymbol{G} Base Course . *Cement Treated* Basa Coursa. (Untraated 2223333333333333333 245332 STA. $990 +00$ 1036+54 To E.O.P. I-OIO-1(8)6 <u>IVz" Plant Mix. Type I'</u> 2222172 $\boldsymbol{\mathcal{H}}$ 350 Course. (Untreated. 22223333323232323232 6" Subbase. Camant Trasted. $\overline{3\%}$ St. Jubbase . [Universited] \bar{c} 1069+07

STA. 1036+54 Begin Connection.

End Connection.

CONDITION SURVEY New Mexico I-010-1(8)6 Road Forks - East August 16, 1960

a - In outer wheel path - traffic lane.

b - Dhere cracking marked "none" indicates could not be observed at this time - might be evident in cold weather.

c - μ_i^m plant mix mat - 3° 2-course plant mix all other sections

BENKELMAN BEAM TEST RESULTS N. M. Project No. *hOlO-l* **(8) 6, Road Forks - East**

DATE: 11-29-60 Wheel Load L = 10810, R-10800 **Experimental Sections**

Plate Bearing Tests and Flexible Pavement Design in Florida

W.H. ZIMPFER, Associate Professor of Civil Engineering, University of Florida, Gainesville

• FIELD PLATE BEARING TESTS have been performed since 1958 in conjunction with the flexible pavement design research program sponsored by the Florida State Road Department. The first field tests were run using the 3-sq in. (1. 95-in. diametej piston of the California Bearing Ratio test. This was followed by the use of 4-, 6-, 8-, 10- and 12-in. diameter rigid plate tests. The tests were initiated to obtain the bearing values of highway base, subbase and subgrade materials as separate layers and as composite pavement sections. All bearing values were related to the deflectio of the plate and the corresponding pressure on the plate. Recent tests have dealt with the bearing value of composite sections, including an asphalt concrete wearing surfac

The review of plate bearing tests, performed in the State of Florida, has been subdivided into sections that are directly related to the various phases of the research pi gram, including (a) plate size and zone of stress, (b) variation of bearing values, (< single layer relationships, (d) subgrade modulus as related to plate size, (e) two-la; theory relationships, (f) thickness of wearing surface, and (g) repetitional loads.

PLATE SIZE AND ZONE OF STRESS

When a circular plate is loaded with a uniform load a zone beneath the plate is stressed. For a homogeneous semi-infinite mass, vertical stresses and maximum shearing stresses may be readily calculated by the use of equations developed by JUr genson (1) , Love and others. Of particular interest, when investigating the stresses

Figure 1. Plate size and pressure bulba for plates and location of plate tests. associated with plate bearing tests on fie ible pavement layers, is the depth of the zone of significant stress as related to tl diameter of the loaded area. The stress zone is often defined by a "pressure bull which defines points of equal stress inte sity. Accurate pressure bulb or contouj of stress diagrams may be found in man publications. Some excellent diagrams appear in HRB Bulletin 114.

Figure 1a presents the pressure bulb corresponding to a vertical stress intend ty of 0.1 p for plates of 1.95-, 4-, and in. diameter. The depth of significant stress is about *1%* times the diameter. For the maximum shearing stress of 0. p the depth of significant stress is abou^ $1\frac{1}{4}$ times the diameter. As can be seen the stressed zone increases in depth as F the plate diameter increases. The CBF piston used for the original bearing test (1958) on base materials has a diamete of 1.95 in. Considering the stressed z under the piston it is obvious that the b ing value obtained is only a direct index

the strength of the base layer. Figure la also shows the stressed zone of the 12-in. diameter plate. It can be seen that for plate tests performed on the top of the base that a homogeneous mass of one layer does not exist throughout the stressed zone but a system of two layers is stressed. This system cannot be analyzed as a single layer but should be investigated as a layered system as was done by Burmister (2). Burmister's work is discussed later. :er's work is discussed later.

The effects of using a 1.95- and 12-in. diameter plate when testing a typical flexible >avement section are shown in Figure lb. The advantages and limitations of each size late are directly related to the depth and extent of the stressed zone. The small plate /ill give stress and displacement values of distinct and separate layers, whereas the arge plate will give values of the layered section. Realizing most wheel loads have ontact pressure areas that may be assumed circular, the use of the test data and theoetical stress computations for circular bearing areas may be used extensively for analsis.

	$5 - 1100$ (11100) (01000) (01001) , (0000)				
Average of Maximum Values Max. Values					
Material	$1.95 - In.$ Plate (CBR)	$4 - In.$ Plate	$8 - In.$ Plate	$12 - \overline{m}$. Plate	$1.95 - In.$ Plate (CBR)
	(a)	Standard CBR Tests			
ind clay	10				17
Imerock (N)	15				25
lmerock (S)	20				47
ab. shell lell	20				37
	25				49
	(b) Load Increment Tests, ASTM 1196-57				
ay sand (4)	35	25	20	15	35

TABLE 1

PERCENTAGE VARIATION OF BEARING VALUES. DACE CEUDY 1000

The early studies conducted in the state were with the 1.95-in. piston. The bearing its were run on all typical base materials throughout the state and on most subbase 1 subgrade materials. Results were presented in reports (3) issued in 1958. These rly tests established the strength characteristics of the individual layers and later, connection with other test data, led to the development of a modified CBR design thod. This was possible because if the properties of the distinct layers are known l/or specified for field construction, a system of layers may be proportioned empir-Uy which will have a known field performance. Later tests utilized 8- and 12-in. meter plates to develop the relationships of layered systems which were and are beinvestigated experimentally and theoretically.

VARIATION OF BEARING VALUES

the use of small plates has been investigated and was reported (4), in 1959. Con-
 the use of small plates has been investigated and was reported (4), in 1959. Con-
 the economy could be realized by performing tests w The use of small plates has been investigated and was reported (4) , in 1959. Contes; however, small plates tend to give erratic and somewhat inconsistent results in performing duplicate tests. Small plates are more sensitive to soil variations in logenity, large particles, and to surface conditions.

Irhe base study, noted previously, included data which is directly related to the var*m* of bearing values. The results of tests, repeated a minimum of three times, led le development of Table 1 which gives the average of the maximum percentage varin and the maximum percentage variation for the tests reported in 1958.

Collins (4) gives an indication of the maximum percentage variation of the 1.95-in. plate and, in addition, the variation of the plates of larger sizes may be estimated from the data. These data are also given in Table 1. The effect of larger plates in reducing the percentage variation is evident.

TABLE 2

NUMBER OF TESTS REQUIRED TO GIVE A MEAN WITHIN 10 PERCENT OF TRUE MEAN WITH 95 PERCENT CERTAINTY

The percentage variation varied with soil type. This is expected because, as men tioned previously, the scatter would be related to homogeneity, particle size and surface irregularities.

An attempt was made to analyze the data of Collins (4) using statistical methods. Sufficient data were not available for a reliable analysis; however, it is of interest to compare some preliminary calculations with those of Robinson and Lewis (5) who reported the results of a series of tests where 20 repetitions of each test were made to establish a true mean. The results of the study are given in Table 2. It may be note that no definite curve exists relating required number of tests and plate size but that a trend does appear. The number of tests required for the 6-in. plate is significantl less than the number required for the 1.95-in. plate. The 3-in. plate test results an

exceptional.
Using some of the data obtained in 1959, with a maximum of six repetitions of eac test, the number of tests required for identical criteria are noted in Table 2. Many test, the number of tests required for identical criteria are noted in Table 2. Many
1. Without use this tests are peopse my in this area of study to establish relationshi additional repetitive tests are necessary in this area of study to establish relationship.
hetwore alate size, pumber of tests required, and soil type. between plate size, number of tests required, and soil type.

SINGLE-LAYER RELATIONSHIPS

A review of the single-layer theory as related to stress and deflection beneath a circular rigid plate was presented in previous reports $(4, 6)$. The original problem of computing the stresses beneath a circular plate was solved by Boussinesq. Boussinesq obtained an equation for the deflection of a rigid plate located on a semi-infini elastic body as follows:

$$
w = \frac{\pi \text{ pr}}{2E} (1 - \mu^2)
$$

in which

w = deflection $\pi = 3.14$ p = pressure $r =$ radius of plate

E = modulus of elasticity
\n
$$
\mu
$$
 = Poisson's ratio
\nfor μ = 0.5
\n w = 1.18 $\frac{pr}{E}$ (average deflection of a rigid plate) for a flexible plate
\n w = 1.5 $\frac{pr}{E}$

["erzaghi, 1943, noted that soils were not truly elastic, but did retain the concept of ilasticity and essentially replaced E by a soil modulus, M, which was equal to Mo + .z. The resulting deflection equation may be written as

$$
w = K' \frac{pr}{Mo + az}
$$

vhen a = o and if w is constant, the pressure required to produce a given settlement *r* **is**

$$
p = \frac{w' \text{ Mo}}{K' r} = K \frac{1}{r}
$$

which

which

$$
K=\frac{w^r \text{ Mo}}{K^r}
$$

m a must fried, a family of curves may be constructed. for equation is that of a hyperbola. The equation $p = K - i s$ a theoretical re**nship between pressure for a given w and plate size. If the soil modulus, M, is**

SUBGRADE MODULUS AS RELATED TO PLATE SIZE

Reference 4 presented a set of curves developed from experimental data (Fig. 2), Jlating subgrade modulus, k, and diameter for various soil types. Noting that k is ual to the pressure at a given deflection divided by the deflection, it is possible to perimpose some theoretical curves of the p = K $\left(\frac{1}{r}\right)$ **type on the experimental data Lg. 2). The theoretical and test curves show good agreement for a = o. Three dif** rent soil modulus values have been plotted to present a typical family of curves. **The relationship between subgrade modulus and plate size may be expressed in many ys in mathematical form. Because the relationship between CBR (Load Increment st) and larger plate sizes is of primary interest in Florida and is essentially one of** parade modulus and plate size, the following equation is presented. CBR, plate size
a pressure are related by: **pressure are related by:**

$$
p = K \frac{1}{r}
$$
 (1)

•when w = 0,1 in., where 0.1 in. is the deflection of Standard CBR, the "CBR" E - .tion (Load Increment Test) becomes

$$
p = \frac{10(CBR)}{r}
$$
 (2)

•rhich

p = pressure, in psi; CBR = ratio at 0.10-in. penetration; and r = radius, in inches.

2 may be used to relate CBR, p, and r until additional test data are available. Isonable agreement exists between test and theory for CBR values greater than 10. litional testing is necessary to relate the results of the Standard CBR Test and the Id **Increment Test (ASTM, 1196-57 and (4)).**

The analysis of the two-layer system was developed and presented by Burmister in 1943 and most recently discussed in 1958 (7). An investigation related to the two-layered system was conducted in 1960 and reported (6). Before discussing the results of the recent tests some comments about the layered system may be desirable to visualize the action of a typical system. A typical two-layer system is shown in Figure la. This system represents much closer agreement to the actual problem that exists when pavement sections are loaded either by wheel loads or plates. The effectiveness of spreading load or reducing vertical stress, when a reinforcing layer with a modulus \overline{E}_1 is used over a second layer with a modulus E_2 less than E_1 , has been discussed and illustrated by Burmister (7) . The reduction is significant and the effectiveness of reduction increases as *Ei/Ea* increases. Another factor of importance in the two-layer system is that of an increase of vertical stress gradient toward the interface, which in turn causes a shearing stress buildup. The shearing stress, as mentioned by Burmister, is much more important than in the Boussinesq case and must be sustained at the interface for continuity between the layers. Shearing stress could lead to failure

Figure 2. 2. Subgrade modulus-diameter curves for some soils and theoretical curves.
due to excessive shearing strain; therefore, the deflection at the surface must be limited so that the shear stresses and strains are not critical. This limiting deflection may be about 0.05 in. for high-type flexible pavements constructed in Florida.

The deflection of a layered system as related to vertical stress and shear stress may be summarized by Burmister's influence curves of settlement coefficient, F_{w} (Fig. 3). The deflection equation for the layered system rigid plate is:

br

$$
w = 1.18 \frac{\text{pr}}{\text{E}_2} \qquad \text{F}_{\text{W}} \left[\frac{\text{r}}{\text{h}}, \frac{\text{E}_2}{\text{E}_1} \right] \tag{3}
$$

$$
w = 1.18 \frac{pr}{E_2} \qquad F_w \tag{4}
$$

 q . 4 is in the same form as the Boussinesq equation for one layer and reduces to this ase for a one-layer system. In the two-layer system the settlement coefficient curves re related to r, h and E_2/E_1 . The effect of these variables will be shown by the curves, oth test and theoretical, that follow.

The state conducted numerous tests on layered systems consisting of a typical Ocala merock base material and a clay-sand subbase. The base thickness was varied from to 11 in. in controlled sections over a 600-ft test area, to study the effect of the the r and thickness of layer h. The results of these tests are presented in some de-

il in an earlier report (6). ickness, h, of the reinforcing layer. Plates having diameters of 1.95, 4, 8, and 12 . were used on the different base course thickness to study the effect of radius of il in an earlier report (6).

Figure 4 shows the equipment used for some of the field testing, performed in conmction with the recent plate bearing test studies.

The data obtained in recent studies have been re-evaluated and important parts are |immarized and discussed.

To calculate the theoretical deflection, w, of the layered system, accurate values the moduli, E_2 and E_1 , are necessary. It has been found (8) that a minimum of thickess of soil at least 1.5 times the diameter of the loaded plate is necessary for calcula-

Figure 4.

tion of the modulus values and a thickness of twice the diameter is recommended.

Examination of numerous pressure deflection curves indicated that a straight line relationship did not extend much beyond a deflection of 0.05 in. and this was selected
for the calculations that follow. Early work used a deflection of 0.10 in., which appears to be too high for all materials, particularly limerock. Using a deflection of 0.05 in., the modulus E_2 may be calculated for a typical subbase as follows:

$$
E_2 = 1.18 \frac{pr}{w} \quad F_w
$$

= 1.18 $\frac{(220)}{0.05}$ (1) = 5,200 psi

'or this study, pr equaled the average product of the pressure (from ASTM 1196-57 nd (4)). times the radius for the 4-, 6-, 8-, 10- and 12-in. diameter plates. The epth of soil tested was in all cases equal to or greater than $4r$, and \overline{E}_1 = 20,000 psi. Tests are being performed during the summer of 1960 to evaluate E₁ for different ase materials. Bearing tests are run in a 7-ft x 7-ft pit using a 12-in. diameter ate. Base thicknesses are increased from 4 to 24 in., the latter thickness being sed to compute E_1 . Using this technique, the modulus value as well as the effect of trying the thickness, h, may be investigated. Two-layer influence curves are being •epared for typical systems.)

Having evaluated E_2 and E_1 and knowing the geometry of the section to be studied, lues of deflection, w, or pressure, p, for a given deflection may be computed from
irmister's equation: rmister's equation:

$$
w = 1.18 \frac{pr}{E_2} \qquad F_W \tag{6}
$$

which F_w is obtained from Figure 3.

re 5. Experimental and theoretical es—US 441—2-layer system study er I, **E**₁ = 20,000 psi, layer II **E**₂ = **5,200 psi).**

As part of the two-layer study, tests were conducted in a test pit as well as on US 441. Tests in this series were performed with 4-, 8- and 12-in, diameter plates and followed a procedure similar to ASTM Standard 1196-57.

The effect of varying plate size as well as base thickness is shown in Figure 5. The curves have been developed from US 441 test data. Agreement between theory and test is fair. The 4- and 8-in. plate test curves cross the theoretical curve showing minus and plus variation. This may be attributed to the fact that when the thicker base sections were constructed in two layers (2 in Fig. 5), density may have increased which would increase E_1 . Increasing E_1 from 20,000 to 25,000 psi for the test on the double lift base sections would result in reasonably good agreement between theory and test. This magnitude of increase is definitely possible.

The results of field tests conducted up to the present time indicate that the use of layered theory is quite promising. Some adjustment of the constants used in the Burmister theory may be necessary to predict the exact results obtained in the field. This is expected inasmuch as the

degree with which real conditions may agree with the idealized conditions is one of the major problems associated with the use of the theoretical equation of Burmister.

THICKNESS OF WEARING SURFACE

The most recent work completed, dealt with the effect of increasing the wearing sur face thickness and studying the effects on the strength and deformation characteristics of a two-layer system. The complete section was then subjected to repetitional loads. A Type-I asphaltic concrete surface was used in the research study and was tested as described in a recent report (8).

The effect of adding layers of wearing surface of 1.5-, 3-, and 4.5-in. total thick-

TABLE 3

EXPERIMENTAL AND THEORETICAL DATA OBTAINED FROM 8-IN. DIAMETER PLATE TESTS PERFORMED ON ASPHALTIC CONCRETE SURFACES OVER LIMEROCK BASE, 1960

ISurface thickness as notedj 2^-in. llmerock base; 8-i n. diameter rigi d plate; p = 200 psi ; Eo = 17,000 psl j and $E_2/E_1 = 1/1.6$, $\mu_1 = \mu_2 = 0.5$.

ness to a limerock base 24 in. thick did generally follow the layered system concepts The data indicate that the actual experimental deflection values are almost equal to the predicted values and the variation that exists between the different thicknesses of sur facing is within the range of experimental error. It appears that the two-layer theor is reasonable for predicting the behavior of the system investigated. Table 3 gives a comparison of experimental and theoretical data. Deflection values are given for a

400 300 PRESSURE (p s.l.) **200 A COMPRESSION OF A.C . SURFACE** 100 **B TOTAL COMPRESSION SURFACE AND BASE 1 I I** o $.05$ ċ **DEFLECTION** (inches)

Figure 6. Pressure deflection curves for 4i**-in. asphaltic concrete, type I over** limerock (LR) base, pit tests (E₂ = 17,-000 psi, $E_2/E_1 = 1/1.6$, $u_1 = u_2 = 0.5$.

Figure 7. **Compression of asphaltic coi Crete surface** (4 **in.) and of limero< base** (24 **in.) ,** 8**-in. diameter plate (E;** $E_1 = 1/1.6$.

Figure 8.

Figure 9. Increase in deflection and settlement with repetitions of a 12,000-1b load 8-in. diameter plate⁽⁸⁾.

pressure, p, of 200 psi. Figure 6 shows the actual pressure deflection curve for 4. in. of wearing surface as well as the theoretical curve obtained by using the two-layc theory.

This study clearly indicated the need for precise measurements of deflection when conducting this type of experiment. Accurate evaluation of the variables affecting the action of the layered system is also necessary to compare test results and theory. The theoretical computations were based on an estimate of the ratio of **Ea/Ei** obtainel from modified CBR tests. This is at best only an estimate and more exact values of the modulus of asphaltic concrete are necessary before any definite conclusions can made with regard to the use of layered theory for predicting the real behavior of wea ing surfaces. Experimentation is also needed to establish values of Poisson's ratio, μ , for asphaltic concrete as in all probability μ is not equal to μ ₂ as assumed.

An increase in the thickness of the surface course above 1. 5 in. had little effect < the slope of the straight line portion of the load deformation curve for the section. However, it is probable that the thicker wearing surface course would have a greate ultimate resistance and resist the shearing stress more effectively than the thin surl face and base section. Additional tests are necessary with thinner thicknesses of as phaltic concrete (0.75 in. to 2.5 in.). Additional tests are also needed where the range of E_2/E_1 is varied to cover the limits encountered on typical pavement section throughout the state and not only on limerock bases. Where three-layer systems an encountered, analysis similar to those presented by Burmister will be used.

The action of the combined section of asphaltic concrete and limerock base was that jf a layered system. Figure 7 shows the deflection both of the upper surface of the isphaltic concrete and of the surface of the limerock. Proportional amounts of delection exist throughout the deformation range tested.

Measurements were also made of the surface deflections surrounding the 8-in. di-Lmeter plate when subjected to a pressure of 80 psi. The deflected surface was typial of a layered system and extended outward from the center of the load a distance of bout four diameters. The deflection curve was almost parabolic and was similar to he surface deflection curves obtained when performing Benkelman beam tests on simlar pavement sections.

Figure 8 shows the field test arrangement used to obtain the compression and deection data for this study.

REPETrriONAL LOADS

One of the major problems is that of limiting the accumulated settlements associated ith repetitional loads. Extensive studies have been made and discussed by McLeod) on the effects of repetitional loads on settlements. As part of one of the bearing ate investigations a preliminary testing program was completed where 30 repetitions load (stress = 234 psi) were applied to a pavement section consisting of 4.5 in. of iphaltic concrete over 24 in. cf limerock base. The results are shown in Figure 9. le findings agreed with those obtained by McLeod. The relationships of deflection, ttlement and elastic deformation are summarized in this figure for an 8-in. diameter ate.

The extrapolation of the curves beyond the 30 repetitions to 100 appears to be justi- (d. Extrapolation beyond this range into the higher numbers of repetitions cannot be ade or justified at this time. Additional tests must be made in the range of 1,000 d 10,000 repetitions to establish the settlement relationships. Plans for building petitional load testing equipment have been made and tests should be initiated in 1961. The repetitional load equipment will permit evaluation of accumulated settlement ler repetitional loads as well as the effective soil modulus. The use of repetitional •id information along with layer system analysis should lead to a more realistic methof analysis of flexible pavements.

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Condition Surveys Used in Oklahoma to Evaluate Flexible Pavement Design

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THIS PAPER outlines the procedure of making flexible pavement condition surveys Ind its use in evaluating the flexible pavement design of the Oklahoma Highway Depart**lent.**

In cooperation with the Bureau of Public Roads the Oklahoma Highway Department litiated a comprehensive research study in 1955 to evaluate the flexible pavement deign adopted in 1947. The thickness design adopted in 1947 uses the California Bearig Ratio curves as given in HRB Proceedings, Vol. 22.

The pavement studied was selected from a list of projects consisting of 2,388 mi of exible pavement constructed after the rational method of design had been adopted in)47. Analysis of the projects indicated that five principal types of construction had sen used. The mileage of each type of construction in the sample selected was in •oportion to the total miles of each type of construction. The selected sample consted of 321 mi of two-lane pavement which had been constructed under 42 separate mtracts.

There are twelve soil problem areas in Oklahoma—so designated because the agri-Itural problems are similar throughout each area. Of these twelve areas, there are *re* **major areas which encompass approximately 80 percent of the state. This was the cond consideration in the selection of a test sample. The 42 projects selected for iidy were located within the five major problem areas. No other consideration was /en to the selection of projects than those previously mentioned.**

The study consisted of completing a testing program to evaluate the performance of 3 pavement and the compilation of historical and environmental data to be analyzed connection with the testing program. Procedures were written for assembling the ta, for analyzing it, and for making all tests. Some 40 items were included which ly be summarized into five general classes.

1. Construction Data. —The items in this group included information taken from the istruction plans; such as, typical pavement section, type of construction, and qualtests of materials made during construction.

2. Other Existing Data. - This group included geology, weather, original soil sur*ra,* **traffic data, and maintenance costs.**

3. Field Data. —This group included condition surveys of the pavement structure, ighometer surveys, field checks of the original soil surveys, and pedological soil •veys.

4. Field Tests. —Included plate bearing tests, Benkelman beam deflection tests, .d California Bearing Ratio tests, density tests, moisture tests, and the taking of iples for laboratory testing.

5. Laboratory Tests. —Included routine laboratory testing to determine whether d samples conformed to specifications for the subbase, base, and surface courses.

Many factors determine the performance of the pavement structure. It was intended nclude in this study all the principal factors that could possibly be evaluated. It was med necessary to obtain a factor for evaluation purposes which could represent the reciation of the pavement structure. Expended maintenance funds for the pavement icture were considered as partial payment for depreciation. The present condition he pavement structure was considered as the other part of depreciation.

To begin the study of depreciation, maintenance costs of each of the 42 construction

projects, as indicated by statistical records, were tabulated and reduced to 1950 costs All maintenance costs were then converted to a factor which represented the average cost per mile per year for each project. The average cost per mile for the contract construction of the pavement structure was obtained and converted to the 1950 cost. The average maintenance cost per mile per year was divided by the average cost per mile for contract construction, 1950 cost, to obtain a percentage factor which represented repaired depreciation. As previously mentioned, the present condition of the pavement structure was considered as the other part of depreciation. Unrepaired depreciation can be estimated by a condition survey and can be expressed as a percentage **of the cost of the pavement structure. Condition surveys require an estimation founde on the judgment of the individual, and the personal factor is a major consideration.**

For an observer to pass over an extent of pavement and mentally total up and reduc to an exact figure a number of areas of several kinds of defects, is an ability that will differ greatly among individuals. For long extents and many items, this ability probably varies greatly in the same individual at different times. To minimize the person al factor it is advisable to divide a project into a number of small parts and to evaluat each part separately. The final condition rating of the project can be made by average **ing the evaluation of the parts.**

To begin the condition surveys, reference points were painted on the surface of the pavement at each 0.2-mi longitudinal interval throughout the length of the project and numbered in consecutive order from the beginning. The exact stations from the construction plans were determined for each of the reference points. The reference poir were used as ties for the condition survey, soil and geological surveys, Benkelman beam deflection sites, and plate bearing sites.

To minimize and standardize the personal factor for rating purposes in making thel condition survey, the following terms, classifications, and ratings were adopted. Del inition of the terms used in describing the different characteristics of the classes is **as follows:**

The percentages are given as part of the total area of the extent rated. The classl ratings, and definition of the characteristics of the classes are as follows:

Excellent (98-100 percent)

1. No major or minor defects are apparent.

2. No maintenance has been performed.

Superior (90-97 percent)

1. There are no base failures or other major defects.

2. No structural maintenance has yet been necessary.

3. Any one or all of the following characteristics may be present within a 0.2| mi extent: (a) slight surface roughness; (b) slight cracking; and (c) the riding quali is impaired but very slightly.

Good (80-89 percent)

1. No base failures.

2. Any one or all of the following characteristics may be present within a 0.2 **2.** Any one or all of the following characteristics may be present which can be a 0.200 μ **mi extent: (a) some surface roughness; (b) some cracking; (c) slight raveling; ancfl (d) slight distortion. •**

Any one or all of the characteristics listed in the following classes may be presel within a 0.2-mi extent:

Average (65-79 percent)

1. Few localized base failures.

- **2. Considerable surface roughness.**
- **3. Considerable cracking.**
- **4. Some raveling, especially in the outer wheel lanes and along the edges**
- **5. Some distortion.**

Poor (50-64 percent)

- **T Considerable base failures.**
- **2. Extensive surface roughness.**
- **3. Cracking is extensive.**
- **4. The surface has raveled extensively throughout its width.**
- **5. Considerable distortion.**

Failure (Less than 50 percent)

- **1. Base failures are numerous and extensive.**
- **2. Distortion is extensive.**
- **3. Traffic hazards are extensive due to failures and distortion.**
- **4. Routine and special maintenance repairs have not been effective.**

If maintenance had been performed, the maintained area was rated in one of the pre- |eding classifications as to its effectiveness. A note was made in the remarks column ' the condition survey form regarding the type of maintenance that had been performed. *tther* **remarks included the general condition of the pavement structure. The final con**ition rating of a project was obtained by averaging the ratings of each 0.2 miles. Fig**t e 1 shows the condition survey form.**

A glossary of terms used in the condition survey follows:

Pavement Structure; The traveled portion of the road consisting of the subbase, base, and surface.

Surface Roughness; Inequalities in the pavement surface which adversely affect the riding quality.

- **Cracks; Approximately vertical cleavage due to natural causes or traffic action.**
	- **Transverse cracks—a crack which follows an approximate course at right angles to the center line.**
	- **B. Longitudinal cracks—a crack which follows an approximate course parallel to the centerline.**

CONDITION SUHVET DATA

- **C, Shrinkage cracks—interconnected cracks forming a series of large polygons usually with sharp corners or angles.**
- **D. Slippage cracks—frequently crescent-shaped cracks which usually point in the direction of the thrust of traffic.**

Stripping; The separation of bituminous films from aggregate particles.

Raveling: The progressive disintegration of the surface by the dislodgement of aggregate particles.

Distortion; Any type of irregularity tending to distort the pavement surface from

- A. Corrugations-transverse undulations at regular intervals in the surface of A. Corrugations — transverse unduced at $\frac{1}{2}$ intervals and crests not more than 2 ft a **the pavement consisting of alternate valleys and crests not more than 2 ft a-**
- part.
Waves-transverse undulations at regular intervals in the surface of the **B.** Waves—transverse undulations at regular intervals in the surface of the payement consisting of alternate valleys and crests 2 ft or more apart.
- C. Rutting-the formation of longitudinal depressions under traffic in the wheel **C. C.** $\sum_{i=1}^{n}$ **C.** $\sum_{i=1}^{n}$

Failure: Disintegration of the pavement structure.

- **A.** Alligator cracking-interlaced cracking of a bituminous surface course into small irregular blocks caused by inadequate base support.
- B. Shoving-lateral displacement of the pavement material due to the action of traffic. **B. Show in the showird displacement of the pavement of the particles due to any**
- **traffic.**
- cause.
D. Potholes-bowl-shaped holes of varying sizes in the pavement resulting from localized disintegration.

After the completion of the condition survey, the average condition rating of the project was computed and divided by the age of the project to obtain the average condi tion depreciation per year. This factor was considered as the unrepaired depreciation percentage and added to the repaired depreciation factor to obtain the total depreciati per mile per year as a percent of the contract construction cost based on 1950 costs.

The depreciation per mile per year of the pavement structure was used as a basic factor in the study to determine the relationship and effect of the following: **The department of the participation per year of the participation** \mathbf{A} is a basic beautiful as a basic \mathbf{A} basic \mathbf{A} basic \mathbf{A} basic \mathbf{A}

factor in the study in the study is and study in the study of the pavement structure as determined by parallel of the study of the study of the following study is and study in Leonard Study is and study is also study in L ing tests and Benkelman beam deflection tests.

- 2. Thickness of the "as built" pavement structure.
- 3. Traffic and wheel load densities.
-
- **4.** Soil and geological extents.
5. Climatic conditions.
- 6. Quality of subbase, base, and surface courses of the pavement structure.
- 7. The original construction cost of the pavement structure.
- **6. The original construction cost of the pavement structure.**
C. The prejulences cost since completion of the pavement structure. 8. The maintenance cost since completion of the pavement structure.

Although this study was started in 1955, the complete analysis has not as yet been completed. The relationship of items 2, 3, 4, 5, 7, and 8 to depreciation has been determined and is included in Part One of the Final Report of the Oklahoma Flexible Paving Research Project, 1958. Analysis is under way as to the effect of each of the items to total depreciation and will be published in Part Two of the Final Report whe **its to the published. its department of the published in Part Two of the Final Report when** $\mathbf{A} = \mathbf{A} \mathbf{A} \mathbf{A} \mathbf{A} \mathbf{A}$

c The pro reasonably good results. It was developed in 1955 prior to the first condition survey of the 42 projects. The procedure has been used for making surveys of the same pricets in 1957, 1959, and 1960. **of the 42 projects. The projects** is a project in the same projects of the same projects in the same projects.

The average condition depreciation per mile per year of the set research projects **The average condition depreciation of the 42 research per year of the 42 research per year of the 42 research projects**

Since the original condition survey was made in 1955, maintenance consisting of Ingle bituminous surface treatments has been placed on 19 of the 42 projects. The re ilts of the condition surveys indicate that the pavements are depreciating at a more ipid rate than was anticipated and maintenance performed has not been adequate.

The rapid depreciation also indicated that the pavement structure was underdesigned • the poorest soil types and resulted in the development of an interim design method, topted in 1958, which extended the design curve to give greater thickness of the paveent structure for the poorest soils. The interim design method consisted of the de**lopment of a subgrade index number ranging from 0 to 40 for soil characteristics jpendent on the plasticity index, liquid limit, and percent passing the No. 200 sieve, le relationship between the subgrade index numbers and the California Bearing Rao**s of the soils was determined, and the appropriate pavement thickness was deter**ined from standard CBR curves for subgrade index numbers. The subgrade index mber was then used in place of the standard CBR curves.**

Preliminary analysis indicates that factors other than strength of the subgrade soils ect the performance of the pavement structure and inadequate design results from jlure to provide for the other factors. Climatic environment, traffic, and wheel load insity are among the chief factors affecting the performance. One project included Ithe study gave almost perfect performance for approximately eight years while prelitation was below normal and then depreciated 38 percent in three years when rain- • l exceeded the normal average.

Another project on a secondary road gave good performance until heavy truck loads lasphalt were moved over it.

Another project performed good for a period of time and then the edges started fail- , probably due to a lack of shoulder width.

The condition survey, which resulted in the calculated depreciation, is being used *X* **basis for evaluation of flexible pavements. The relationship of depreciation to the Iny factors affecting performance is being determined by machine analysis. The end ^ult of the study will be a mathematical regression equation, including major factors, I designing flexible pavement thickness.**

Non-Dimensional Techniques Applied to Rigid Plate Bearing Tests on Flexible Pavements

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> **Non-dimensional techniques based on the methods of dimen**sional analysis provide a rational basis for analyzing rigid **plate bearing tests on flexible pavements. Test data re ported by Benkelman and Williams (1, Table 4) have been successfully analyzed by such techniques. The surface de**flection is explicitly expressed as a function of the applied **load, bearing plate diameter, pavement thickness, and the strength characteristics of the subgrade. Several illustrative examples are presented using the derived deflection equation to indicate possible applications. For the Hybla Valley data analyzed, the analysis shows that the load-carrying capacity of the flexible pavement as expressed by the surface deflection is dependent on the total pavement thickness and not on its proportion of asphaltic concrete or base course.**

NE of the most comprehensive field investigations of rigid plates bearing on flex**ible pavements is a cooperative study conducted by the U.S. Bureau of Public Roads,** the Asphalt Institute and the Highway Research Board on a specially constructed track at Hybla Valley near Alexandria, Virginia. The factual test data of the study are pre **sented in tabular form by Benkelman and Williams {!).**

Included are static rigid-plate bearing tests on full-scale pavement sections constructed on a minimum embankment of 5 feet of uniform A-7-6 soil (AASHO Classification–1949). The test sections of pavement were built with great care and every precaution was exercised to insure uniformity of thickness, compaction and composition of the various component layers. The soil used in the embankment was secured **from a previously prospected area and a high degree of uniformity of the material, both in composition and condition, was obtained. The first stages were completed 1946, whereas some sections were not placed until 1949.**

There are innumerable possible procedures for conducting static load tests. For any given pavement section the various controllable factors that may affect the result **of tests of this type include the magnitude of the load and the manner in which it is** applied, the number of applications and releases of a given load, the duration of each load application and release, and the size of the bearing plate. The data presented were obtained by the use of four different load-test procedures; namely, the incremental, the incremental-repetitional, the accelerated and the repetitional. The vast **majority of the tests were made with the accelerated and repetitional procedures.**

The incremental tests were conducted on 3-, 6-, and 9-in. asphaltic concrete su] face courses of a 24-in. base section using circular bearing plates of 1.954- and 3.568-in. diameters. The relatively small plate diameters, compared to the thickness of the surface course, confined the effects of the applied load to the surface course. Therefore such tests do not give a true indication of the load-carrying capacity of the pavement section. The most desirable procedure would have been to use the incremental test with 12-, 18-, 24- and 30-in. diameter bearing plates for surface deformations up to approximately 1 or 1.5 in.

The accelerated test procedure was conceived in a search for a method that woul produce the data sought and at the same time permit the conduct of a number *d* **test** **per day. It consists of two parts, an incremental portion (part a) which is a much ab-Sreviated version of the actual incremental test procedure mentioned, and an accelerited portion (part b). The incremental portion provides for the application and release, ince each, of three individual loads of increasing magnitude. The period of application)** release is maintained until the rate of movement slows to 0.001 in. per 15 sec.. The **oad magnitudes are such as to produce gross deflections of approximately 0.20, 0.30 md 0.40 in. for each of the three loads, respectively. Following the release of the hird load and after the movement-time criterion of the incremental portion has been atisfied, the accelerated portion of the test is begun. It consists of the continuous aplication of a load of varying magnitude which is controlled so as to produce a rate of ertical movement of the surface under test of 0.5 in. per min. The application of the)ad is continued until (a) the material is unable to support a further increase, or (b) le gross deflection exceeds 2.0 in. or (c) the total reaction load is used.**

hickness of Asphaltic Concrete a (in.)	Thickness of Base Course b (in.)	Bearing Plate Diameter d (in.)			
		12	18	24	30
3	ß	x	X	x	x
3	12	x	x	x	x
3	18	x	X	x	x
3	24	x	x	x	x
6	6	x	X	$\mathbf x$	
В	12	X	x	X	
6	18		X	x	x
Ð	24		x	x	x
9	6	x	X	x	
9	12	x	x	X	
9	18		X	x	x
g	24		x	x	x

FLEXIBLE PAVEMENT SECTIONS AND PLATE SIZES ANALYZED

Because the accelerated procedure is actually two types of test—an incremental, d creep test (quasi static) followed by a constant rate of deformation test—it is not isable to use the results for deformation greater than 0.4 in. which is the limiting lormation for the incremental portion. It would be possible to analyze a constant l e of deformation-type test if the incremental had not been conducted first, trhe incremental-repetitional tests were conducted on subgrades and the repetltional • s covered only small deformations. In addition, the tests conducted on the base course *Wri* **the asphaltic concrete removed were influenced by the confining effect of the surface**

After carefully examining the various test procedures, it was decided that the incremen**a r t of the accelerated tests given in Table 4 of HRB Special Report 46 (1) for the complete ement section is the most meaningful data and as such is the only data analyzed in this paper.)ne method of analysis using the results of the constant rate of deflection portion of accelerated procedure was presented by Inglmarrson (3), in which the linear e- ;ion of Housel's perimeter-shear theory is shown to be applicable. Ihgimarsson's ification of the constant rate of deflection data to eliminate the effects of the preng incremental portion is questionable. The results of Ingimarsson's paper are rented in terms of Housel's "perimeter-shear constant" and "developed-pressure itant" which are plotted as functions of the surface deflection. However, these re -**

TABLE 2

PHYSICAL QUANTITIES CONSIDERED FOR THE RIGID BEARING PLATE TESTS ON FLEXIBL E PAVEMENTS

sults are not expressed explicitly in terms of the parameters pertinent to the study. It is the purpose of this paper to study this same data by non-dimensional techniqu based on the variables involved in the investigation, and to develop an explicit function **al relationship among these variables. •**

THEORETICAL DEVELOPMENT

Although some of the concepts of dimensional analysis go back to the time of Galil and have been used in various ways by such investigators as Mariotte, Newton, Foui Stokes, Froude, Reynolds, Rayleigh, and others (3), the basic theorem was not forr ly presented and proved until 1914 by Buckingham74) in his famous Pi Theorem, A i general proof has more recently been given by Martinot-Lagarde (5). The general th of dimensional analysis has been illustrated by numerous authors, particularly in th field of fluid mechanics, and several books have been written on the subject; for ex ple, Bridgman (6), Murphy (7) and Langhaar (8). At present the senior author has be applying such techniques to a variety of problems in the field of soil mechanics (9, 1) **11, 12, 13, 14, 15). Because of the complex properties of the various pavement ma rials and the complicated interaction of these various layers with the loads being su** ported, it is felt that the use of non-dimensional techniques in both model and protot **research investigations of pavement problems would offer definite advantages with ^ gard to the cost, scope, and time for completion of such studies.**

Thus the study reported in this paper not only provides another analysis of a *pori* of the Hybla Valley test data, but of more importance, it illustrates and calls attent to the possible advantageous use of such a well-known general research tool as dime sional analysis in the field of pavement design. The authors are certainly not propd **any new theoretical methods, but are only calling attention to an existing research and illustrating one way in which such techniques can be extended into the practical pects of pavement design.**

Examples of the practical use of non-dimensional techniques, based on the method of dimensional analysis, in the area of soil mechanics have been given by Kondner ' 10, 12, 14, 15), Kondner and Edwards (11) and Kondner and Krizek (13),

The methods of dimensional analysis as used to determine relationships between ihysical quantities may be briefly summarized as follows; there are m physical quanities, containing n fundamental units, which can be related by an equation, then there

ment.

are (m-n) and only (m-n) independent, nondimensional parameters, called π terms, **which are arguments of an indeterminate, , • homogeneous function F .**

$$
F(\pi_1, \pi_2, \pi_3 \ldots \ldots \pi_{m-n}) = 0 \qquad (1)
$$

The physical quantities given in Table 2 have been selected for use in the dimensional analysis of the problem of the rigid plate bearing test on the surface of a flexible pavement. A force, length, time system of fundamental units has been used. Figure 1 is a typical cross-section of a flexible pavement showing the bearing plate, asphaltic concrete layer, base course and subgrade.

It is assumed that the material constants needed to describe the deformation charteristics of the cohesive soil subgrade are implicit in a characteristic soil strength rameter and the viscosity. The characteristic soil strength parameter used is the bximum unconfined compression strength of the soil. It may very well be that for the Inge of surface deflections being considered in this paper that the problem is primarone of deformation and not of failure. As such the soil moduli in compression and EXECUTE: Solven as the unconfined compressive strength. In addition previous work by a sonior outbox (10) on stress relaxion and areas changed in addition of a solvenium and **ar should be used instead of the shearing strength as given by the unconfined comssive strength, but with regard to practical application these quantities are not as senior author (10) on stress relaxation and creep characteristics of a cohesive soil Bicate that compression and shear moduli tend to be proportional to the maximum un- |ifined compressive strength. The viscosity controls the rate at which the deforman takes place and may include non-Newtonian effects. It is also assumed that the demation characteristics of the asphaltic concrete and the subbase are each controlled characteristic strength parameters and viscosities. The duration of loading is imtant in creep and viscous response. The effect of the geometry of the bearing plate [expressed by the cross-sectional area and the circumference.**

Because there are thirteen physical quantities and three fundamental units, there $\mathbf s$ ist be ten independent, non-dimensional $\boldsymbol{\pi}$ terms. By a methodical process pre**usly described by Kondner (9, 10, 11, 12) the following** π **terms can be obtained;**

$$
\pi_1 = \frac{F}{A\tau}, \quad \pi_2 = \frac{c^2}{A}, \quad \pi_3 = \frac{x}{c}, \quad \pi_4 = \frac{c}{h}, \quad \pi_5 = \frac{a}{c}, \quad \pi_6 = \frac{\tau t}{\eta}, \quad \pi_7 = \frac{k_1}{\tau}, \quad \pi_8 = \frac{k_3}{\tau},
$$

$$
\pi_9 = \frac{k_1 t}{c_1}, \quad \pi_{10} = \frac{k_2 t}{c_2}
$$
(2)

The above π terms can be substituted into Eq. 1 to obtain the function **F**. **| A general interpretation of these non-dimensional parameters has previously been e**n by Kondner (10, 12). The terms π_1 , π_7 , and π_8 express the strength ratios of the **grade, asphaltic concrete, and base course, respectively. The ratios of the time of fding to the relaxation time for the subgrade, asphaltic concrete, and base course are 21** by π ₆, π ₉, and π ₁₀, respectively. The term $\frac{c^2}{A}$ is a shape factor, and $\frac{c}{h}$ and $\frac{a}{c}$ **characteristic length ratios. For circular- and square-shaped plates the value of Is 417 and 16, respectively, regardless of the size. The settlement parameter is en as** $\frac{x}{c}$ **and is the dependent parameter for the study.**

Surface Deflection (inches)

Figure 2. Applied pressure versus surface deflection.

Figure 3. Non-dimensional plot: strength ratio versus deflection parameter.

The functional relationship given by Eq. 1 can be written as:

$$
\frac{x}{c} = \theta \left[\frac{F}{A\tau}, \frac{c^2}{A}, \frac{c}{h}, \frac{a}{c}, \frac{\tau t}{\eta}, \frac{k_1}{\tau}, \frac{k_2}{\tau}, \frac{k_2 t}{c_1}, \frac{k_2 t}{c_2} \right]
$$
(3)

EXPERIMENTAL RESULTS

For all of the Hybla Valley tests reported (1) , τ , η , k_1 , c_1 , k_2 and c_2 were mainined constant and hence π_7 , π_8 , π_9 , and π_{10} were also constant for the investigation **id can be eliminated from Eq. 3. This does not mean that the load-deflection relation ; independent of the type and quality of pavement materials, but only that the pavement aterials were constant for the data analyzed. It is to be expected that the curves giv-**1 **would in general be different for different pavement materials and perhaps even for fferent types of loading. Thus the analysis that follows is for the particular values of ITS , ITS , and IT 10 used at Hybla Valley. The tests were conducted in such a manner** as to minimize time effects and hence π_6 is relatively constant and can be dropped, ecause only circular bearing plates were used in the study, the diameter, d, expresses **} geometry of the bearing plate and replaces the perimeter and cross-sectional area, his leaves one dependent and three Independent variables which can be algebraically ansformed into the form given by Eq. 4. It is important to note that the new** π **terms** e the variables under consideration and not the individual physical quantities compos**the** π terms.

$$
\frac{x}{d} = \theta \cdot \left[\frac{F}{dh \tau}, \frac{d}{h}, \frac{a}{d} \right]
$$
 (4)

Figure 2 is a typical conventional plot of applied pressure versus surface deflection variousthicknessesof base course with a bearing plate of constant diameter and a count thickness of asphaltic concrete. The four different straight lines for various val-If of b indicate the apparent effect of the base course thickness; however inasmuch as a Ja constant, the variation in b is reflected as a variation in the total pavement thick-Bs h and, because d is a constant, the variation of b is expressed as a variation of ratio $\frac{1}{b}$. The same test results are plotted in Figure 3 in the non-dimensional form \mathbf{F} \mathbf{H} \mathbf{x} dimensional analysis as an experimental guide and the advantages of expressing eximental data in non-dimensional form. Because τ was constant for all tests, the **land in the dimensional form.** Because T was constant for all tests, the causer $\frac{F}{dh\tau}$ is proportional to $\frac{F}{dh}$ and is given for τ_{N} , a normalized value of τ e-**1** to unity. Figure 3 is not affected by the variation of $\frac{u}{b}$ and hence $\frac{u}{b}$ can be elimin**d** from Eq. 4. For these data the ratio $\frac{a}{d}$ was a constant value of 0.25. **Another conventional method of presenting the data is shown in Figure 4 where the lied pressure is plotted against the surface deflection for various values of the ;kness of the-asphaltic concrete with constant values for the plate diameter and the base thickness. Note the apparent influence of the thickness of asphaltic concrete. :ause the diameter of the plate is constant, this variation can be expressed in terms** \mathbf{F} \mathbf{F} \mathbf{x} $\frac{1}{2}$ is the same data plotted as $\frac{dh \tau}{dh \tau}$ versus $\frac{d}{d}$. The three curves of Fig-**4 are reduced to one curve in Figure 5. The same linear relationship of Figure 5 btained for base courses of 12, 18and24in. with a constant plate diameter of 18 in. repeating this analysis for plate diameters of 12, 24 and 30 in., a single resultant | v e can be obtained for each plate diameter (Fig. 6). Thus, the non-dimensional** ameter $\frac{a}{d}$ exerts very little influence on the phenomena and can be dropped from Eq. **F x The results of Figure 6 can also be obtained by plotting** *^^pf^* **versus ^ , as shown figure 3 for d = 24 in., for all the plate diameters.**

Surface Deflection (inches)

Figure 4. Applied pressure versus surface deflection.

Figure 5. Non-dimensional plot: strength ratio versus deflection parameter.

Figure 6. Strength ratio versus deflection parameter: variable plate parameter.

Figure 7. Strength ratio versus deflection parameter: normalized diameter.

The curves of Figure 6 can be reduced to the straight line of Figure 7 by normalizing with respect to the bearing plate diameter. Thus, the data of Table 4 (1) can be reduced to the relation given in Figure 7. Because the curve of Figure 7 is a straight line from the origin, the surface deflection as a function of the applied load, bearing **plate size, subgrade strength characteristics, and pavement characteristics can be written as**

$$
x = M \frac{F}{dh\tau} = \frac{F}{4dh\tau}
$$
 (5)

where M includes the effect of normalizing with respect to the diameter as well as the slope of the straight line. For the Hybla Valley study considered in this paper the factor **N** in Eq. 5 was found to be 1/4. Because of the normalization process the factor 1/4 in Eq. 5 has the units of inches. Eq. 5 is also based on an estimated value of the maximum unconfine compressive strength of the subgrade obtained from another report on the Hybla Valley Stu

(16). Because $\frac{F}{dh\tau}$ is non-dimensional, any system of compatible units may be used in **Eq. 5 and the value of the deflection will be given in inches.**

Because of possible variations in the properties of the subgrade, asphaltic concretel and base course, the results expressed by Eq. 5 or by Figure 7 for the Hybla Valley Study **may not apply to pavement sections in all localities of the country. It is felt that the** basic method of analysis given in Eq. 3 and applied to the Hybla Valley data could also **be applied in other localities to determine the necessary relationship to replace Eq .**

If the pavement response is linear as indicated in Figures 2 and 4, and if the **present techniques are applicable in other localities under various conditions, the procedure required to determine the factor M would be as follows. Determine the maximum unconfined compressive strength of the subgrade and then conduct sev**eral rigid plate bearing tests using several plates of different diameter, each with sev

F *xer* **eral applied loads. For each diameter plate used, plot versus ^ . To reduce**

these plots into a single relationship, select a convenient diameter as a normalizing factor and apply it to each plot. If the single resultant plot is a straight line, its slog **can be determined and divided into the plate diameter which was used as the normall**

izing factor in order to obtain the factor M to replace $\frac{1}{4}$ **in Eq. 5. If the resultant ple**

is not a straight line and its equation cannot be determined, the resultant plot itself should be used.

For the case of large surface deflections involving non-linearities Eq. 3 could als be used, but the procedure involved in determining the explicit form of Eq . 3 might l | considerably different.

ILLUSTRATIVE EXAMPLES

The following examples are given to illustrate the possible use of Eq. 5.

Example 1

Predict the surface deflection of a flexible pavement consisting of a 6-in. asphalt concrete surface course and a 12-in. dense-graded aggregate base course supported by a subgrade with a maximum unconfined compressive strength of 64 psi when teste in rigid plate bearing under an applied pressure, p, of 78 psi and a bearing plate diamet **of 24 in.** \blacksquare

Solution;

The total applied load is 35,400 lb and Eq. 5 gives

$$
x = \frac{F}{4dh\tau} = \frac{35,400}{4(24)(18)(64)} = 0.32 \text{ in.}
$$

This problem was randomly selected from Table 4 of Special Report 46 (1) and ha **a field deflection of 0.3 in.** The predicted deflection value given by Eq. 5 is 6.7 per **cent higher than the recorded value.**

Sample 2

Determine the applied pressure, p, necessary to cause a surface deflection of 0.2 in. 3r a flexible pavement section of a 3-in. asphaltic concrete and a 24-in. base course lyer on a subgrade with a maximum unconfined compressive strength of 64 psi when *isted* **with an 18 in. diameter, rigid bearing plate.**

Solution:

$$
p = \frac{4F}{\pi d^2} = \frac{4(4dh \tau x)}{\pi d^2} = 5.09 \frac{h \tau x}{d} = 5.09 \frac{27(64)(0.2)}{18} = 98 \text{ psi}
$$

The predicted value of 98 psi is 6.7 percent lower than the measured value of 105 li given in Special Report 46 (1^).

ample 3

The following hypothetical problem can be solved. It is necessary to design a flexile pavement on a cohesive subgrade with an unconfined compressive strength of 64 A certain design criteria states that the desired pavement section must be able **support a rigid bearing plate of 24-in. diameter under an applied pressure, p, of 136 • such that the surface deflection does not exceed 0.4 in. Determine the minimum vement section.**

Solution;

$$
h = \frac{F}{4d\tau x} = \frac{p \pi d^2}{4d\tau x(4)} = \frac{pd}{5.09 \tau x} = \frac{136(24)}{5.09(64)(0.4)} = 25 \text{ in.}
$$

The field tests indicate a pavement thickness of 24 in. Thus, the predicted value higher by approximately 4,2 percent.

The preceding examples illustrate some possible applications of the results develled in this paper. It may be possible to use these results, or other results developby the methods presented, as a basis for a design criteria for flexible pavements. In important to point out that the present results indicate that the load-deflection

aracteristics of flexible pavements are dependent on the total thickness of the section

d not on the ratio of asphaltic concrete surfac **s important to point out that the present results indicate that the load-deflection .racteristics of flexible pavements are dependent on the total thickness of the section viewpoint of riding characteristics and durability, under both normal wear and the |rerse conditions of water and frost action, the thickness of the surface course will quite important.**

CONCLUSIONS

Non-dimensional techniques based on the methods of dimensional analysis seem to pvide a rational basis for analyzing rigid plate bearing tests on flexible pavements. **The test data reported by Benkelman and Williams (1^, Table 4) has been successfulfenalyzed by such techniques. The surface deflection, x, in inches can be expressed lequational form as a function of the applied load, F , bearing plate diameter, d, pave-***Int* **thickness, h, and the unconfined compressive strength,** T **, of the subgrade in the owing form:**

$$
x = \frac{F}{4dh\tau}
$$

Several illustrative examples have been presented using this equation to indicate its sible application. Because of the test procedure used in the Hybla Valley Study this ation is restricted to surface deflections of approximately $\frac{1}{2}$ in. for flexible pave**its on cohesive subgrades. A significant result of the analysis is that the loadrying capacity of the flexible pavement as expressed by the surface deflection is de-Ident on the total pavement thickness and not on its proportion of asphaltic concrete ubbase. With regard to the durability of the pavement the thickness of the asphaltic •crete would be important.**

gThe results also indicate that it may be possible to use the non-dimensional method

in conjunction with durability studies to develop design criteria for flexible pavements. The authors recommend that additional field studies be conducted, using load creep
procedures with greater surface deflections, on flexible pavement sections supported procedures with greater surface deflections, on flexible pavement sections supported
by subgrodes of different unconfined compressive strengths subjected to various envir by subgrades of different unconfined compressive strengths subjected to various environ-
onmental conditions.

onmental conditions.
This study and other studies conducted by the senior author $(11, 12, 13, 14, 15)$ indicate that both model and prototype research investigations designed and conducted or the basis of non-dimensional techniques can help prevent unnecessary duplication of costly, time-consuming experimental work. Many times, tests which seem to be different because of different values of the physical quantities involved, are in reality duplicate tests giving the same results when examined in non-dimensional form. The reason for this is that in the search for an explicit relation expressing a physical phen menon, it is the values of the non-dimensional parameters, which are the new variabl that are important and not simply the magnitudes of the individual physical quantities. Thus it is felt that if such a program is designed and conducted on the basis of non-dimensional techniques, there is a better chance of developing rational design criteria with a minimum of expended effort.

Although the method of analysis is a general research tool and some recommendations are made for future work, the quantitative results of this paper were obtained solely from the results of the cooperative study of flexible pavements conducted at solely from the results of the cooperative study of flexible parameters of \mathcal{L} Hybla Valley.

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