DESIGN OF PRECAST PRESTRESSED BRIDGE GIRDERS MADE CONTINUOUS
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DESIGN OF PRECAST PRESTRESSED BRIDGE GIRDERS MADE CONTINUOUS

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AREAS OF INTEREST
Structures Design and Performance
Construction
(Highway Transportation, Public Transit)

TRANSPORTATION RESEARCH BOARD
NATIONAL RESEARCH COUNCIL
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Systematic, well-designed research provides the most effective approach to the solution of many problems facing highway administrators and engineers. Often, highway problems are of local interest and can best be studied by highway departments individually or in cooperation with their state universities and others. However, the accelerating growth of highway transportation develops increasingly complex problems of wide interest to highway authorities. These problems are best studied through a coordinated program of cooperative research.

In recognition of these needs, the highway administrators of the American Association of State Highway and Transportation Officials initiated in 1962 an objective national highway research program employing modern scientific techniques. This program is supported on a continuing basis by funds from participating member states of the Association and it receives the full cooperation and support of the Federal Highway Administration, United States Department of Transportation.

The Transportation Research Board of the National Research Council was requested by the Association to administer the research program because of the Board’s recognized objectivity and understanding of modern research practices. The Board is uniquely suited for this purpose as: it maintains an extensive committee structure from which authorities on any highway transportation subject may be drawn; it possesses avenues of communications and cooperation with federal, state, and local governmental agencies, universities, and industry; its relationship to the National Research Council is an insurance of objectivity; it maintains a full-time research correlation staff of specialists in highway transportation matters to bring the findings of research directly to those who are in a position to use them.

The program is developed on the basis of research needs identified by chief administrators of the highway and transportation departments and by committees of AASHTO. Each year, specific areas of research needs to be included in the program are proposed to the National Research Council and the Board by the American Association of State Highway and Transportation Officials. Research projects to fulfill these needs are defined by the Board, and qualified research agencies are selected from those that have submitted proposals. Administration and surveillance of research contracts are the responsibilities of the National Research Council and the Transportation Research Board.

The needs for highway research are many, and the National Cooperative Highway Research Program can make significant contributions to the solution of highway transportation problems of mutual concern to many responsible groups. The program, however, is intended to complement rather than to substitute for or duplicate other highway research programs.
This report contains the findings of a study that was performed to develop procedures for the computation of design moments in precast prestressed bridge girders made continuous through connections in cast-in-place slabs and diaphragms at bridge piers. Based on these procedures, recommended specification provisions have been developed that can ensure more rational design and economical construction for simple-span precast prestressed bridge girders made continuous. The recommended procedures and specifications are based on a comprehensive experimental and analytical research program. The contents of this report will be of immediate interest and use to bridge engineers, researchers, specification writing bodies, and others concerned with the design and performance of precast prestressed bridge girders made continuous.

The design and construction of bridges composed of simple-span, pretensioned girders made continuous for composite dead loads and for live loads has become widespread. In general, the design of these structures has been based on the procedures outlined in "Design of Continuous Highway Bridges with Precast, Prestressed Concrete Girders," which was published by the Portland Cement Association (PCA) in 1969. Although existing bridges designed by these procedures are generally performing well, it is believed that this method may not accurately predict the true behavior of these structures in light of new knowledge regarding material properties and behavior, new methods of analysis, and expansion of this concept to longer spans and wider girder spacings.

One of the major uncertainties in the design of these structures is the prediction of the elastic, inelastic, time-dependent, and ultimate positive and negative moments at the cast-in-place connections at bridge piers. This uncertainty is caused by a number of different loading and construction stages, time-dependent effects, and the details used to make connections. Because of these uncertainties and the lack of guidance in the AASHTO Standard Specifications for Highway Bridges, widespread differences exist in applying the results of the PCA procedure for selecting the continuity moments used for the connection design at the piers.

NCHRP Project 12-29, "Design of Simple-Span Precast Prestressed Bridge Girders Made Continuous," was initiated with the objective of resolving the uncertainties in the prediction of positive and negative moments for the design of the connections in precast prestressed bridge girders made continuous. The research included experimental investigations of concrete creep and shrinkage, and analytical investigations of typical bridge designs accounting for the time-dependent nature of the materials.
and loading stages. The work was performed by Construction Technology Laboratories, Inc., in Skokie, Illinois.

This report summarizes the findings from that study. The report contains recommended procedures for determining the positive and negative moments at the cast-in-place connections, recommended specification provisions for incorporation into the AASHTO Standard Specifications for Highway Bridges, and a description of a simplified computer program that will calculate the design moments. The recommended specification provisions may be considered for adoption by AASHTO in 1990.

The report notes that time-dependent effects and various construction timing sequences must be considered for service-moment design. Continuity will result in a reduction of midspan positive design moments for the prestressed girder. Recommended combinations of girder age at time of deck and diaphragm casting, and age at application of live load for analyses to determine maximum service moment, are also contained in the report. The report also notes that there is no structural advantage in providing positive moment reinforcement at the supports, and it can therefore be omitted, leading to economies in construction. The improved analysis and design procedures developed in this study will provide a more rational design and simplify construction of this type of bridge.

Two computer programs that will calculate service moments were developed during the study. The programs, which are fully described and documented in Appendix E, will operate on an IBM PC or compatible computer. The programs are not included in this report, nor are they available from the Transportation Research Board. They can be obtained from the McTrans Software Center. Interested parties should contact McTrans and ask for computer programs BRIDGERM and BRIDGELL. McTrans can be reached at: The Center for Microcomputers in Transportation, University of Florida, 512 Weil Hall, Gainesville, Florida 32611 (904/392-0378).
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The research reported herein was performed under NCHRP Project 12-29 by Construction Technology Laboratories (CTL), Skokie, Illinois. Ralph G. Oesterle, Manager, Structural Analytical Section, served as Principal Investigator. He was assisted by Joseph D. Gilkin, Senior Engineer, and Steven C. Larson, Engineer, Structural Analytical Section. Timothy R. Overman, Engineer, Structural Development Section, assisted in implementation of the computer programs. Basile G. Rabbat, Manager, Structural Codes, Portland Cement Association, served as a consultant to CTL.

A special acknowledgment is made to the four precast concrete manufacturers who supplied concrete cylinders for the creep and shrinkage tests. Also sincere appreciation is expressed to the respondents of the questionnaire for their time and efforts.
This study was carried out to resolve uncertainties associated with behavior and design provisions for bridges constructed with precast prestressed girders and a continuous deck. The girders behave as simple-spans for dead load. However, with the continuous deck providing a negative moment connection at support piers, the bridge girders may behave as a continuous structure for loads applied after casting the deck and diaphragms. The degree of continuity depends on time-dependent material behavior. Current criteria for design in the AASHTO Standard Specifications for Highway Bridges is vague. The appropriateness of design methods currently in use are uncertain because of the complexity of time-dependent behavior and construction sequences. Common practice includes design provisions for a positive moment connection in the diaphragms. Construction of the positive moment connection is generally cumbersome, time consuming, and costly.

The first task of NCHRP Project 12-29 was a compilation of current knowledge. A literature review was conducted and a questionnaire was distributed to state departments of transportation, bridge designers, and precasters. Also, creep and shrinkage tests were performed to provide data on steam-cured concrete loaded at an early age. From this information, analytical techniques capable of simulation of the complex behavior were determined. Also, potential variations in design parameters were selected in order to study the expected range of behavior for this type of bridge.

A series of computer simulations was carried out to study the effects of variation in time-dependent material behavior and variation in bridge design parameters on the resultant service moments in the bridge girders. Results indicated that the positive moment connection in the diaphragms does not provide any structural advantage and is not required. Also, results show that effective continuity can vary from 0 to 100 percent with variation in time-dependent effects. Also, construction timing has a major influence on resulting effective continuity. Maximum potential continuity occurs with a combination of the deck and diaphragms cast on relatively older girders, and relatively early application of live load. This combination, however, also produces the highest potential for transverse cracking in the deck over the supports. Cracking reduces the stiffness of the negative moment connection and limits the effective reliable continuity moment to a value equal to 125 percent of the negative cracking moment.

Maximum potential for loss of continuity occurs with a combination of deck and diaphragms cast on relatively young girders, and late age application of live load. Variations in construction sequencing of casting the deck before the diaphragms, or casting the diaphragms before the deck, have only minor influence on resulting service moments.

A series of computer simulations was carried out to study the influence of the amount of deck reinforcement and the girder cross-sectional shape on the potential for premature crushing of the bottom flange of the girders near the supports. Results indicate that limiting the negative moment reinforcement ratio, \( \rho \), to a value less than...
or equal to 0.5 $\rho_b$ will ensure ductile behavior and attainment of maximum girder strength. The balanced reinforcement ratio, $\rho_b$, must be calculated considering the depth-to-neutral axis and bottom flange geometry as described in this report.

Time-dependent effects and various construction timing sequences must be considered for service moment design. Continuity will result in a reduction of midspan positive design moments for the prestressed girder. Recommended combinations of girder age at time of deck and diaphragm casting, and age at application of live load for analyses to determine service moments, are contained in this report. Computer programs developed in this project and capable of running on IBM PC and compatible computers are available to calculate the service moments. Proposed revisions to the AASHTO Specifications along with a Commentary to define design requirements for this type of bridge are also included in this report.

CHAPTER ONE

INTRODUCTION AND RESEARCH APPROACH

PROBLEM STATEMENT AND RESEARCH OBJECTIVES

Application of precast, prestressed girders to bridge construction started in the United States in the early 1950's. Use of pretensioned I-girders with cast-in-place concrete decks grew rapidly. Until the early 1960's, bridges built with pretensioned I-girders and cast-in-place concrete decks were designed as simply supported spans. However, longitudinal reinforcement placed in continuous deck slabs above the piers provided negative moment capacity. Therefore, these I-girders could be considered as partially continuous for negative moments at the piers. The degree of continuity depends on the time-dependent effects and the effective stiffness of the moment connection provided at the piers.

In a pretensioned member, prestress will usually cause the member to camber. If the member is simply supported, the ends of the member will tend to rotate, as shown in Figure 1(a). When members are made continuous through positive and negative moment connections at the piers, the ends of the pretensioned girder are restrained from rotating. As a result, a positive restraint moment, as shown in Figure 1(b), may occur at the pier. Positive moment also occurs at the piers when alternate spans are loaded.

In 1961, the Portland Cement Association (PCA) conducted an experimental research program on this type of bridge. The research program studied the influences of creep in the precast girders and differential shrinkage between the precast girders and the cast-in-place deck slab on continuity behavior after an extended period of time. As a result of these studies, procedures were developed for design of the positive moment connection and the negative moment reinforcement over supporting piers. Reinforcement for positive moment connection is designed for the summation of positive moment due to time-dependent effects and live load application. Construction of the positive moment connection detail is generally expensive and time consuming.

Although existing bridges designed by the PCA procedure are generally performing well, it is believed that this method may not accurately predict the true behavior of these structures. Since the PCA research was completed over two decades ago, there have been significant advancements in understanding of the time-dependent effects of creep and shrinkage in concrete. Recent research has also made it possible to refine computations for prestress losses. In addition, inexpensive computers with large capacity are currently available. These advancements make

![Figure 1. Two-span bridge with precast, prestressed girders made continuous.](image-url)
it possible to perform more rigorous analyses of prestressed bridge girders made continuous.

There are several uncertainties associated with the PCA procedures. Some of the uncertainty stems from the simplifying assumptions made in the PCA procedures. One assumption is that girder concrete and deck concrete have the same creep and shrinkage properties. This would not generally be the case, particularly if the sequence of construction results in significantly different ages between the girder, diaphragm, and deck concrete. Different concrete mixes and curing conditions for girder, diaphragm, and deck concretes also cause differences in creep and shrinkage properties. Also, for the PCA simplified analyses, the continuity connections are considered to have zero length and to be fully rigid. Full continuity is assumed in calculation of live load positive and negative moments. The actual connections have finite lengths and rotational stiffnesses. The moment of inertia of the reinforced concrete section at the connection after cracking from either positive or negative moment will be significantly lower than the moment of inertia of prestressed girder section. In addition, when positive restraint moment from time-dependent effects causes cracking in the diaphragm concrete, these cracks must close before the full section becomes effective for negative live load moment.

Because of the various design methods, construction sequences, connection details, and materials in use in different states, the degree of continuity which develops at supports of this type of bridge varies significantly. Because of uncertainty in prediction of the positive and negative moments and because of the lack of guidance in the AASHTO Specifications, widespread differences exist in the design approach used for the connections at the piers.

The objectives of this investigation are to: (1) investigate the behavior of precast, prestressed bridge girders made continuous by connections using cast-in-place slabs and diaphragms at the piers; and (2) develop design procedures and guide specifications that can be used to compute elastic, inelastic, time-dependent, sag of noncomposite and composite members; (3) mathematical formulations to predict creep and shrinkage; and (4) analytical techniques to account for the time-dependent effects of creep, shrinkage, relaxation of strands, and construction sequence on the behavior of continuous prestressed girders.

SCOPE OF STUDY

The foregoing objectives were accomplished within the following scope:

1. Current practice in analysis, design, and construction of bridges built of prestressed girders made continuous was investigated.
2. Analyses were conducted to study the effects of variation in time-dependent material behavior and variation in bridge design parameters on the resultant service moments at continuity connections and girder midspan regions.
3. Analyses were conducted to study the effects of variation in bridge design parameters on inelastic redistribution of moments and development of the maximum strength of the bridge girders.
4. Computer programs were developed for simplified analysis methods.
5. Recommendations were developed for design procedures.

RESEARCH APPROACH

The project was divided into four tasks. This section briefly describes each of these tasks. The results and interpretation of the results are covered in Chapters Two and Three, respectively. The conclusions derived from the study are included in Chapter Four. The material provided in the appendices consists of further detailed discussion on questionnaire responses (App. A), creep and shrinkage test results (App. B), methods of analysis (App. C), parametric study (App. D), program documentation (App. E), design examples (App. F), and finally the proposed AASHTO Provisions and Commentary (App. G).

Task 1—Review of Existing Data

Task 1 consisted of reviewing current design and construction practices, performance data, and research findings related to simple-span precast, prestressed bridge girders made continuous. This information was assembled from both the technical literature and the unpublished experiences of designers and owners of structures of this type.

A review of published literature was conducted focusing on the following items: (1) creep and shrinkage data for steam-cured concrete loaded at an early age; (2) data on camber or sag of noncomposite and composite members; (3) mathematical formulations to predict creep and shrinkage; and (4) analytical techniques to account for the time-dependent effects of creep, shrinkage, relaxation of strands, and construction sequence on the behavior of continuous prestressed girders.

A questionnaire was prepared to obtain information from members of the AASHTO Subcommittee on Bridges and Structures, bridge designers, and girder fabricators. Respondents were requested to provide information on typical bridge configurations, material properties, positive and negative moment reinforcement details for connections at piers, design procedures for connection details, and bridge construction timing and sequence. Respondents were also requested to provide available unpublished data and descriptions of experience with specific bridges. Information gathered from questionnaire responses was used to select parameters for analytical studies of restraint moments and negative moment strength.

Because of the scarcity of published data on creep and shrinkage of steam-cured concrete loaded one or two days after casting, creep and shrinkage tests were conducted at the Construction Technology Laboratories (CTL). Four precasters provided cylinders from concrete used in actual bridge girder production. Precasters were selected to represent various regions of the United States. Creep and shrinkage measurements were conducted for at least one year. Measured data were compared to the American Concrete Institute (ACI) Committee 209 recommendations and other data. Results of the tests were used to select the range of creep and shrinkage properties used in the analytical study of service moments.

Task 2—Analytical Study of Service Moments

In Task 2, improved procedures were used to determine the degree of continuity and the moments resulting from dead loads, live loads, and time-dependent effects. Advanced analytical techniques were applied. Realistic geometry and material properties were used for analyses.
Time-dependent deformations and restraint moments induced in multispans bridges built of precast, prestressed girders made continuous were studied using computer analyses. The computer program used is capable of analyzing composite prestressed concrete structures of any cross-sectional shape having one axis of symmetry. The program accounts for the effects of nonlinearity of stress-strain responses of materials and variations with time of strength, stiffness, creep, and shrinkage of concrete, and relaxation of steel. The program also allows flexibility in analyzing various construction sequences and live load applications.

Initial analyses were conducted for verification of the computer program by comparison of analytical results with experimental data. Extensive computer analyses were then carried out for a parametric study of the effects of various amounts of continuity reinforcement, different construction sequences, girder age at deck casting, and variation in time-dependent material properties for concrete and prestressing steel in bridges with a range of girder types, spans, and spacings. The primary factor used to evaluate and compare results was the response to live load applied at various stages of service life. Time-dependent support restraint moments and live load service moments at supports and midspan were evaluated.

**Task 3—Flexural Strength Analysis**

Improved analytical procedures were used to predict ultimate strength and inelastic deformation capacity of negative moment regions for this type of bridge. Available flexural strength and ductility were determined using computer analyses. The computer program used is capable of determining flexural and shear strengths, inelastic deformation, and failure modes for the hinging region of reinforced or prestressed concrete sections subjected to combined axial load, moment, and shear.

Initial analyses were conducted for comparison of calculated and measured behavior of negative moment hinging regions of bridge girder sections. A parametric study was then carried out to evaluate effects of girder bottom flange configuration, amount of negative moment deck reinforcement, and material properties on negative moment strength and rotational ductility. Rotation capacities of analyzed sections were compared to required rotations for development of full failure mechanisms under ultimate load after redistribution of moments.

**Task 4—Pier Connection Design**

In Task 4, improved procedures to determine the strength and serviceability requirements for the positive and negative moment connections at the piers were developed. Advantages and disadvantages of providing positive moment reinforcement at continuity connections were weighed. Implications of the use of positive moment reinforcement were evaluated. Two computer programs were developed to assist in determination of service moments at supports of continuous bridges constructed of precast, prestressed girders and cast-in-place deck. Program BRIDGERM is an improved version of the PCA procedure for calculating time-dependent restraint moments. Results of analyses using this program were compared to results of analyses conducted in Task 2 and with results of analyses using the PCA procedure. Program BRIDGESSL was developed to calculate live load moments in a continuous bridge under AASHTO HS loading.

Results of analyses conducted in Tasks 2 and 3 were used to establish recommendations concerning: (1) the need for positive moment reinforcement within the connection at the piers; (2) conditions for determination of design moments; and (3) minimum and maximum limitations on the amount of deck reinforcement used in this type of bridge to ensure sufficient strength and ductility.

**NOTATION**

\[ A_d = \text{cross-sectional area of deck slab} \]
\[ A_f = \text{cross-sectional area of bottom flange, up to junction with web} \]
\[ A_g = \text{cross-sectional area of girder} \]
\[ A_p = \text{cross-sectional area of positive moment reinforcement provided at supports} \]
\[ A_s = \text{cross-sectional area of reinforcement in the deck slab} \]
\[ a = \text{empirical constant used in the age-strength relationship for concrete} \]
\[ b = \text{width of bottom flange} \]
\[ c = \text{depth from extreme compression fiber to neutral axis} \]
\[ d = \text{depth from extreme compression fiber to centroid of deck reinforcement} \]
\[ E = \text{modulus of elasticity} \]
\[ E_{cd} = \text{initial modulus of elasticity of concrete} \]
\[ E_d = \text{modulus of elasticity of deck concrete at time } T_i \]
\[ E_g = \text{modulus of elasticity of girder concrete} \]
\[ e = \text{eccentricity between centroid of prestress and centroid of girder section} \]
\[ e_c = \text{distance between the top of the girder section and the centroid of the composite section} \]
\[ F = \text{discrete element axial force} \]
\[ F_{pe} = \text{prestress force after losses} \]
\[ F_{pe} = \text{initial prestress force} \]
\[ F_2 = \text{axial force in girder element} \]
\[ f = \text{tension in deck to establish compatibility with the girder} \]
\[ f_a = \text{parameter defining the hyperbolic time function for shrinkage} \]
\[ F_{f_b} = \text{stress at the bottom of the section} \]
\[ f_c = \text{concrete compressive stress} \]
\[ f_c^* = \text{concrete cylinder compressive strength} \]
\[ f_c^{*28} = \text{maximum compressive stress in concrete stress-strain curve} \]
\[ f_{py}^{(1)} = \text{concrete cylinder compressive strength at time } t \]
\[ f_{py}^{(28)} = \text{concrete cylinder compressive strength at age of 28 days} \]
\[ f_{pu} = \text{ultimate tensile strength of prestressing steel} \]
\[ f_{py} = \text{stress at one percent elongation of prestressing steel} \]
\[ f_{ru} = \text{modulus of rupture} \]
\[ f_{ty} = \text{stress in prestressing strand at time } t \]
\[ f_{ty}^{(2)} = \text{stress in prestressing strand at time } t_i \]
\[ f_s = \text{stress in prestressing strand at time } t_i \]
\[ f_y = \text{steel yield stress} \]
\[ h_f = \text{depth of bottom flange, up to junction with web} \]
\[ I_c = \text{moment of inertia of composite section} \]
\[ I_g = \text{moment of inertia of cross section} \]
\[ K = \text{stiffness matrix} \]
FINDINGS

This chapter presents the results of the research including review of existing data, analyses for service moments, analyses for flexural strength, and development of analysis procedures for design. Interpretation of the results and recommendations for design procedures are presented in Chapter Three.

CHAPTER TWO

SUMMARY OF LITERATURE REVIEW

Advantages of Continuous Bridges

The design and construction of bridges composed of simple-span prestressed girders and cast-in-place decks have become widespread. Continuous bridges of this type have several practical, economical benefits. A primary reason for using continuity with precast, prestressed girders is the elimination of the maintenance costs associated with bridge deck joints and deck drain-
age onto the substructure. To avoid problems that occur at expansion joints, the State of Tennessee designed and constructed a 2,700-ft long prestressed concrete bridge with provision for expansion at the abutments only (1). Joints at abutments have been eliminated in several states that use girders built integrally with the abutment (2).

A method of bridge construction in Great Britain, utilizing precast, pretensioned concrete beams with cast-in-place concrete deckinng, is presented in Ref. 3. This paper discusses a number of different methods of eliminating joints in the decks of composite bridges. It is shown that an additional advantage of continuity for live loads in the bridge superstructure could be achieved. The same is presented in Ref. 4, where it is reiterated that, in continuous spans, the positive moment due to live loads is decreased at girder midspan. As a result, for a given span, fewer prestressing strands are needed in continuous spans compared to simply supported spans. The advantages of continuity were also studied in New Zealand (5). It was concluded that use of continuity will lead to greatly enhanced structural performance, particularly in earthquake zones, and will produce savings in the cost of construction. Additional reasons for using continuity with pretensioned girders are to improve the appearance and riding qualities of this type of bridge.

Portland Cement Association Research

An extensive experimental and analytical investigation on long-time behavior of continuous precast, prestressed concrete bridges was reported in a series of Portland Cement Association Research and Development Bulletins (6, 7, 8, 9, 10, 11). Behavior of structures consisting of two half-scale I-shaped girders connected by a continuous cast-in-place deck slab and a cast-in-place diaphragm at the interior support was investigated. The results of the experimental investigation clearly showed the feasibility of establishing continuity between precast girders from span to span. Long-term measurements were made at suitable time intervals after casting the deck slab. Continuity moment at the interior support was studied for the two continuous bridge structures. The structures were identical, except that one incorporated a positive moment connection at the interior support while the other did not. Restraint moments due to creep and shrinkage of concrete were studied for these two bridges.

It was shown that higher restraint moments were present for the bridge with positive moment connection. On the other hand, when no positive moment connection was provided between the ends of the girders, cracking occurred at the bottom of the diaphragm enclosing the ends of the girders, and continuity between the girders for live loads was reduced. As a result of the theoretical and test studies, a design procedure developed by PCA (12) was published in 1969. This publication offers guidelines for the design of the positive moment connection between adjacent girders and the negative moment reinforcement over the piers. For design purposes, it was assumed that the distribution of moments and forces will change toward that which would have occurred if the loads applied to the individual elements before continuity was established had instead been applied to the structure after continuity was present.

As a result of the PCA investigations (6–11), the structural continuity obtained in bridges built with precast, prestressed girders and cast-in-place concrete deck was recognized by introducing design guidelines in the 1971 Interim AASHTO Specifications (13). These guidelines have not been revised and appear in Article 9.7.2 of the 1983 AASHTO Specifications (14), entitled "Bridges Composed of Simple Span Precast, Prestressed Girders Made Continuous." That section states that "the effects of creep and shrinkage shall be considered in the design" of this type of bridge. No specific guidance is given as to how these effects should be considered in design. Some general guidelines for design of the positive moment connection as well as the negative moment reinforcement at piers are provided.

Although existing bridges designed by this procedure are generally performing well, it is believed that this method may not accurately predict the true behavior of these structures. This uncertainty is due to different loading and construction stages, time-dependent effects, and details used to make the connections.

Two papers (15, 16) relating portions of the research carried out in this study have been written prior to this report. In the initial paper (15), the PCA analysis method (12) was evaluated by comparison with more sophisticated computer analyses. ACI Committee 209 (17) procedures for the estimation of the time variation of compressive strength, creep, and shrinkage of concrete were used in the computer analyses. It was concluded that girder restraint moments at pier supports are similar for early age at continuity, say 17 days after girder prestress. However, as the age at continuity increases, so does the difference between the computer analysis and the simplified method. In a second paper (16), the need to consider construction timing in determining design moments, and the effects of providing positive moment reinforcement at the diaphragms are discussed.

Time Dependent Material Properties

Composite members, consisting of precast prestressed bridge girders and cast-in-place deck slabs, are sensitive to creep and shrinkage of concrete and relaxation of prestressing steel. Differential shrinkage between girder concrete and deck concrete and creep of girder concrete due to combined effects of prestress force and dead load produce secondary forces and deformations in the composite member. A complex interaction exists between concrete aging, creep, and shrinkage and relaxation of prestressing steel. In the literature, several state-of-the-art papers exist. Major contributions have been made by Sattler (18), Branson and Ozell (19, 20), Branson (21), Roll (22), Birkeland (23), Trost and co-workers (24, 25), and Dilger and Neville (26). The last three references make use of the aging coefficient developed by Trost (27) and later by Bazant (28). This approach has been used by many authors (29, 30, 31) because of its relative simplicity.

Several practical models for predicting mean cross-section creep and shrinkage exist at present. These models (Model of ACI Committee 209 (17), Model of CEB-FIP (32), and Model of Bazant and Panula (33)) differ in their degree of accuracy and simplicity.

The ACI model is the simplest one, while the Bazant and Panula model is the most comprehensive. Experimental creep and shrinkage studies have been performed by many authors. Properties of steam-cured concrete loaded at an early age have been reported by ACI Committee 209 (17), Hanson (34), Kliger (35), Gamble (36), and Pfeifer (37).

Various publications (17, 38–41) present prestress loss measurements and methods to predict prestress losses due to steel
Methods of Analysis

The problem of predicting complete time-dependent response of a continuous prestressed concrete bridge is very complex. It depends on time-dependent properties of materials, geometry of the structure, amount of prestressing, methods and sequences of prestressing and construction, loading arrangement, and age at loading. There are a number of mathematical formulations to predict time-dependent effects for prestressed structures. They have been reported by Bazant and Wittmann (42), Aswad (43), Scordelis (44), and Anderson (45). Various computer programs (46, 47, 48, 49, 50, 51, 52, 53) use step-by-step procedures to calculate prestress loss and deformations due to loading, creep, shrinkage, and steel relaxation. Since the first application of the finite element method to the analysis of reinforced concrete structures, made by Ngo and Scordelis (54) in 1967, numerous studies have taken place covering all aspects of structural behavior of concrete structures. A comprehensive review has been made by Bazant, Schnobrich, and Scordelis (55).

Computer Program PBEAM (53), developed by C. Suttikan, is capable of analyzing composite prestressed concrete structures of any cross-sectional shape having one axis of symmetry. The program accounts for the effects of nonlinearity of stress-strain responses of materials and variations with time of strength, stiffness, creep, and shrinkage of concrete, and relaxation of steel. A step-by-step method is used in the time-dependent analysis with a tangent stiffness method implemented for solving nonlinear response. Precast, prestressed bridge girders with composite cast-in-place decks are modeled using a discrete element method as developed by Hays and Matlock (56).

In order to study the parameters affecting bridge girder capabilities to attain maximum strength, methods of analyses to determine ductility capacity of girder sections and the ductility demand for hinging regions of bridge girders are required. Program WALL–HINGE (57) was developed to analyze reinforced concrete shear walls and predict failure modes including web crushing and compression zone crushing. The program is used to determine the strength, inelastic deformation capacity, and failure modes for the hinging region of structures subjected to combined axial load, moment, and shear. The analysis considers both longitudinal and transverse equilibrium through the hinging region and across the transverse plane near the support. The analysis accounts for important behavioral effects within a hinging region including a nonlinear strain distribution, dowel action, aggregate interlock, and the interaction of compressive stress and shear stress in the compression zone with a strength criteria based on a critical octahedral shear stress.

A general method for calculating required hinge rotations is described by Park and Paulay (58). Using this method, the required plastic rotation at the supports is equal to the discontinuity of slope between the ends of adjacent members determined from an elastic analysis of each member supporting the maximum load condition including the external load and moments at support hinges.

Other Research

Time-dependent behavior of noncomposite and composite prestressed concrete structures under field and laboratory conditions was also studied by Mossiossian and Gamble (59, 60). Instrumentation was installed in three structures and deformation data were gathered and interpreted. Also, two 1/4th-scale models were constructed to simulate portions of the field instrumented structures. The models were tested to provide data to help confirm some information developed in the field study.

Extensive parametric studies were carried out (46, 47) as part of the project to develop a relatively complete understanding of the factors influencing the growth in camber in bridges, the loss of prestress with time, the development of moments at interior supports, and the various interactions between the time-dependent strains in the deck and girder concrete which exist in composite structures. Experimental studies of camber and deflection of prestressed concrete beams were also presented in Ref. 47, where various mathematical models for creep, camber and deflection are discussed. Studies on camber or sag of noncomposite (61, 62, 63) and composite (64, 65, 66) members are also published.

RESULTS OF QUESTIONNAIRE

Questionnaires were sent to transportation officials, designers, fabricators, and others to obtain knowledge on the current state of practice in design and construction of bridges constructed of precast, prestressed girders made continuous. Information gathered from 49 questionnaire responses was used to establish typical ranges for the various parameters used in analytical portions of this project. In this section, the major categories of responses will be discussed. The questionnaire and a detailed summary of responses are included in Appendix A.

Bridge Configuration

Several questions dealt with configuration of bridges constructed of prestressed girders made continuous. In the experience of the respondents, the maximum number of continuous spans ranged from 2 to 29, with the majority falling between 3 and 7. The most commonly used standard girders were AASHTO-PCI sections (4) particularly Types II, III, and IV. Span lengths and girder spacings for the AASHTO-PCI sections were consistent among the respondents using a particular section. A large variety of non-AASHTO sections were indicated, none of which were used in a particularly wide area. Non-AASHTO girders were primarily I or Bulb-Tee sections, although several box girders were also specified. Twenty respondents used a standard profile for draped strands. Forty-two respondents indicated that positive moment connection is used in their continuous bridges.

Material Properties

Specified properties of concrete, prestressing strand, and conventional reinforcement used in simple span bridges made continuous were requested of questionnaire recipients. The most common girder concrete strengths at prestress transfer were between 4,000 and 5,500 psi. The most common concrete strengths at 28 days were between 5,000 and 6,500 psi. All respondents indicated that they used grade 270 prestressing strand. The type of strand used was nearly evenly divided between stress-relieved and low-relaxation. The most common strand diameter was 1/4 in. with 0.6 in. and 7/16 in. the only...
exceptions. Nearly all of the specified deck and diaphragm concrete strengths ranged between 3,000 and 4,500 psi, with most between 4,000 and 4,500 psi. Deck reinforcement used by respondents was primarily Grade 60.

**Design Procedures**

Questionnaire recipients were requested to provide information on procedures used in design for service loads and long-term effects. Most respondents indicated that provision was made for an additional wearing surface during a bridge's service life. Average magnitude of the additional load was 25 psf, and the average age at which the load is applied was about 15 years. Thirty-eight respondents indicated that they use AASHTO HS20-44 (1/4) live load alone or in combination with other loads. Several respondents used HS25 or larger design loads.

In order to calculate midspan and support design moments, the degree of continuity for negative and positive moments at supports must be established. A variety of procedures was specified by questionnaire recipients. Current practice includes:

1. Designing and providing positive moment reinforcement or using standard details at the pier connection and considering negative moment continuity for reduction of live load positive moment near midspan.
2. Designing and providing moment reinforcement or using standard details, but ignoring negative moment continuity for reduction of live load positive moment near midspan.
3. Providing no positive moment reinforcement, but considering negative moment continuity for reduction of live load positive moment near midspan.
4. Providing no positive moment reinforcement and ignoring negative moment continuity for reduction of live load positive moment near midspan.

The most common design method employed by respondents for proportioning positive moment reinforcement at piers was that published by PCA in Ref. 12. Thirty of the 42 respondents who provide positive moment reinforcement indicated that their design process is based on the PCA method, occasionally with supplementary information or procedures. Several respondents indicated that they do not calculate long-term positive moments at piers and provide standard reinforcement based on previous experience with specific girder types, spacings, and span lengths.

**Reinforcement Details**

Recipients of the questionnaire were requested to provide information on typical details used for positive moment reinforcement at piers as well as negative moment and deck reinforcement. The most common positive moment details used by respondents were the embedded bent bar and the extended strand detail shown in the questionnaire. Eighteen respondents provided this information. The majority of the respondents indicated that girders were between 10 to 90 days old at the time of construction. The sequence of placing concrete in the deck and diaphragms at supports has an influence on the long-time behavior of the bridge. Nine respondents indicated that bridge decks are typically cast before diaphragms at piers. A common variation consists of casting positive moment areas of the deck first and then casting piers, then applying the diaphragms and negative moment areas of the deck. Sixteen of the respondents typically cast deck and pier diaphragm concrete simultaneously. Ten respondents typically cast pier diaphragms after casting deck concrete.

**Construction Sequence**

The questionnaire requested information regarding problems encountered during the service life of simple span bridges made continuous. Specifically, information was requested about construction, service, and maintenance problems. Twenty-eight respondents returned information on problems encountered in their experience. Most common among the responses were problems encountered during bridge construction. Specific problems in each of the three areas were mentioned by several respondents. Some of these common problems are listed below:

- Positive moment reinforcement which required field adjustment because of poor fit.
- Misplacement of reinforcement, such as extended strands inadvertently cut off.
- Transverse cracking of the deck in negative moment areas and throughout the bridge.
- Excessive girder camber, requiring adjustment of profile grade, etc.
- Incorrect construction sequencing.
- Cracking of pier diaphragms due to long-term creep and shrinkage.
- Cracking and spalling of pier diaphragms when diaphragms are cast before the deck.
- Spalling of piers and abutments due to poor girder location or inadequate seat detailing.
- Movement of girders during construction when deck concrete is poured before diaphragms.

Each of these problems was mentioned by at least two respondents. In addition, several problems were mentioned individually, such as brittle fracture of bent reinforcing bars during girder placement, corrosion of deck reinforcement after cracking has taken place, opening of expansion joints due to long-term girder movements, and difficulty in replacing girders when necessary.
Miscellaneous

Questionnaire recipients were requested to provide information on previously conducted measurements of camber or sag of prestressed girders, deflections of composite deck-girders, and creep and shrinkage of concrete used in bridge girders. Nine respondents indicated that they had conducted measurements in these areas or were initiating projects. Six of the nine respondents were transportation officials. Two girder fabricators and one designer also had conducted tests. Eight of these respondents had conducted or were initiating measurements of camber or sag of prestressed concrete girders. Two respondents indicated a reference for published data.

The last section of the questionnaire requested information on specific bridges designed or constructed by the respondent. Eleven respondents provided this information.

A detailed summary of questionnaire responses is given in Appendix A.

CREEP AND SHRINKAGE TESTS

Creep tests were conducted on concretes obtained from precasting plants from different regions of the United States to broaden the knowledge of creep and shrinkage properties of steam-cured concrete loaded at an early age. Prestressed girders are usually steam cured. Transfer of prestress can occur as early as 18 hours after casting. Review of the literature indicates that data on creep of steam-cured concrete loaded at one day are scarce. Within the limited data on steam-cured concrete loaded within the first week, there is a lot of scatter in the test results. Creep and shrinkage tests were conducted at CTL to increase the data base and to compare results with mathematical models. In this section, the creep and shrinkage test data are presented and comparisons are made to coefficients determined using ACI 209 (17) recommendations. Further details of the creep and shrinkage data are included in Appendix B.

One local (Chicago area) and three nonlocal precasting plants were selected for participation. Standard 6-in. by 12-in. cylinders were cast from concrete used in actual bridge girder production. The cylinders were steam cured at the plants. Cylinders from the three nonlocal plants were shipped air freight to CTL as soon as possible after the steam curing was completed. Creep tests conforming to ASTM Standard C 512 (67), “Creep of Concrete in Compression,” were begun immediately upon arrival.

Initially, two sets of cylinders were obtained from a local precasting plant. For one set, creep tests were initiated following steam curing within a minimum time required to transport the cylinders to the laboratory. This condition simulates cylinders loaded at about the same age as the concrete in girders at transfer of prestress. Creep tests were initiated on the second set from the local plant at a concrete age equivalent to the average age of the cylinders received air freight from the nonlocal plants. Because of unreliable test results, a third and fourth set of cylinders were obtained from the local plant. Creep tests on these cylinders were repeated to duplicate the timing of creep tests on the first two sets of local specimens. Results of tests on the first two sets of cylinders from the local plant are not reported here. A total of five creep and shrinkage tests are included in this report.

Table 1 shows the concrete mix designs for cylinders from the four precasters. Precaster A is located in the Eastern U.S., Precasters B and C are located in the Western U.S. Precaster D is located in the Chicago area. Table 2 gives the pretest conditions and concrete properties just prior to the start of creep tests.

Appendix B contains measured values of creep test parameters for the five creep tests. The initial elastic strain was computed by dividing the unit pressure acting on the loaded cylinders by the pretest modulus of elasticity determined from tests on companion cylinders. Drying shrinkage strains are measured on unloaded cylinders stored in the same controlled environment (75°F and 50 percent relative humidity) as the loaded cylinders are stored in. Creep strain is determined by measuring total strain of loaded cylinders and subtracting shrinkage strains. Creep strain/psi is determined by dividing creep strains by the pretest modulus of elasticity determined from tests on companion cylinders.

<table>
<thead>
<tr>
<th>Table 1. Concrete mix designs for creep test specimens.</th>
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<tbody>
<tr>
<td>Component</td>
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<tr>
<td>---</td>
</tr>
<tr>
<td>Cement, pcy</td>
</tr>
<tr>
<td>Sand, pcy</td>
</tr>
<tr>
<td>Stone, pcy</td>
</tr>
<tr>
<td>Water, pcy</td>
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<tr>
<td>W/C Ratio</td>
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<td></td>
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<td>Admixtures</td>
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<tr>
<td>Agent, Water</td>
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<tr>
<td>Reducer</td>
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</tbody>
</table>

Table 2. Pretest concrete conditions for creep test specimens.

<table>
<thead>
<tr>
<th>Curing conditions</th>
<th>Precaster A</th>
<th>B</th>
<th>C</th>
<th>D*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Steam</td>
<td>12 hr</td>
<td>Steam</td>
<td>14-1/2 hr</td>
<td>Steam</td>
</tr>
<tr>
<td><em>overnight</em></td>
<td>54-1/2 hr</td>
<td>51-1/4 hr</td>
<td>48 hr</td>
<td>14-1/2 hr</td>
</tr>
<tr>
<td>26 hr (16)</td>
<td>50 hr (26)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Time from casting to loading for creep test</td>
<td>6570</td>
<td>7510</td>
<td>6800</td>
<td>4770 (16)</td>
</tr>
<tr>
<td>Pretest comp. strength, psi</td>
<td>4800</td>
<td>4640 (16)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Pretest Mod. of Elasticity, ksi</td>
<td>4650 (20)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*Designations (16) and (20) refer to cylinders loaded for the creep test at 1 day and 2 days after casting, respectively.
stress acting on the loaded cylinders. The creep coefficient is determined by dividing creep strain by the initial elastic strain.

The forms of equations used to fit the drying shrinkage and creep coefficient data are those given by ACI-209, “Prediction of Creep, Shrinkage, and Temperature Effects in Concrete Structures” (17). For creep coefficient, the standard equation is:

\[ \nu_t = \nu_u \frac{t^a}{d + t^f} \]  

where: \( \nu_t \) = creep coefficient at time \( t \) days, \( \nu_u \) = ultimate creep coefficient, and \( \Psi, d, f = \) parameters defining the hyperbolic time function.

Normal ranges for \( \nu_u, \Psi, \) and \( d, f = \) are: \( \nu_u = 1.30 \) to 4.15, \( \Psi = 0.40 \) to 0.80, and \( d = 6 \) to 30.

For shrinkage strain, the standard equation is:

\[ (\epsilon_s)_t = (\epsilon_s)_u \frac{t^a}{f + t^f} \]  

where: \( (\epsilon_s)_t \) = shrinkage strain at time \( t \) days (millionths), \( (\epsilon_s)_u \) = ultimate shrinkage strain (millionths), and \( \alpha, f, \Psi = \) parameters defining the hyperbolic time function.

Normal ranges for \( (\epsilon_s)_u, \alpha, \) and \( f, \Psi = \) are: \( (\epsilon_s)_u = 415 \) to 1,070, \( \alpha = 0.90 \) to 1.10, and \( f = 20 \) to 130.

Curves were fit to the measured data by applying linear regression analyses to converted data. For creep coefficient, curve fit parameters were determined for \( t^a/\nu \) versus \( t^a \) data. Similarly, for shrinkage strains, \( t^a/(\epsilon_s)_t \) versus \( t^a \) was analyzed. In each case, a range of exponents was specified for \( \Psi \) or \( \alpha \). A least squares regression was performed for each specified exponent. For each resulting curve fit, the sum of squared errors between the fit curve and the actual data was calculated. The exponent which yielded the minimum sum of squared errors was used to determine the best fit curve.

The curve fit parameters for results of the five creep tests are given in Tables 3 and 4. The creep test for Precaster C was terminated after one year. Figures 2 and 3 show plots of creep coefficient and shrinkage strain data for Precasters A, B, C, and D. Also shown on Figures 2 and 3 are ACI-209-recommended equations with upper and lower limits for ultimate values. In all cases, curves for creep coefficient and shrinkage strain are within the range recommended by ACI-209 for later ages. Particularly for shrinkage strain, the time functions are somewhat different from ACI-209 recommendations. The differences occur primarily in the early age behavior of the time functions. This can be seen in Figures 4 and 5, in which test results for the first 100 days are shown. Creep coefficient results for all specimens fall within ACI-209-recommended bounds. For very early age, less than about 15 days, shrinkage strain results for all five specimens were slightly greater than the ACI-209 recommended upper bound.

Also given in Tables 3 and 4 are ACI-209 recommended values for ultimate creep coefficient and shrinkage strains. These values were determined using ACI-209 concrete composition modification factors, which account for variations in slump, percent of fine aggregate, cement content, and air content. These modification factors were applied to the recommended ultimate creep coefficient of 2.35 and the recommended ultimate shrinkage strain of 780 millionths. Generally, the ACI-209 recommended values underestimate test results. In Appendix B, ACI-209 recommended time curves are further compared to test results.

During the work on this study, the measured creep data were also compared to predictions using the simplified Bazant-Panula (BP2) relationship (33). Although the Bazant-Panula approach is significantly more complex than the ACI-209 approach, in general, the results of the BP2 relationships are expected to be more accurate. However, as stated in Ref. 33, the BP2 approach is not intended to be used for concrete loaded earlier than 7 days. The comparisons made in this study indicated that the application of the BP2 relationships to steam-cured concrete loaded at 1 or 2 days resulted in significantly larger errors than with the use of the more simplified ACI-209 relationships. Although there is some inaccuracy in the ACI-209 relationships, as shown in Tables 3 and 4, the error for the steam-cured concrete loaded at 1 or 2 days in this study is not any larger than the expected error for concrete loaded at a later age. The ACI-209 recommended time functions were used for analyses conducted in this study.

**VERIFICATION OF ANALYTICAL PROCEDURES**

Existing computer programs PBEAM (53) and WALL-HINGE (57), discussed in the summary of literature review, were selected for use in this study because of the direct
Applicability of each of these programs to the analytical tasks. Information concerning verification of each of the programs by comparison with experimental data was contained in the literature on the programs. However, further verification analyses were carried out in this study. This section presents a description of the programs along with comparisons between analysis and test results. More detailed descriptions of the programs are included in Appendix C.

Analyses for Service Moments

Program Description. Time-dependent deformations and restraint moments induced in multispans bridges built of prestressed girders made continuous were studied using a modified version of computer program PBEAM (53). A detailed description of the program is given in Appendix C. This program, developed by Suttikan, is capable of analyzing composite pre-
stressed concrete structures of any cross-sectional shape having one axis of symmetry. The program accounts for the effects of nonlinearity of stress-strain responses of materials and variations with time of strength, stiffness, creep, and shrinkage of concrete, and relaxation of steel. A step-by-step method is used in the time-dependent analysis with a tangent stiffness method implemented for solving nonlinear response.

Precast, prestressed bridge girders with composite cast-in-place decks are modeled using a discrete element method as developed by Hays and Matlock (36). Element deformations and forces are estimated by analyzing stress-strain relationships of a series of rectangular fibers distributed over the depth of the cross section. It is assumed that strain in each fiber is constant at the centroidal axis of the fiber and strain distribution varies linearly through the depth of the section. For each time step, equilibrium at each element is maintained by determining the time dependent stress corresponding to the level of strain in each fiber. Stress multiplied by area is summed over all fibers and force equilibrium is checked. If necessary, the strain distribution is adjusted and the process is repeated until forces balance.

The ACI Committee 209 (17) procedures to estimate the time variation of compressive strength, creep, and shrinkage of concrete and relaxation of prestressing steel are used in the PBEAM computer program. The rate of creep method and method of superposition are available in the program to account for the effect of concrete creep on the distribution of stresses in a section. The method of superposition was used for the studies conducted in this project.

The PBEAM computer program allows unlimited flexibility in analyzing various construction sequences and live load applications. The analysis accounts for construction sequence such that the simple span behavior of the girder before casting of deck and diaphragm, and continuous behavior thereafter, are correctly modeled. Casting of deck and diaphragm can be done at any girder age and in any sequence. Live load can also be applied at any stage of service life and in any configuration. The program can therefore be used to investigate behavior under a wide variety of conditions likely to be encountered in actual use of this type of bridge.

The program's capabilities also allow a realistic analysis of the influence of diaphragm cracking on the behavior of this type of bridge. Depending on stress level and time-dependent material properties, the program accounts for cracking of the girder and/or the deck concrete under positive or negative moments. For each time step of the analysis, the program stores the stress-strain relationship in every fiber of each element. These stored conditions serve as the starting point for the behavior calculated for the succeeding time step. In this way, the program can follow both crack development and crack closing. This analytically models the situation shown experimentally in Ref. 10, in which cracks, which had opened at the bottom of the diaphragm under the influence of positive restraint moments, were closed by the negative moment induced upon application of live load. With initial application of live load, the diaphragm crack is open and girders behave essentially as simply-supported beams. With increasing live load and rotation at the diaphragm, the bottom crack closes and negative moment continuity becomes effective. The amount of rotation needed to close the crack is dependent on the creep and shrinkage properties of both the girder and deck concrete, the ages of the two concretes at the time of live load, the amount of restraint provided by the positive moment reinforcement in the diaphragm, and the girder type, span length and spacing. Therefore, the degree of negative moment continuity is dependent on all these parameters. With proper incremental application of live load, PBEAM correctly models the change in negative moment stiffness that accompanies closing of the diaphragm cracks, thereby providing an analytical tool to evaluate the effects of all these parameters.

A "tension stiffened" effective stress-strain relationship for top and bottom reinforcement at supports was also used in PBEAM in order to model behavior of reinforcing steel at cracked sections (37). These features allow application of PBEAM to predict the changes in continuity at supports due to cracking of diaphragm and deck concrete as well as closing of cracks upon reversal of moments from application of live load.

Comparison Between Analysis and Test Results. To confirm the PBEAM analytical methods of predicting the time-dependent response of precast, prestressed bridges, results of computer analyses were compared to the PCA test observations conducted by Mattock (10). The test bridges included precast, prestressed girders with continuous cast-in-place deck slab and diaphragm. Long-term behavior of two half-scale model structures, identified as Girder ½ and Girder ¾, were recorded by PCA. The two bridge girders were virtually identical except that Girder ¾ incorporated both positive and negative moment connections at the interior support while Girder ½ had only a negative moment connection.

The precast girders were 1-shaped in cross section and 33-ft long. The prestressing force was released when the age of the girders was about 8 days. The girders were positioned on load cells on the top of columns, with their adjacent end faces 3 in. apart. About 13 days after positioning the girders, 800-lb concrete blocks were hung at points 3 ft apart along the entire length of each girder to compensate for the dead weight of the half-scale model. The continuity reinforcement was placed and the deck slab and diaphragm were then cast when the age of girders was about 28 days.

The girders were monitored for long-term behavior. Also, at intervals throughout the test period, the girders were subject to live load tests by concentrated loads applied at the middle of each span. This was done in order to check continuity moment developed at the center support by service load.

The comparison of test results and computer analysis for long-term variation of the center support reaction is shown in Figure 6. It can be seen that variation of the center support reaction with time as estimated by the program PBEAM and from the test are in a good agreement.

Continuity behavior of the girders with live load applied at various stages of the long term test was compared to the computer time-dependent analysis. Results for Girder ¼ at age 45 days are shown in Figure 7. Before cracks were observed in the deck, elastic theory midspan moment and time-dependent moment from PBEAM computer program differed by approximately 5 percent. After cracking of the deck slab, a significantly lower degree of continuity was observed for both the test girder and the PBEAM analysis.

Test observations and results of computer analysis at age 694 days for Girder ½ are compared in Figure 8. Time-dependent positive moment had induced a crack in the bottom of diaphragm concrete over the pier. Girder ½ did not have any positive moment reinforcement within the diaphragm. With application of live load, the positive moment crack must close
Figure 6. Variation with time of center support reaction.

Figure 7. Variation with applied load of center support moment, Girder $\frac{1}{2}$.

Figure 8. Variation with applied load of center support moment, Girder $\frac{1}{2}$. 
prior to including negative moment at the continuity connection. The test continuity moment during closing of the crack averaged only about 18 percent of the elastic continuity moment, comparing with 12 percent from computer analysis. Test results and time-dependent computer analysis showed that stiffness of the connection in Girder ½ became fully restored after closing of the crack at the bottom of the diaphragm. However, the negative continuity moment was significantly below the value determined from analysis as a fully continuous beam. Consequently, the positive moment at midspan was larger than that determined from a fully continuous analysis.

The observed correlation between test results and computer analyses indicated that PBEAM is capable of adequately modeling the time-dependent and nonlinear behavior of these simple span girders made continuous.

**Analyses for Flexural Strength**

*Program Description.* Program WALL—HINGE (57) was developed to analyze reinforced concrete shear walls and predict failure modes including web crushing and compression zone crushing. A detailed description of the program is given in Appendix C. The program is used to determine the strength, inelastic deformation capacity, and failure modes for the hinging region of structures subjected to combined axial load, moment, and shear. The analysis considers both longitudinal and transverse equilibrium through the hinging region and across the transverse plane near the support. The analysis accounts for a nonlinear strain distribution within the hinging region using a compatibility relationship between the summation of tensile strain over the hinge length resulting from the "fanned" cracking pattern with the summation of compressive strains within a relatively short length near the tip of the fan as shown in Figure 9. This is an important effect to consider in analyses for flexural-compression or shear-compression failure modes that is not accounted for in typical sectional analyses made assuming a linear strain distribution. The important effects of dowel action, aggregate interlock, and interaction of compressive stress and shear stress in the compression zone for analysis of transverse equilibrium across a plane near the support were included. The program uses a complete tri-axial concrete stress-strain relationship developed by Ahmad and Shah (70), with strength criteria based on a critical octahedral shear stress.

In order to analyze negative moment ductility of composite prestressed girders, the precompression effects of prestressing strand in the bottom flange of the girder were included. The effective prestress in strand was estimated at an assumed critical plane located a distance from the end of the girder equal to the neutral axis depth at ultimate moment. This accounts for experimentally observed behavior in which concrete crushing occurs beyond the end of the girder enclosed in the cast-in-place diaphragm.

**Comparison Between Analysis and Test Results.** In order to verify the applicability of program WALL—HINGE to analysis of negative moment ductility of composite prestressed girders, the program was used to analyze girders tested in Ref. 6. This test program investigated experimentally the feasibility of establishing continuity in a bridge constructed of precast, prestressed concrete girders by casting a concrete deck with negative moment reinforcement over supports and a diaphragm between ends of girders. In the experimental program, the girder was a ½-scale model of a 44-in. deep I-girder. Tests were conducted with varying amounts of prestressing steel and conventional deck reinforcement. Program WALL—HINGE was used to analyze three of the tested girders. The three analyzed girders had 0.9

![Figure 9. Negative moment hinging region.](image-url)
and calculated using programs BEAM BUSTER and WALL_HINGE. Table 6 contains measured strains from tests and calculated strains for deck steel. Predictions from program WALL_HINGE are in better agreement with test results than are results from BEAM BUSTER. This is particularly true for Girder 3, which failed by crushing of the bottom flange prior to yielding of the deck reinforcement.

Results from both programs indicate failure modes similar to observed behavior from tests. For Girder 1, failure of the PCA test structure occurred well after yield of deck steel. Program WALL_HINGE predicted failure after high strains are reached in both deck steel and bottom concrete. Crushing of concrete occurred after strain hardening of deck steel started. BEAM BUSTER results also show crushing of concrete after large strains developed in the deck steel.

For Girder 2, failure of the PCA test structure occurred in a nearly balanced mode. Experimental and analytical results indicate that crushing of concrete occurred nearly simultaneously with or just after yielding of steel. In PCA test results, measured strains indicated that deck steel yielded occurred simultaneously with crushing of concrete. Both programs showed failure occurring while steel stress was in the flat region of the stress-strain curve just beyond yield. It should be noted that program WALL_HINGE includes a "tension-stiffened" stress-strain relationship for reinforcement which includes effects of bond and slip between concrete and reinforcement and the effects of concrete cracking. The deck reinforcement strains reported in Table 6 for WALL_HINGE results are the peak calculated strains occurring right at crack locations. The relationships between strain gage locations and crack locations in the PCA test specimens are unknown.

For Girder 3, test results indicate that failure occurred due to crushing of concrete before yielding of steel. BEAM BUSTER results indicate that failure occurred when concrete crushed essentially simultaneously with yielding of the steel. WALL_HINGE results more accurately predicted failure due to concrete crushing before yield of steel.

### SERVICE MOMENTS

A primary task of this project was to determine the time-dependent effect on continuity of precast, prestressed girders made continuous. To accomplish this, a parametric study was carried out using PBEAM to examine the range of bridge behavior as related to ranges of material properties and bridge design parameters. The main emphasis of the parametric study was on the resultant design service moment for the girders. This section presents the results of the parametric study concerning continuity effects for positive and negative service moments. Further detailed results of computer analyses are included in Appendix D.

### TABLE 5. Negative moment capacities from tests and analyses.

<table>
<thead>
<tr>
<th>Girder</th>
<th>Deck Steel, %</th>
<th>PCA Test, in-kip</th>
<th>BEAM BUSTER Calculated, Mcalc in-kip</th>
<th>WALL_HINGE Calculated Mcalc in-kip</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.83</td>
<td>-2440</td>
<td>1.18</td>
<td>-2230</td>
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<tr>
<td>2</td>
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<td>3</td>
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<td>-4000</td>
<td>0.81</td>
<td>-4290</td>
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### TABLE 6. Deck reinforcement strains near moment capacity from tests and analyses.

<table>
<thead>
<tr>
<th>Girder</th>
<th>Deck Steel, %</th>
<th>PCA Test</th>
<th>BEAM BUSTER</th>
<th>WALL_HINGE</th>
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</thead>
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<td>0.0119</td>
<td>0.0195</td>
<td>0.0220</td>
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<td>0.0016</td>
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### Parametric Study

The program PBEAM was used to evaluate the effects of variations in several parameters on the behavior of bridges constructed of prestressed girders made continuous. Table 7 provides a summary of the parameters analyzed in the study. The basic model used for the parametric study consisted of a bridge of four equal length spans, as shown in Figure 10(a). Characteristics of the model which were varied included:

1. Girder type.
2. Span length.
3. Girder spacing.
4. Positive moment continuity reinforcement.
5. Time-dependent material properties (a) concrete (compressive strength, creep coefficient, shrinkage strain) and (b) prestressing steel (relaxation characteristics).
6. Girder age when deck and diaphragm are cast.
7. Girder age at application of live load.
8. Construction sequence.

Values for these parameters were chosen to reflect the range of current practice as indicated by responses to the questionnaire. Following are brief discussions of the variables used in the parametric study.

Four girder types, shown in Figure 10(b), were used in the parametric study, AASHTO Types IV and VI, Modified Bulb Tee BT72/6 (4), and a box section. Questionnaire responses indicated that AASHTO standard sections were most commonly used. The AASHTO-IV and AASHTO-VI sections were chosen to represent girders used for medium to long span bridges. The AASHTO-IV girder was used with span lengths of 70 ft and 100 ft in the parametric study. The AASHTO-VI girder was used with span lengths of 100 ft and 130 ft in the parametric study. These AASHTO standard girders have heavy cross sections for their span length capabilities. Questionnaire responses also indicated that a variety of lighter girder sections are in
Table 7. Bridges analyzed in parametric study.

<table>
<thead>
<tr>
<th>Bridge Number</th>
<th>Girder Type</th>
<th>Span, ft.</th>
<th>Spacing, ft.</th>
<th>Ultimate Creep Coefficient</th>
<th>Ultimate Shrinkage, millionths</th>
<th>Age at Continuity, days</th>
<th>Age at Live Load, days</th>
<th>Prestress Steel</th>
<th>t’c Girder/Deck, psi</th>
<th>Positive Reinforcement, sq in.</th>
<th>Miscellaneous</th>
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<td>17</td>
<td>650</td>
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<td>6500/4000</td>
<td>7.2, 3.6, 0.2</td>
<td>2.0 x LL</td>
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<td>SR</td>
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<td>7.2, 3.6, 0.2</td>
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<td>6500/4000</td>
<td>7.2, 0.2</td>
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<td>800</td>
<td>10 / 17</td>
<td>650</td>
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<td>67 / 74</td>
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<td>6500/4000</td>
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a) Bridge with Four Spans of Various Girder Types

b) Girder Sections for Parametric Study

Figure 10. Bridge model for parametric study.
current use, particularly for longer spans. The BT72/6 section was chosen to represent girders with a lighter, more efficient cross section. This girder was used with span lengths of 100 ft and 130 ft in the parametric study. The girder spacing used for these three girders throughout the majority of parametric study analyses was 8 ft. Preliminary studies indicated that girder spacings varying between 4.5 and 8 ft had a minor influence on bridge behavior. The box girder span length and girder spacing used in the parametric study were 100 ft and 11.7 ft, respectively. For AASHTO-IV, AASHTO-VI, and BT72/6 sections, deck dimensions were 92 in. by 6.5 in. For the box girder section, deck dimensions were 140 in. by 9 in. The dimensions for girder areas, composite section areas, and simple span composite dead load moments at midspan for the four sections are given in Table 8.

One of the main priorities of the parametric study was to determine the effect on bridge behavior of varying amounts of positive moment reinforcement at supports. For each analyzed combination of parameters, positive moment reinforcement was set equal to one or more of 0.2, 3.6, or 7.2 sq in. These values represent a range of reinforcement equivalent to one No. 4 bar up to twelve No. 7 bars and encompass the range of reinforcement areas specified by questionnaire respondents. The 0.2-sq in. reinforcement is intended to represent an unreinforced section. A small amount of reinforcement had to be used in the PBEAM program to obtain a satisfactory numerical solution. Bridges analyzed with 3.6 sq in. or 7.2 sq in. of positive moment steel will be referred to as reinforced. Bridges analyzed with 0.2 sq in. will be referred to as unreinforced.

Preliminary PBEAM results indicated that variations in deck and girder concrete compressive strength had a minor effect on bridge behavior. Therefore, for the majority of parametric study analyses, girder and deck concrete compressive strengths were 6,500 psi and 4,000 psi, respectively. Two ultimate creep coefficients were used throughout the parametric study. A value of 3.25 represented the high end of the range and 1.625 was used for the low end value. Three values of ultimate shrinkage strain were used in the parametric study. A value of 200 millionths was used for a low end value and 780 millionths was used to represent an unreinforced section. A small amount of reinforcement had to be used in the PBEAM program to obtain a satisfactory numerical solution. Bridges analyzed with 3.6 sq in. or 7.2 sq in. of positive moment steel will be referred to as reinforced. Bridges analyzed with 0.2 sq in. will be referred to as unreinforced.

Appendix D contains the parametric study results for PBEAM analyses of 41 combinations of variables. Continuity Connection Effects for Positive Moment. The effects of providing varying amounts of positive moment connection steel on typical bridge behavior when positive support restraint moments develop are illustrated in Figures 11 and 12. The results shown are from PBEAM analyses for AASHTO-VI girders with 130-ft span lengths and ultimate creep coefficient of 3.25. The girder age at which continuity was established was 17 days, and live load was applied at 650 days. The results when the deck was cast 7 days before the diaphragm and vice versa.

To evaluate the behavior of bridges under service conditions, bridge response was analyzed for the live load configuration shown in Figure 10(a). The pattern of live load was chosen because it is symmetrical about the central support and produces the maximum negative moment at the central support. The magnitude of the loads is based on the AASHTO (4) HS20-44 lane load with a girder spacing of 8 ft, two girders per lane of traffic, and an impact factor for span length equal to 130 ft. For purposes of comparison, the magnitude of load was not changed to account for different impact factors for 70-ft and 100-ft spans. For bridges with girder age at continuity of 17 days, live load was applied at 650 days. For bridges with girder age at continuity of 67 days or greater, live loads were generally applied approximately 30 days after continuity was established. However, for several runs with continuity at 67 days, live loads were applied at 650 days.

From responses to the questionnaire, it was learned that current bridge construction practices include a number of aspects. Girder age at the start of bridge construction varies from about 10 days up to about 300 days. The majority of respondents indicated that construction of deck and diaphragm fell into three general categories: (1) casting the deck and diaphragms simultaneously at various girder ages; (2) casting the deck approximately 7 to 10 days before the diaphragm at various girder ages; and (3) casting the diaphragm approximately 7 to 10 days before the deck at various girder ages.

For purposes of the parametric study, the majority of PBEAM runs were conducted assuming the deck and diaphragm were constructed simultaneously. The girder age at which continuity was established for these runs was either 17 or 67 days. Additional runs were conducted with girder age at continuity up to 320 days. Several runs were also done to investigate behavior

<table>
<thead>
<tr>
<th>Girder Type</th>
<th>Girder Cross Section Area, in.²</th>
<th>Composite Section Area, in.²</th>
<th>Midspan Composite Dead Load Moment, kip-in.</th>
</tr>
</thead>
<tbody>
<tr>
<td>AASHTO-IV</td>
<td>789</td>
<td>1387</td>
<td>21,700</td>
</tr>
<tr>
<td>AASHTO-VI</td>
<td>1685</td>
<td>1683</td>
<td>26,300</td>
</tr>
<tr>
<td>BT72/6</td>
<td>701</td>
<td>1299</td>
<td>20,300</td>
</tr>
<tr>
<td>Box</td>
<td>920</td>
<td>2180</td>
<td>34,100</td>
</tr>
</tbody>
</table>

*For simple span length = 100 ft

The pattern of live load was chosen because it is symmetrical about the central support and produces the maximum negative moment at the central support. The magnitude of the loads is based on the AASHTO (4) HS20-44 lane load with a girder spacing of 8 ft, two girders per lane of traffic, and an impact factor for span length equal to 130 ft. For purposes of comparison, the magnitude of load was not changed to account for different impact factors for 70-ft and 100-ft spans. For bridges with girder age at continuity of 17 days, live load was applied at 650 days. For bridges with girder age at continuity of 67 days or greater, live loads were generally applied approximately 30 days after continuity was established. However, for several runs with continuity at 67 days, live loads were applied at 650 days.

Figure 11. Central support moments for continuity at girder age of 17 days, loading at 650 days.
shown in Figures 11 and 12 and the following discussion are typical of all girder types, span lengths, and ultimate creep coefficient combinations analyzed in the parametric study for continuity age of 17 days and live load applied at 650 days. In these cases, a large proportion of girder prestress creep occurs after continuity is established, causing positive restraint moments to develop. Also, negative restraint moments caused by differential shrinkage between deck and girder concrete are lessened because a relatively small amount of girder shrinkage has occurred before the deck is cast.

Time-dependent restraint moments at the central support of the four-span bridge up to day 650 are shown in the left side of Figure 11. The right side of Figure 11 indicates moments upon incremental application of live load at day 650. The three curves on the graph are from PBEAM analyses with three quantities of positive moment reinforcement at supports, $A_r$. With positive moment reinforcement provided, $A_r$ equal to 3.6 or 7.2 sq in., positive restraint moments develop over time. At an age of 650 days, restraint moment at the central support is equal to about 8,000 kip-in. With a small amount of positive reinforcement, $A_r$ equal to 0.2 sq in., positive restraint moments are negligible. With a small amount of provided reinforcement, the girder end rotation causes cracks to develop in the bottom of the diaphragm. The flexural stiffness of the diaphragm is therefore reduced and restraint against girder end rotation is decreased. When a substantial amount of reinforcement is provided, girder end rotation is more effectively restrained.

Figure 11 also shows response of central support moments to application of live load at 650 days. Live load was applied in three increments to reach 25, 50, and 100 percent of the load. It can be seen that the behavior of the reinforced and unreinforced sections differs. For analyses of bridges with reinforced diaphragms, application of live load causes an immediate decrease of the central support moment. At 100 percent live load, the moments are negative. In general, moments decrease linearly up to 100 percent of live load. For the analysis of the unreinforced diaphragm bridge, application of live load causes only a slight decrease in central support moment. This results from the fact that girder end rotation due to the applied live load is not restrained because of the low rotational stiffness of the cracked diaphragm. The positive moment crack at the bottom of the diaphragm must close prior to inducing negative moment at the continuity connection.

Time-dependent interior span midspan moments up to day 650 are shown in the left side of Figure 12. The right side of Figure 12 indicates midspan moments due to incremental application of live load at day 650. The three curves on the graph are from PBEAM analyses with three quantities of positive moment reinforcement at supports. With provided positive moment reinforcement at the diaphragms, midspan moments increase due to the positive restraint moments which develop at the supports. On the other hand, with unreinforced diaphragms, midspan moments remain essentially constant through day 650. Because the girder ends are virtually unrestrained, small restraint moments develop at supports, and midspan moments remain approximately equal to the composite section simple span dead load moment of 44,500 kip-in. The difference in midspan moments at 650 days between the unreinforced and reinforced diaphragm analyses is due to the difference in restraint moments at supports.

Upon application of live load at day 650, midspan moments increase in amounts dependent on the degree of continuity at supports. For analyses of bridges with reinforced diaphragms, support regions have relatively high rotational stiffnesses. As a result, continuous sections at supports resist some of the applied live load and the increase in midspan moment is reduced. For the analysis with negligible positive reinforcement, support regions have very small rotational stiffnesses because of diaphragm cracking. Therefore, essentially all of the applied live load is resisted by bending of the composite girder and midspan moments increase substantially until girder end rotation results in closing of diaphragm cracks.

An important feature of the data shown in Figure 12 is that the resultant moment is the same regardless of the amount of positive moment reinforcement provided. The resultant moment is defined as the moment resulting from the summation of dead load, restraint, and live load plus impact moments. The resultant midspan moment is equal to 66,000 kip-in for the bridge analyzed in Figure 12. The average change in midspan positive moment with application of live load for the reinforced diaphragm analyses is 11,000 kip-in. For the unreinforced diaphragm analysis, change in midspan moment with application of live load is 20,000 kip-in. However, because of the differences in time-dependent restraint moments, net positive moments at midspan resulting from the combination of dead load, time-dependent restraint, and live load plus impact are virtually identical. This is a feature of behavior that was observed within all the analyses carried out for the various parameters used in this study.

Table 9 gives the parametric study results for bridges with 100-ft span lengths with various girder cross sections and ultimate creep coefficients. Resultant moments at interior span supports and midspan are given. These results, which are typical of parametric study results for age of continuity of 17 days, indicate that, for an interior span, the resultant midspan moment is practically identical for a bridge with and without positive moment reinforcement provided at the pier connections. Since providing positive reinforcement connections at piers is a time consuming and expensive procedure, the economical effect of minimizing or not providing positive moment steel at the piers...
should be considered in the design procedure of multispan bridges consisting of precast, prestressed girders made continuous.

The results in Table 8 also show influences of girder type and creep coefficient on behavior of this type of bridge. The four girders used in the parametric study represent a range of cross-sectional areas in use for medium to long span bridges. As may be noted in Table 9, sections with larger areas and as a result, larger dead loads, have larger resultant midspan moments. These range from about 30,000 kip-in. for BT72/6 to about 48,000 kip-in. for the box section. Higher ultimate creep coefficients result in more positive restraint moments at the supports. Also, upon application of live load, the girders with higher creep have more positive resultant moments at supports and midspan.

**Continuity Connection Effects for Negative Moment.** Results of the analyses indicate that negative restraint moments can develop in the diaphragms at the supports, dependent primarily on the age of the girder when the diaphragm and deck are cast. The maximum resultant negative moment that can develop depends on the differential age between the girder and deck, and on the age of the bridge when live load is applied. Figure 13 shows typical time-dependent restraint moments at the center support for a bridge with continuity made by casting the deck and diaphragm at a girder age of 67 days. The data shown in Figure 13 are for AASHTO-IV girders with 100-ft spans and ultimate creep coefficient of 1.625. This figure is typical of parametric study results for a late age of continuity of 67 days with deck and diaphragm cast simultaneously, regardless of girder type, ultimate creep coefficient, and amount of positive reinforcement at supports. High negative restraint moments develop initially due to differential shrinkage between the cast-in-place deck and the precast girder. At the age of 67 days, a large portion of girder concrete shrinkage has occurred. Therefore, the difference between deck shrinkage and remaining girder shrinkage is large and dominates restraint moment development immediately after continuity is established. As time progresses, creep reduces the large initial negative restraint moments. Figure 14 shows resultant moments at the center support for live load applied at 100 days and 650 days. It can be seen that negative resultant support moments are higher for the earlier age of loading. At 100 days, resultant moment at the central support is -15,300 kip-in.; and at 650 days, the resultant moment is -10,800 kip-in. There is a corresponding difference in resultant midspan moments for live load applied at the different ages.

Table 10 gives parametric study results for an interior span. Support and midspan resultant moments are listed for 100-ft and 130-ft girder lengths for various girder sections and ultimate creep coefficients. It can be seen that different amounts of positive reinforcing steel at supports have a negligible effect on resultant support and midspan moments. Because the positive reinforcing steel is in the compression zone of the section under negative moment, varying amounts of reinforcement have a small effect on bending stiffness. For a given girder type and span length, PBEAM predictions given in Table 9 indicate that resultant moments are independent of ultimate creep coefficient for age of continuity of 67 days and live loading at 100 days. This is because early age restraint moments are dominated by the negative restraint moment contribution of differential shrinkage.
Table 10. Resultant moments from parametric study—girder age at continuity 67 days, age at loading 100 days.

<table>
<thead>
<tr>
<th>Girder Type</th>
<th>Span Length, ft</th>
<th>Ultimate Creep Coefficient</th>
<th>Positive Reinforcement, in.</th>
<th>Resultant Moments, kip-in.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>At Support B</td>
<td>At Midspan</td>
</tr>
<tr>
<td>AASHTO-IV 100</td>
<td>3.25</td>
<td>1.2</td>
<td>-16,100</td>
<td>19,800</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.2</td>
<td>-16,000</td>
</tr>
<tr>
<td></td>
<td>1.625</td>
<td>1.2</td>
<td>-16,100</td>
<td>19,800</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.2</td>
<td>-16,000</td>
</tr>
<tr>
<td>BT2/6 100</td>
<td>3.25</td>
<td>1.2</td>
<td>-16,800</td>
<td>18,500</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.2</td>
<td>-15,100</td>
</tr>
<tr>
<td></td>
<td>1.625</td>
<td>1.2</td>
<td>-16,500</td>
<td>18,700</td>
</tr>
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<td></td>
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<td>-14,900</td>
</tr>
<tr>
<td>Box 100</td>
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<td>19,000</td>
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<td></td>
<td>0.2</td>
<td>-29,400</td>
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<td></td>
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<td>46,000</td>
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<td>-18,700</td>
</tr>
<tr>
<td>BT2/6 130</td>
<td>3.25</td>
<td>1.2</td>
<td>-17,100</td>
<td>30,700</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.2</td>
<td>-15,200</td>
</tr>
<tr>
<td></td>
<td>1.625</td>
<td>1.2</td>
<td>-16,400</td>
<td>30,500</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>0.2</td>
<td>-15,800</td>
</tr>
</tbody>
</table>

Table 11. Resultant moments for various girder ages at establishment of continuity.

<table>
<thead>
<tr>
<th>Girder Age at Continuity, Days</th>
<th>Girder Age at Loading, Days</th>
<th>Resultant Moments, kip-in.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>At Support B</td>
</tr>
<tr>
<td>67</td>
<td>100</td>
<td>-19,000</td>
</tr>
<tr>
<td>97</td>
<td>130</td>
<td>-27,200</td>
</tr>
<tr>
<td>190</td>
<td>230</td>
<td>-25,300</td>
</tr>
<tr>
<td>320</td>
<td>350</td>
<td>-29,900</td>
</tr>
</tbody>
</table>

Figure 13, the restraint moment may remain negative for the life of the structure. The response will be as a fully continuous girder for application of live load. As shown in Figure 16, with high creep values and/or earlier age of girder at the time of casting the diaphragm and deck, the restraint moment can become positive at late ages. At this time, some degree of effective continuity will be lost either because the positive restraint moment adds to the midspan moment or because of diaphragm cracking that must be closed with application of live load before inducing negative moments at the support.

Effects of Construction Sequence. Restraint moments at supports of bridges constructed of simple span prestressed girders made continuous are highly dependent on the timing of construction. The primary factor is girder age at the time continuity is established by construction of the cast-in-place deck and the diaphragm. However, the sequence of deck and diaphragm construction, either simultaneous or one before the other, also affects the development of restraint moments.

From the responses to the questionnaire, actual construction sequences fell into three general categories: deck and diaphragms...
cast simultaneously, deck cast before diaphragms, and diaphragms cast before deck. In some cases, respondents indicated that portions of the deck in positive moment regions were cast before the deck in negative moment regions and diaphragms.

For purposes of the parametric study, the majority of PBEAM runs were conducted for the deck and diaphragm cast simultaneously at girder ages of 17 days or 67 days. Resultant moments from PBEAM analyses for the deck cast before the diaphragms and the diaphragms cast before the deck are compared to the results for simultaneous casting in Table 12. The girder age at continuity is the age at which the diaphragm is cast. The analyses for the data in Table 12 were made for AASHTO-IV girders of 100-ft span length with ultimate creep coefficient equal to 1.625. For all PBEAM runs, the deck is cast over the full length of the girder at the indicated time.

The results in Table 12 show that for the construction sequence of the deck cast before the diaphragm compared to simultaneous casting, resultant moments at the supports and midspan have a higher positive value for both 17-day and 67-day continuity. This may be seen by comparing runs 1 and 2 with runs 6 and 7, and by comparing runs 3 and 4 with runs 8 and 9. When the deck is cast before the diaphragm, the two components contributing to negative restraint moments are reduced. When the deck is cast, girder end rotation due to the additional dead load of the deck is unrestrained. More importantly, end rotation due to differential shrinkage between the deck and girder is unrestrained until the diaphragm is in place. As a result, the negative restraint moment component and the potential for transverse cracking in the deck are reduced. In turn, resultant moments after application of live load have a higher positive value, as shown in Table 12.

When the diaphragm is cast before the deck, resultant moments are only slightly affected. For run 11 with a girder age at continuity of 67 days and deck cast at 74 days, results for loading at 100 days are virtually identical to run 3 with simultaneous deck and diaphragm casting. Comparing run 12 with run 5 for loading at 650 days, however, the resultant positive moment at midspan is reduced slightly by casting the diaphragm 7 days before the deck. For early age of continuity with the diaphragm constructed before the deck, run 10, resultant moments have a higher negative value than run 2 with deck and diaphragm cast simultaneously. With the construction sequence of diaphragm before deck, the diaphragm has attained a higher strength at the time the deck is cast. Therefore, the diaphragm

<table>
<thead>
<tr>
<th>Construction Sequence</th>
<th>Run No.</th>
<th>Girder Age at Deck Casting, Days</th>
<th>Girder Age at Continuity, Days</th>
<th>Girder Age at Loading, Days</th>
<th>Positive Reinforcement, in.²</th>
<th>Resultant Moments, kip-in.</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>At Support B</td>
<td>At Midspan</td>
</tr>
<tr>
<td>Deck and Diaphragm</td>
<td>1</td>
<td>17</td>
<td>17</td>
<td>650</td>
<td>7.2</td>
<td>1230</td>
</tr>
<tr>
<td>Simultaneous</td>
<td>2</td>
<td>17</td>
<td>17</td>
<td>650</td>
<td>0.2</td>
<td>230</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>67</td>
<td>67</td>
<td>100</td>
<td>7.2</td>
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<td></td>
<td>5</td>
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<td>67</td>
<td>650</td>
<td>0.2</td>
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</tr>
<tr>
<td>Deck Before Diaphragm</td>
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<td>10</td>
<td>17</td>
<td>650</td>
<td>7.2</td>
<td>5220</td>
</tr>
<tr>
<td></td>
<td>7</td>
<td>10</td>
<td>17</td>
<td>650</td>
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</tr>
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<td>67</td>
<td>74</td>
<td>100</td>
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<td>74</td>
<td>100</td>
<td>0.2</td>
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<tr>
<td>Diaphragm Before Deck</td>
<td>10</td>
<td>17</td>
<td>10</td>
<td>650</td>
<td>0.2</td>
<td>-490</td>
</tr>
<tr>
<td></td>
<td>11</td>
<td>74</td>
<td>67</td>
<td>100</td>
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<td>74</td>
<td>67</td>
<td>650</td>
<td>7.2</td>
<td>-13200</td>
</tr>
</tbody>
</table>

Table 12. Resultant moments for various construction sequences.
resists some negative moment induced by the deck dead load and develops higher negative restraint moment from differential shrinkage between the newly cast deck and the restrained girder. The end result is that restraint moments and resultant moments after application of live load have a somewhat higher negative value. This sequence increases the probability of establishing full continuity and reducing resultant positive moments at mid-span but only slightly. In turn, the potential for transverse deck cracking is slightly increased.

**FLEXURAL STRENGTH**

In a continuous bridge structure, the maximum strength is reached when a full mechanism develops after redistribution of moments. When the mechanism forms, the structure theoretically has no resistance to additional load and failure occurs. Ideally, a bridge girder should be designed to be capable of attaining the full mechanism state without premature failure of connections in order to obtain a maximum safety margin against collapse of the bridge.

For an interior span of a continuous bridge, a full mechanism occurs when plastic hinges develop at each support and near midspan. Depending on the configuration of load and relative positive moment and negative moment structural resistance, the first plastic hinge(s) will form at the supports or near midspan. After the occurrence of the first hinge(s), the yielded region(s) must possess adequate ductility to allow the redistribution of moments until the full mechanism is formed.

If the ratio of negative to positive moment capacity is equal to the ratio of negative to positive elastic moment under the given loading, hinges will form simultaneously in positive and negative moment regions at the maximum load. In this case, the required inelastic rotation at the central support will be zero. When the ratio of negative to positive moment capacity is less than the ratio of elastic moments, the negative moment hinge will form first. The required inelastic rotation at the central support will then be dependent on the ratio of negative to positive moment capacity. As the ratio of moment capacities approaches the ratio of elastic moments, the rotational demand decreases. Therefore, for a given continuous bridge configuration in which negative moment hinges form first, a lightly reinforced section at the supports will require more ductility than a heavily reinforced section to form a full mechanism under the maximum load.

In a bridge constructed of prestressed concrete girders with a composite cast-in-place deck, the positive moment region within the span is inherently much more ductile than the negative moment region at the supports. The large compressive area of the concrete deck in the positive moment region ensures that yielding of prestressing steel occurs before crushing of concrete. As a result, the positive moment region reaches its flexural strength after a large amount of deformation, giving adequate warning of failure. The negative moment region has only the bottom flange area and web of the prestressed girders available for compression. Because of this relatively small compression area, crushing of concrete in the bottom of the girder can occur before yielding of the reinforcement in the deck, particularly for heavily reinforced decks. This type of failure is brittle, with little or no deformation prior to failure. If brittle failure of negative moment regions occurs before the positive moment capacity is reached, the full mechanism will not form and the maximum strength of the span will not be reached. In order for sufficient redistribution of moments to occur to form the full mechanism and to avoid brittle failures, adequate negative moment ductility must be provided.

The current AASHTO Specifications (14) Article 9.7.2.3.2 implies a critical value for deck reinforcement ratio, \( p = A_d / bd \), of 0.015. It appears that this value is based on testing (6) that included 40 ksi deck reinforcement, 5,000 psi to 6,000 psi concrete, and an AASHTO-type girder. Therefore, an investigation of negative moment ductility which included effects of variations in deck reinforcement yield strength, concrete compressive strength, and relative girder bottom flange area was needed.

This section of the report describes parameters and results of an analytical study conducted to investigate the effects of varying amounts of negative moment reinforcement, various girder bottom flange configurations, and varying material properties on the negative moment ductility of composite deck-girder sections. Results of the study are used to establish criteria to limit the amount of reinforcement in the deck to ensure ductile behavior.

**Analytical Study**

The two main parameters used in the study were size and shape of girder bottom flange and amount of negative moment reinforcement. Figure 17 shows the five girder sections used: California 66, BT72/6, AASHTO-IV, AASHTO-VI, and BIV-48. These girders represent a range of girder bottom flange configurations in current use. The California 66 and BT72/6 girders represent deep girders with a small bottom flange area. The AASHTO-IV, AASHTO-VI, and BIV-48 are girders with large bottom flange areas. Girder bottom flange areas range from 27 percent to 46 percent of the total girder area for BT72/6 and AASHTO-IV, respectively. Negative moment reinforcement areas of 8, 16, and 24 sq in. were used for each of the girders analyzed. Reinforcement ratios based on width of compression flange and depth to reinforcement ranged from 0.0036 to 0.0109 for BIV-48 up to 0.0060 to 0.0180 for California 66. All five girders with three amounts of deck reinforcement were analyzed with girder concrete compressive strength of 6,500 psi and deck steel yield stress of 60,000 psi. Analyses were also conducted with 5,000 psi concrete and 40,000 psi deck steel to investigate the influence of material properties on ductility.

**Results of Analytical Study**

Program WALL—HINGE (57) was used for the study of negative moment ductility. The program generates information about elastic and inelastic behavior of girder sections up to failure. Program results include bending moment, shear force, steel and concrete stresses and strains, neutral axis depth, deformation and mode of failure. Deformation results include rotation at selected locations. To evaluate rotational ductility of analyzed sections, rotations at a distance equal to \( d \) away from the support were used. The distance \( d \) is the distance from the bottom of the compression flange to the centroid of deck reinforcement. This length was taken as representative of the length of the post-yield hinging region.
Figure 17. Girder sections for flexural strength study.

Figure 18 shows typical moment-rotation relationships from WALL_HINGE analyses. Comparisons of WALL_HINGE analyses to test results from Ref. 6 are presented in Chapter Two.

Required Rotations. Calculated rotation capacities from the WALL_HINGE program were compared to required rotations developed using an analysis method presented by Park and Paulay (58). Initially, analyses were made with PBEAM to attempt to define required rotations. However, results indicated that PBEAM was not reliable in finding convergence at high load levels when flexural hinges were forming and slopes of material stress-strain relationships were relatively flat. Therefore, the analysis method presented by Park and Paulay (58), with a constant effective flexural rigidity calibrated against PBEAM results, was used to define required rotations. This method is further described in the remainder of this section.
Required rotations were calculated for the central support of a two-span continuous beam. Each span was loaded with uniform load and a single point load with relative magnitudes conforming to AASHTO-HS lane loading as shown in Figure 19(a). Under these conditions, with typical ratios of negative to positive moment capacity, the first hinge will form at the central support, as shown in Figure 19(b). The required hinge rotation, \( \theta_r \), in Figure 19(c), is the change in slope at the central support determined from an elastic analysis of the maximum load condition. The maximum load condition causes formation of the failure mechanism. The required rotation is determined by assuming a frictionless hinge at the central support and calculating the rotation at the support under the combination of maximum external load and the negative maximum moment at the interior support hinge. This method is based on the following assumptions. The moment-curvature relationships for positive and negative moment are bilinear, with post-yield moments constant and equal to flexural strength moments. An effective flexural rigidity, \( EI \), is assumed to be constant over the entire girder length.

Following is the derivation of the expression used to calculate \( \theta_r \) for girders analyzed in this study. The rotation at the central support under maximum load is:

\[
\theta_r = \frac{L}{EI} \left[ \frac{w_u L^2}{24} + \frac{P_u L}{16} - \frac{M'_u}{3} \right]
\]  

(3)

The terms used in Eq. 3 are defined in Figure 19. The ultimate load is assumed to be a multiple of AASHTO lane loading. Therefore, \( w_u \) is proportional to 0.64 kip/ft and \( P_u \) is proportional to 18 kip, and

\[
\alpha_2 = \frac{w_u}{0.64} = \frac{P_u}{18}
\]

(4)

\[
w_u = \frac{P_u}{28.125}
\]

(5)

Substituting this into Eq. 3 gives

\[
\theta_r = \frac{L}{EI} \left[ \frac{P_u L^2}{675} + \frac{P_u L}{16} - \frac{M'_u}{3} \right] \times 12
\]

(6)

where \( L \) is in feet, moment is in kip-ft, and other quantities are in inches and kips. Assuming that the positive moment hinge forms under the point load at midspan:

\[
M_u = \frac{P_u L}{4} + \frac{w_u L^2}{8} - \frac{M'_u}{2}
\]

(7)

\[
P_u L = (M_u + M'_u/2)/(L/225 + \gamma_0)
\]

(8)

Substituting \( P_u L \) into Eq. 6 gives the expression for required rotation, \( \theta_r \):

\[
\theta_r = \frac{M'_u L}{EI} \left[ \left( \frac{M_u}{M'_u} + \frac{1}{2} \right) \left( \frac{L/675 + \gamma_0}{L/225 + \gamma_0} \right) - \frac{1}{3} \right] \times 12
\]

(9)

It can be seen from the expression for \( \theta_r \), that the required central support rotation depends on the magnitude of the constant \( EI \), the magnitudes of positive and negative moment strengths, and span length. Where possible, values selected for calculation of \( \theta_r \) were chosen to produce a conservative (large) estimate of required rotation. Rotational demand increases with decrease of \( EI \) and increase of span length.

Values for flexural rigidity, \( EI \), were calculated using a weighted averaging procedure which gave conservative values compared to results of PBEAM analyses. As suggested by ACI 318-83 (68) Section 9.5, a weighted average of \( EI \) values from positive and negative moment regions can be used to represent a constant flexural rigidity. Several PBEAM analyses were conducted in which girders were loaded to a level well beyond the load producing yielding of support regions. An average value of \( EI \) was computed from elastic deflection equations using midspan deflection of a loaded interior span, applied external loads, and changes in support moments. This calculated average \( EI \) was considered an effective constant \( EI \) for the span.

Based on the PBEAM analyses, a conservative value for the effective \( EI \) for use in calculating required rotation was determined to be the sum of 80 percent of the gross composite section \( EI \) and 20 percent of the elastic cracked section negative moment \( EI \) from WALL_HINGE results.

Span lengths were chosen to be near the upper end of the feasible span range for a particular girder.

Positive moment capacities, \( M'_{uw} \), were calculated using AASHTO procedures for each girder with 8, 16, and 24 sq in. of deck reinforcement. Positive moment capacities calculated using AASHTO procedures agreed well with WALL_HINGE results. Negative moment capacities for use in calculating required rotation were reduced by the service dead load simple span moment due to girder and deck weight. This accounts for the fact that positive live load plus impact moments are superimposed on the simple span dead load moment. The discontinuity in slope at the support due to deck and girder dead load is accommodated in the casting of the diaphragm.

Negative moment capacities, \( M'_{uw} \), were calculated using AASHTO procedures for each girder with 8, 16, and 24 sq in. of deck reinforcement. Negative moment capacities calculated using AASHTO procedures agreed well with WALL_HINGE results. Negative moment capacities for use in calculating required rotation were reduced to 80 percent of calculated values. This accounts for a possibility of negative restraint moment equal to 20 percent of the strength existing at the support before application of live load.

Resulting ratios of reduced negative to reduced positive moment capacity used for calculating required rotations ranged from 0.18 to 1.14.

For the two-span bridge with AASHTO-HS lane loading, the ratio of elastic negative support moment to midspan positive moment is about 1.66 for span lengths considered here. Therefore, negative moment hinges form first for all cases analyzed in this study.

Rotation Capacity. Table 13 gives required central support rotation, \( \theta_r \), and rotation capacities, \( \theta_c \), calculated at a distance \( d \) from the support using Program WALL_HINGE. Calculated required rotations, \( \theta_r \), averaged 0.007, 0.005, and 0.004 radians for 8, 16, and 24 sq in. of deck reinforcement, respectively. Both required rotations and rotation capacities decrease with increasing amounts of deck reinforcement. In only one
case, BT72/6 with 24 sq in. reinforcement, is required rotation greater than rotation capacity.

Table 14 lists ratios of rotational capacities from WALL_HINGE divided by required rotations; ultimate curvature, $\phi_u$, divided by yield curvature, $\phi_y$; and reinforcement ratio, $p$, divided by balanced reinforcement ratio, $p_b$, for each analysis. Rotation ratio is calculated from data in Table 13. The ratio of curvatures or ductility ratio was determined from WALL_HINGE results by dividing rotation at the ultimate moment by rotation at yield of deck reinforcement. Since average curvature can be obtained by dividing rotations at $d$ from the support by the distance $d$, the ratio of ultimate to yield rotations is equal to the ratio of ultimate to yield curvatures.

The typical failure mode for these analyses was flexural compression, in which yield of deck reinforcement was followed by crushing of compression zone concrete. As can be seen by examining the data in Table 14 and the example output in Figure 18, girders with larger bottom flange areas, such as AASHTO-VI, are much more ductile than sections with small bottom flange areas, such as BT72/6. The ratio of calculated to required rotation, $\theta_u/\theta_r$, averages 2.2 for AASHTO-VI and 1.1 for BT72/6. The ductility ratio, $\phi_u/\phi_y$, averages 6.0 for AASHTO-VI and 2.9 for BT72/6.

The data in Table 14 show that for a given area of deck reinforcement, use of lower strength girder concrete reduces ductility. With lower strength girder concrete, a larger compression zone is required to equilibrate the force in the yielded deck reinforcement. For a given area of deck reinforcement, use of Grade 40 deck reinforcement significantly increases ductility, as shown by rotation ratio and ductility ratio values in Table 14. The compression zone is required to equilibrate a significantly lower force when deck reinforcement yields. As a result,
Table 13. Rotation at central support—required and WALL-HINGE results.

<table>
<thead>
<tr>
<th>Girder</th>
<th>Span Length, ft</th>
<th>Concrete Strength, psi</th>
<th>Deck Reinforcement, in.2</th>
<th>Rotation Ratio, $\theta_{c,rad.}/\theta_{r,rad.}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cal. 66</td>
<td>100</td>
<td>60000</td>
<td>8</td>
<td>$0.0035, 0.0060$</td>
</tr>
<tr>
<td>AASHTO-IV</td>
<td>100</td>
<td>60000</td>
<td>16</td>
<td>$0.0021, 0.0039$</td>
</tr>
<tr>
<td>AASHTO-VI</td>
<td>130</td>
<td>60000</td>
<td>24</td>
<td>$0.0027, 0.0039$</td>
</tr>
<tr>
<td>BT72/6</td>
<td>130</td>
<td>60000</td>
<td>8</td>
<td>$0.0019, 0.0026$</td>
</tr>
<tr>
<td>RIV-48</td>
<td>90</td>
<td>60000</td>
<td>24</td>
<td>$0.0020, 0.0027$</td>
</tr>
</tbody>
</table>

Table 14. Comparison of rotation and ductility ratios.

<table>
<thead>
<tr>
<th>Girder</th>
<th>Concrete Strength, psi</th>
<th>Deck Reinforcement, in.2</th>
<th>Rotation Ratio, $\theta_{r,rad.}/\theta_{c,rad.}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cal. 66</td>
<td>65000</td>
<td>8</td>
<td>$0.0061, 0.0093$</td>
</tr>
<tr>
<td>AASHTO-IV</td>
<td>65000</td>
<td>16</td>
<td>$0.0040, 0.0045$</td>
</tr>
<tr>
<td>AASHTO-VI</td>
<td>65000</td>
<td>24</td>
<td>$0.0062, 0.0067$</td>
</tr>
<tr>
<td>BT72/6</td>
<td>65000</td>
<td>8</td>
<td>$0.0061, 0.0093$</td>
</tr>
<tr>
<td>RIV-48</td>
<td>65000</td>
<td>16</td>
<td>$0.0040, 0.0045$</td>
</tr>
</tbody>
</table>

prior to failure the compression zone can accommodate more deformation and force as strain hardening of deck steel occurs.

Use of the reinforcement ratio $\rho$ without consideration for cross-sectional shape or material strengths is not a particularly good indicator of ductility. The ratio of $\rho$ to $\rho_b$ was considered likely to be a better indicator in that $\rho_b$ includes the effects of $f'_{ce}$ and cross-sectional shape as follows. The reinforced concrete section which resists negative moment at supports consists of bottom flange and web concrete in compression and deck reinforcement in tension. In calculating the balanced reinforcement ratio, the actual compression area of concrete in the bottom flange and web must be used. At the balanced condition, the extreme compression fiber is assumed to reach a strain of 0.003 at the same time as deck reinforcement reaches yield strain. The effects of reinforcement and prestressing strand in the bottom flange are neglected. Using the assumed linear strain distribution, the compression block depth can be determined from the neutral axis depth.

$$x_b = \beta_1 \frac{87,000}{87,000 + f_v} d$$

where: $\beta_1$ = factor defining depth of compression block, from ACI 318-83 Section 10.2.7.3 (68); $f_v$ = steel yield stress, psi; and $d$ = depth from extreme compression fiber to centroid of deck reinforcement, in.

The balanced reinforcement ratio, $\rho_b$, can then be calculated:

$$\rho_b = \frac{0.85 f'_{ce} (A_f + (x_b - h_f)t_w)}{f_f b d}$$

where: $f'_{ce}$ = girder concrete compressive strength, psi; $A_f$ = cross-section area of bottom flange, up to junction with web, sq in.; $x_b$ = depth of compression block, in.; $h_f$ = depth of bottom flange, up to junction with web, in.; $t_w$ = web thickness, in.; $f_f$ = steel yield stress, psi; $b$ = width of bottom flange, in.; and $d$ = depth from extreme compression fiber to centroid of deck reinforcement, in.

**Design Implications.** Requirements of ACI 318-83 Section 8.4.3 (68) limit reinforcement ratio for continuous non prestressed flexural members to 0.5 times the balanced reinforcement ratio if moment redistribution is to be allowed. Therefore, a reinforcement ratio of 0.5 times $\rho_b$ was investigated as a possible limit to ensure sufficient ductility to form the full failure mechanism in bridges of the type investigated in this study. In Figure 20, the ratio of rotation from WALL-HINGE results to re-
The reinforcement ratio is calculated by dividing deck steel area by the product of bottom flange width and depth from extreme compression fiber to centroid of deck steel. No steel in compression zone was included. The single section with rotation less than required has a reinforcement ratio of 0.78 times balanced. The trend of the data is negatively sloped, but there is a large amount of scatter. All analyzed sections with less than 50 percent of the balanced reinforcement ratio theoretically had adequate rotation to form the failure mechanism.

In Figure 21, the ductility ratio, \( \phi_c/\phi_f \), is plotted against the reinforcement ratio divided by \( \rho_b \). The data show a strong trend of decreasing ductility with increasing percentage of balanced reinforcement ratio. The intersection of 0.5 times \( \rho_b \) and the best fit exponential curve occur at a ductility ratio of 3.4. All analyzed sections with reinforcement ratios less than or equal to 50 percent of the balanced reinforcement ratio had ductility ratios greater than or equal to 3.4. All analyzed sections with reinforcement ratios greater than 50 percent of the balanced had ductility ratios less than 3.4. Although all but one of the analyzed sections with reinforcement ratio greater than 50 percent of balanced reinforcement ratio theoretically have sufficient ductility to form a full failure mechanism, these failures will occur with a relatively small amount of deformation prior to failure. With deck reinforcement limited to 50 percent of the balanced reinforcement ratio, composite girder-deck sections will have adequate rotation available to form the failure mechanism and sufficient ductility to ensure that failure occurs with enough deformation to provide warning.

Table 15 contains limiting reinforcement ratios and deck steel quantities for the girder sections and material properties used in this study. Depth to reinforcement is girder depth plus 4 in.

It can be seen that limiting reinforcement ratios for Grade 60 deck steel are generally less than the limit of 0.015 implied in Section 9.7.2.3.2 of the 1983 AASHTO Code (14).

### Analysis Procedures

Results of the questionnaire indicated that the method of design most commonly used was the method published by PCA (12). In this section of the report, the PCA method is described briefly and predicted moments using the PCA method and the computer program PBEAM are compared. New simplified computer programs developed in this project and proposed for use in calculating design moments are then presented.

#### Table 15. Deck reinforcement limits.

<table>
<thead>
<tr>
<th>Girder</th>
<th>( f'_c ) psi</th>
<th>( f'_y ) psi</th>
<th>( \text{Max. } 0.5 \rho_b )</th>
<th>Maximum ( A_{12} ), in.(^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cal. 66</td>
<td>6500</td>
<td>60,000</td>
<td>0.0110</td>
<td>14.6</td>
</tr>
<tr>
<td>AASHTO-IV</td>
<td>6500</td>
<td>60,000</td>
<td>0.0130</td>
<td>19.6</td>
</tr>
<tr>
<td>AASHTO-VI</td>
<td>6500</td>
<td>60,000</td>
<td>0.0113</td>
<td>24.0</td>
</tr>
<tr>
<td>BT72/6</td>
<td>6500</td>
<td>60,000</td>
<td>0.0084</td>
<td>15.3</td>
</tr>
<tr>
<td>BIV-48</td>
<td>6500</td>
<td>60,000</td>
<td>0.0087</td>
<td>19.2</td>
</tr>
<tr>
<td>Cal. 66</td>
<td>5000</td>
<td>60,000</td>
<td>0.0091</td>
<td>12.1</td>
</tr>
<tr>
<td>AASHTO-IV</td>
<td>5000</td>
<td>60,000</td>
<td>0.0105</td>
<td>15.8</td>
</tr>
<tr>
<td>Cal. 66</td>
<td>6500</td>
<td>40,000</td>
<td>0.0183</td>
<td>24.3</td>
</tr>
<tr>
<td>AASHTO-IV</td>
<td>6500</td>
<td>40,000</td>
<td>0.0208</td>
<td>31.5</td>
</tr>
</tbody>
</table>
PCA Method

In current design practice, the PCA method developed by Mattock (12) is generally used for predicting restraint moments at supports. For this analysis, it is assumed that the distribution of moments and forces will change toward that which would have occurred if the loads applied to the individual elements before continuity was established had, instead, been applied to the structure after continuity was established. A similar approach to account for time-dependent forces in continuous structures built in stages is given in Ref. 31.

Using this method, the restraint moments due to dead load, prestress, and differential shrinkage between deck slab and girder are calculated. These moments are calculated for a continuous girder, assuming rigid connections between individual spans at the piers. Any convenient method for the analysis of statically indeterminate structures may be used.

The creep restraint moments are determined by multiplying the dead load and prestress moments by a coefficient \((1-e^{-\phi})\). The coefficient \(\phi\) is the ratio of creep strain to elastic strain. The resulting restraint moments are those which will be caused eventually by creep of the precast girder after the creation of continuity.

RestRAINT moments due to differential shrinkage are determined using a multiplier of \((1-e^{-\phi})/\phi\).

The restraint moments over piers are calculated as the sum of moments due to creep and differential shrinkage. The maximum positive and negative moments due to live load and impact are determined from analysis of the girders as a fully continuous beam. The time-dependent restraint moments are superimposed on the live load and impact moments for design of the positive moment connections at the supports and for design of the girder for positive midspan moments. The negative moment connections are designed for the full negative moment due to live load and impact without consideration of the time-dependent restraint moments. The PCA design procedure does not address design implications of situations in which negative restraint moments occur.

Comparison of PCA Method and PBEAM Analyses

The accuracy of the PCA method of design of continuous highway bridges with precast, prestressed concrete girders was evaluated using the computer program PBEAM (53). For the purpose of comparison, a sample calculation was taken from the PCA design procedure publication (12). The positive restraint moments at piers due to creep and shrinkage, and negative moments from live load plus impact, were calculated for a bridge with four 130-ft spans, shown in Figure 10(a). Degree of continuity was studied, assuming continuity connections are made at 17, 37 or 67 days after girder prestress release. Analyses were also carried out assuming a reduced amount of positive moment reinforcement and reduced tensile capacity of the concrete in the continuity connection.

The following data from the PCA example were used: exposure at 50 percent relative humidity, ultimate shrinkage equal to 0.0006 in./in., ratio of creep strain per psi of stress to elastic strain per psi of stress with a continuity connection made at 28 days, \(\phi = 1.95\), which corresponds to an ultimate \(\phi = 3.25\). All other design criteria for the Type VI AASHTO girder used for this study are given in the PCA example (12). For evaluation of live load response, AASHTO HS20-44 lane load was applied at spans BC and CD only, as shown in Figure 10(a).

Results of the comparison between the PCA method and the time-dependent computer analyses are presented in Tables 16 and 17. Restraint moments at the cast-in-place connections at the Piers B and C are given in Table 16 for 650 days after casting the girder. Resultant moments, including live loads, in the girders at an age of 650 days are presented in Table 17.

As can be seen from Table 16, restraint moments at Support B for both methods are similar for the age of continuity of 17 days. However, as the age at continuity increases, so does the difference between the computer analysis and the PCA method. The same relationship between the restraint moment and the age of continuity can be seen at Support C. Both methods of analysis indicate a tendency of the positive restraint moment to decrease with the increased continuity age. However, the time-dependent computer analysis predicts significantly more change and reversal of sign of the restraint moment at age of continuity of 67 days. The largest absolute difference between the PCA method and time-dependent computer analysis results occurs at Support B for the age of continuity of 67 days.

Differential shrinkage induces a negative restraint moment and creep induces a positive restraint moment. Therefore, the data in Table 16 demonstrate that differential shrinkage restraint moment becomes more influential with increasing age at continuity and creep becomes less influential than is predicted by the PCA method. This has the effect of decreasing the probability of positive moment cracking at the connection and avoiding the behavior illustrated in Figure 8. However, the probability of negative moment cracking at the connection is increased.

Comparison of resultant moments, including restraint mo-
ments and dead load plus live load plus impact moments at Supports B, C, and midspan for different ages at continuity, are shown in Table 17. The PCA method assumes that live load is applied to the elastic continuous structure. This elastic analysis does not consider the finite length of the connection nor does it consider the loss of stiffness with possible cracking in the connections. The negative moments over piers from live load plus impact shown in Figure 10(a) for the fully continuous beam are $-447.0$ kip-ft at B, and $-1,341$ kip-ft at C.

The PBEAM computer analysis for live load plus impact applied at girder age of 650 days accounted for realistic stiffness of girders at this age, including finite length of the connection and the effects of cracking of the concrete in the connections. Comparing results from Table 16, the PCA method predicts the highest negative moment to occur at Support C for continuity age of 67 days with a value of $-1,119$ kip-ft. The computer solution shows the highest moment to be $-1,525$ kip-ft and to occur at Support B. Even though there is a difference in the relative magnitude of negative moments at Support B and Support C, it is interesting to note that maximum midspan moments are practically the same for two methods for the 17-day age of girder continuity. That may not be the case for a different structure. However, in this example, with increased age of continuity of 37 days and 67 days, the value of midspan moments is higher and, therefore, more conservative when calculated by the PCA method. The data in Table 16 suggest that, although more negative moment reinforcement might be required, there is a potential for more economical design for positive moment in the prestressed girders depending on the age at continuity.

It should be noted, however, that the degree of continuity is not only dependent on the age at continuity but also on the age at application of service load. For age of continuity at 67 days, negative moment at C from PBEAM analyses changes from $-809$ ft-kip to $-1,225$ ft-kip when loaded at 100 days rather than 650 days. This demonstrates that while long-term effects produce the more critical situation for design for positive moments, short-term loading effects are more critical for negative moment.

To examine the effects of joint stiffness, comparable analyses were made assuming only one-half the amount of positive moment reinforcement. The PCA sample calculation resulted in a required 7.20 sq in. of positive reinforcement. The girders were reanalyzed using only 3.60 sq in. of positive reinforcement. The results of PBEAM analysis for restraint moments and resultant moment with application of live loads are given in Tables 16 and 17. The moments predicted using the PCA method are not affected by the amount of positive moment reinforcement and are repeated in Tables 16 and 17 for comparison purposes. These data indicate that, for this example, the long-term positive restraint moments are sensitive to the amount of positive reinforcement provided. However, the net effect on the resultant midspan positive moments with live load is not significant.

Some of the factors that contribute to the differences in calculated restraint and resultant moments are discussed below. A major difference is that the PCA method assumes full structural continuity for calculation of moments. Supports at piers are considered to be ideal pin supports. The PBEAM analysis considers the finite length of the diaphragm between supported ends of adjacent girders. The PBEAM analysis also accounts for cracking of concrete and yielding of reinforcement as critical moment levels are reached. Therefore, a realistic stiffness of support regions is used in the determination of restraint and resultant moments. The PCA method also has limitations in the handling of time-dependent effects. The design method in Ref. 12 does not incorporate up-to-date models for shrinkage and creep of concrete. PBEAM uses more recent models, such as that of ACI Committee 209 (17), for prediction of time-dependent behavior. Another advantage of PBEAM's analysis is that separate time-dependent functions can be used for deck and girder concrete shrinkage. The PCA method uses the same time-dependent curve for both deck and girder concrete shrinkage. The PBEAM analysis incorporates an incremental analysis using the method of superposition. This allows the time history of behavior to be studied. The PCA method is configured to produce restraint moments at one point in time rather than a complete history. Also, the shrinkage restraint moment component in the PCA method is defined by an equation which does not correctly account for compatibility between the girder and deck as shrinkage occurs. This is correctly accounted for in the analyses using PBEAM. These factors contribute to differences in moments shown in Tables 16 and 17 for PBEAM and PCA method results. Also, Ref. 12 does not include consideration of negative restraint moments in the design procedure.

Computer Programs for Proposed Analysis Procedures

Determination of time-dependent effects for this type of bridge is a necessary part of analyzing behavior of the structure. The degree of continuity to be counted on for reduction of midspan live load plus impact moments can vary from essentially zero to fully continuous, depending on time-dependent effects and construction timing and sequence. In order to determine design moments for service conditions, restraint moments due to creep and shrinkage should be evaluated to determine the appropriate degree of structural continuity. The current restraint moment analysis method from PCA's design procedure (12) has been shown to have shortcomings. The computer program PBEAM is capable of carrying out the complex analyses accounting for the time-dependent effects. However, use of PBEAM is very cumbersome, time consuming, and requires a large amount of computer memory. There was a need for an improved simplified analysis procedure for use in design.

One of the complex time-dependent effects modeled by PBEAM was the opening of cracks in the bottom of the diaphragm when positive moment reinforcement is not provided. However, based on parametric study results, resultant moments at midspan are nearly identical for a given situation regardless of the amount of positive moment reinforcement in place at the supports. This is illustrated in Figure 22, in which moment diagrams on the left are for an early age of continuity structure with positive moment reinforcement and on the right for the same structure without positive moment reinforcement. Dead load moments are the same. With time-dependent effects, positive restraint moments develop for the structure on the left. Without positive reinforcement, cracks occur and little or no positive restraint moment develops for the structure on the right. With application of additional dead load and live load plus impact, positive midspan moment increments for the continuous structure are less than for the structure in which cracks may have opened because of the lack of positive moment reinforcement. However, resultant midspan moments, equal to superposition of dead load, time-dependent, additional dead load, and
live load plus impact moments, are essentially the same. This results because the loss of stiffness and structural continuity due to opening and closing of the crack at the bottom of the diaphragm when positive moment reinforcement is not provided is compensated for by the restraint moment that develops if positive moment reinforcement is provided. Therefore, either of the two routes shown in Figure 22 may be used to determine positive midspan service moment.

The simplest method is to assume full structural continuity for calculation of both live load plus impact and time-dependent restraint moments. Because development of negative restraint moments occurs with full structural continuity until the deck cracks, this method is appropriate for calculation of positive and negative restraint moments.

A computer program was developed as an improved method to predict restraint moments at redundant supports of bridges constructed of precast, prestressed girders made continuous. The program, called BRIDGERM, is described in detail in Appendix E. A second program, called BRIDGELL, also described in Appendix E, was developed to calculate maximum moments under AASHTO HS live load plus impact specifications (14). Documentation of the programs, user instructions, and source listings are included in Appendix E. Example runs are also included in Appendix E. Descriptions of the programs are given in the following sections.

Calculation of Restrains. Program BRIDGERM was developed based on the PCA restraint moment calculation procedure in Ref. 12. Modifications to the PCA method were made to improve the analysis. Separate time-dependent functions are provided for girder concrete creep, deck concrete shrinkage, and girder concrete shrinkage. The time-dependent functions used in BRIDGERM are those suggested by ACI Committee 209 (17) for creep coefficient, shrinkage of moist-cured concrete, and shrinkage of steam-cured concrete, respectively. Ultimate values of creep coefficient, deck shrinkage strain, and girder shrinkage strain are provided by the user. Deck concrete compressive strength also varies with time according to the ACI-209 recommended time curve, assuming moist-cured concrete with Type I cement. Deck concrete modulus of elasticity is calculated from the time-dependent compressive strength using the relationship in AASHTO (14). Prestress force is determined as a function of time using the PCI prestress loss calculation procedure in Ref. 41. The stress at the strand centroid due to restraint moments is included in the loss calculation.

An additional modification involves use of a simplified bridge model for calculating the elastic distribution of restraint moments. A single interior span is supported by a double pinned support at each end, as shown in Figure 23. The double pinned support accounts for the finite length of the diaphragm. An exterior span is supported by a single pin at one end and a double pinned support at the other end. The distance between the double supports (XLD) should be taken as the distance between the centerline of the support bearings of adjacent girders over a common pier. For purposes of elastic analyses the ratio of sectional stiffness (EI) of the girder to the sectional stiffness of the diaphragm between supports was taken to be one. Because of the high stiffness of the double support region (assuming no uplift at either reaction), the influence of adjacent spans on restraint moments in the subject span can be neglected.

The analysis is conducted for typical exterior and interior spans in a multispans continuous bridge. For a two-span bridge, the analysis is modified to account for two adjacent exterior spans. For a three-span bridge, the analysis is conducted for an exterior span and for an interior span with exterior spans adjacent to each end. For bridges of four spans and greater, restraint moments are calculated for exterior spans, interior spans adjacent to an exterior span, and interior spans adjacent to interior spans at each end. The analysis procedure allows for the possibility of uplift at the first interior support region when the change in moment over the support region causes one reaction to become negative. In this case, the model is adjusted to account for the reduced stiffness in the support region and the effect of the adjacent span.

The analysis in BRIDGERM is conducted by superimposing restraint moment increments calculated over a series of time intervals. The user specifies the girder age at which continuity is established and the age at which the deck is in place. In general, these ages should be assumed to be the same unless it is specifically known that there will be a difference of more than several days. The program calculates prestress losses from the user-specified age of prestress release until continuity is established. When the deck is in place, the strand stress is increased

![Figure 22. Resultant moments for bridges with and without positive moment reinforcement at supports.](image)

![Figure 23. Simplified bridge models for BRIDGERM analysis.](image)
because of the imposed deck load. Restraint moments are calculated over a predetermined sequence of time increments starting at the age continuity is established. For each time step, the three components of change in restraint moments, differential shrinkage, dead load creep, and prestress creep, are calculated. The calculated increment of restraint moment is added to the sum from the preceding time step to determine the restraint moment at the end of an interval. The change in restraint moment within a time step is determined using a modification to the procedure in Ref. 12. The modified procedure incorporates a time-dependent creep effect factor to account for the age at loading for the change in moment within each time step. Details of this procedure are further discussed in Appendix E.

In order to determine the success of the simplified restraint moment calculation method, a comparison to results of the PBEAM analyses was made. Initial comparisons showed that the simplified method overestimated the effects of differential shrinkage, particularly for late restraint moments in a bridge with a late age of continuity. The formula suggested by Dischinger (69) to account for the restraining action of reinforcement was used to reduce the ultimate shrinkage strain of the deck when restraint moments were negative. Use of this modification factor is further discussed in Appendix E.

Tables 18 and 19 show comparisons of restraint moments calculated using PBEAM, the CTL method using program BRIDGERM, and the PCA method from Ref. 12. The tables compare restraint moments at the central support of a four-span bridge. Three girder sections are compared, each with two span lengths. Each analysis was done using a low value of 1.625 and a high value of 3.25 for the ultimate creep coefficient. Table 17 shows restraint moments calculated at 650 days for an early age of continuity of 17 days. The CTL moments show significantly better agreement than moments calculated using the PCA method. The mean absolute error of the PCA method compared to PBEAM results is 334 ft-kip. The mean absolute error of CTL method results is 77 ft-kip.

Table 19 shows the maximum negative restraint moments for bridges with a late age of continuity of 67 days. The improvement in predicting the maximum negative moment for late age of continuity using the CTL method is not as significant as for early age of continuity results shown in Table 17. For maximum negative moment, the mean absolute error for the CTL method is 184 ft-kip, compared to 185 ft-kip for the PCA method.

Three typical restraint moment time responses are shown in Figures 24, 25, and 26. Each figure shows restraint moments from PBEAM and CTL method calculations at the central support of a four-span bridge. Analyses were done for low and high ultimate creep coefficients of 1.625 and 3.25, respectively. Figure 24 is for BT72/6 girders with 130-ft spans and age of continuity of 17 days. PBEAM results for both low and high creep give positive restraint moments immediately after continuity is established. Because of the configuration of the girder cross section, dead load is relatively small and the composite centroid is close to the top of the girder. As a result, the two contributors to negative restraint moments, dead load creep and differential shrinkage, are relatively small compared to the positive restraint moment contribution of prestress creep. CTL method restraint moment for the high creep case is close to PBEAM results and converges at a later age. For low creep, the CTL method moment is slightly negative initially, but recovers and runs parallel, but approximately 270 ft-kip below the PBEAM moment at later ages. This represents the largest

### Table 18. Restraint moments at central support of four-span bridge—age of continuity 17 days.

<table>
<thead>
<tr>
<th>Ultimate Creep Coefficient</th>
<th>Girder Type</th>
<th>Span Length, ft</th>
<th>PBEAM Moment 0 650 days ft-k</th>
<th>CTL Method Moment 0 650 days ft-k</th>
<th>PCA Method Moment 0 650 days ft-k</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.25</td>
<td>AASHTO-IV</td>
<td>70 100</td>
<td>217 405</td>
<td>275 390</td>
<td>40 131</td>
</tr>
<tr>
<td></td>
<td>AASHTO-VI</td>
<td>100 130</td>
<td>313 678</td>
<td>340 771</td>
<td>-83 316</td>
</tr>
<tr>
<td></td>
<td>BT72/6</td>
<td>100 130</td>
<td>275 1017</td>
<td>297 975</td>
<td>54 736</td>
</tr>
<tr>
<td>1.625</td>
<td>AASHTO-IV</td>
<td>70 100</td>
<td></td>
<td>41 124</td>
<td>-105 -120</td>
</tr>
<tr>
<td></td>
<td>AASHTO-VI</td>
<td>100 130</td>
<td>9% 385</td>
<td>21 320</td>
<td>-352 -68</td>
</tr>
<tr>
<td></td>
<td>BT72/6</td>
<td>100 130</td>
<td>26 425</td>
<td>26 425</td>
<td>-201 -206</td>
</tr>
</tbody>
</table>

*PBEAM analyses of girders with positive moment reinforcement at the supports was not carried out for this set of parameters.

### Table 19. Restraint moments at central support of four-span bridge—age of continuity 67 days.

<table>
<thead>
<tr>
<th>Ultimate Creep Coefficient</th>
<th>Girder Type</th>
<th>Span Length, ft</th>
<th>Maximum Negative Moment 0 650 days ft-k</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>PBEAM</td>
</tr>
<tr>
<td>3.25</td>
<td>AASHTO-IV</td>
<td>70 100</td>
<td>-900 -668</td>
</tr>
<tr>
<td></td>
<td>AASHTO-VI</td>
<td>100 130</td>
<td>-1160 -916</td>
</tr>
<tr>
<td></td>
<td>BT72/6</td>
<td>100 130</td>
<td>-644 -785</td>
</tr>
<tr>
<td>1.625</td>
<td>AASHTO-IV</td>
<td>70 100</td>
<td>-900 -738</td>
</tr>
<tr>
<td></td>
<td>AASHTO-VI</td>
<td>100 130</td>
<td>-1130 -1009</td>
</tr>
<tr>
<td></td>
<td>BT72/6</td>
<td>100 130</td>
<td>-634 -585</td>
</tr>
</tbody>
</table>

### Figure 24. Comparison of CTL method and PBEAM results—BT72/6, early age of continuity.
difference for the comparisons made in Table 17. The difference of 270 ft-kip is approximately 6 percent of the resultant midspan moment for dead load, restraint moment, and live load plus impact.

Figure 25 represents a common situation for heavier girders with early age of continuity. In this case, the girders are AASHTO Type VI with spans of 100 ft. For heavier girders, dead load creep and differential shrinkage components dominate in early ages and produce negative restraint moments. Prestress levels in heavier girders are often high, particularly for longer spans, and therefore positive restraint moments eventually develop as the differential shrinkage contribution decreases. Again, for high creep, the CTL method prediction agrees fairly well with the PBEAM results. For low creep, the CTL method overestimates early age negative moment and then runs parallel but below the PBEAM results.

Figure 26 shows typical behavior of a girder with an age of continuity of 67 days. This bridge consists of 100-ft spans with AASHTO Type IV girders. For later age of continuity the differential shrinkage component dominates the early restraint moments because most of the girder shrinkage has occurred before the deck is in place. High negative restraint moments result. PBEAM analyses generally result in a large negative restraint moment, initially with a strong recovery due to prestress creep after 150 days. The CTL method results do not attain the extremes of the PBEAM analyses in that the high early negative restraint moment is generally underestimated and later age negative moments are overestimated.

In general, the CTL method as implemented in program BRIDGERM shows reasonable agreement with PBEAM results for each of the three situations described above. The method is an improvement in ease of use as well as accuracy of results over the PCA method from Ref. 12. The mean absolute error of 77 ft-kip for the CTL method results in Table 17 represents approximately 2 percent of the sum of positive midspan service restraint, dead load, and live load plus impact moments for the six girder/span length combinations studied.

Calculation of Live Load Plus Impact Moments. Program BRIDGELL was developed to calculate maximum live load plus impact moments for a continuous interior bridge girder loaded by AASHTO standard (14) HS truck and lane loads. An elastic continuous beam analysis program was modified by addition of routines to generate AASHTO HS truck and lane loads. For AASHTO HS truck loads, a single standard truck is placed at a number of positions on each span. The user specifies the number of truck positions per span and the number of axle spacings to be used between the 14 and 30 ft extremes. For each combination of truck position, direction, and axle spacing, the bridge is analyzed. Extreme shears and moments are updated after each analysis. The program is capable of analyzing the structure without positive moment continuity for AASHTO truck load cases. For AASHTO HS lane loading, the program generates combinations of patterned loading to produce maximum positive midspan moments and maximum positive and negative support moments. The AASHTO lane load specifies use of one concentrated load for positive moments and two concentrated loads for negative moments, placed to cause maximum stress. For each pattern of lane uniform loading, the user specifies the number and locations of different positions for the concentrated load(s). For each combination of uniform and point load(s), the bridge is analyzed. Extreme shears and moments are updated after each analysis. The load magnitudes are based on AASHTO HS20-44 specifications. Loads are adjusted to account for the number of lanes per girder and the lateral distribution of load according to AASHTO recommendations. The user may specify load magnitudes other than HS20-44 by entering a multiplication factor, such as 1.25 to analyze for HS25-44 loading.

SUMMARY OF FINDINGS

Chapter Two presented the findings of the research for this project. Based on a review of the literature, existing analytical techniques and computer programs PBEAM and WALL....HINGE were selected for evaluation of time-dependent behavior and strength of precast, prestressed girders made continuous. Creep and shrinkage tests were carried out to investigate behavior with early age loadings and to evaluate mathematical models. Coefficients for time-dependent behavior of
CHAPTER THREE

INTERPRETATION, APPRAISAL, AND APPLICATION

DESIGN FOR SERVICE MOMENTS

Current AASHTO provisions for the design of bridges constructed of prestressed girders made continuous do not specify how to consider the effects of creep and shrinkage. The following recommendations for the design for service moments are based on the findings of the analytical studies of the long-term behavior of this type of bridge presented in Chapter Two.

Positive Moment at Supports

Results of the parametric study of time-dependent restraint moments and service load moments at supports of bridges constructed of prestressed concrete girders made continuous indicate that there is no structural advantage for providing positive moment reinforcement at supports. With continuity established at an early girder age, positive restraint moments and the apparent degree of continuity with application of live load are highly dependent on the amount of positive reinforcement provided in the girder connections at the supports. The time-dependent positive restraint moment generally induces a crack in the bottom of the diaphragm concrete. With the application of live load, the positive moment crack must close prior to inducing negative moment at the continuity connection. The presence of positive moment reinforcement helps to maintain relatively small cracks, thereby increasing apparent live load continuity. However, the positive restraint moment resulting from the presence of the reinforcement in the support connection increases the positive midspan resultant moment. The effect of the lack of full continuity caused by not providing positive reinforcement in the diaphragm and allowing the bottom diaphragm crack to open is virtually balanced by the increased positive restraint moment. Therefore, the resultant midspan moments, which include moments due to dead load, restraint moments due to creep and shrinkage, and live load moments, are independent of the area of positive reinforcement provided in the diaphragm connections at the supports. Therefore, providing positive moment reinforcement has no benefit for flexural behavior of this type of bridge.

The primary advantage of positive moment reinforcement is in maintaining a smaller crack near the bottom of the diaphragm. However, questionnaires returned by four state departments of transportation (California, Florida, Minnesota, and Wisconsin) reported using continuous decks over the supports without any positive moment connection. There were no serviceability problems associated with the lack of positive moment connections. Because construction of this detail is expensive, time-consuming, and difficult, the provision of positive moment reinforcement at the supports is not recommended.

Positive Moment at Midspan

Positive service moments at midspan consist of simple span moments due to girder and deck weight and moments acting on the continuous structure, including those due to additional dead load, live load plus impact, and time-dependent restraint...
moments at supports. AASHTO Specifications require that allowable stresses of Article 9.15.2.2 (14) not be exceeded under the critical combination of service loads. Results of this study indicate that the time-dependent behavior influences the continuous behavior such that the effective continuity for live load plus impact can vary from 0 to 100 percent. Therefore, the time-dependent effects must be considered in design if continuity is to be counted on to reduce positive service moments at midspan.

To account for the effects of time-dependent restraint moments on midspan positive service moments, the first step is to determine restraint moments assuming full structural continuity. Calculated restraint moments, support moments for the service load case which causes maximum midspan moment, and support moments due to additional dead load are then added. The summation of support moments governs the amount of positive midspan moment reduction due to the effects of structural continuity.

Time-Dependent Restraint Moments. Restraint moments can be determined using the program BRIDGERM developed in this study. The analysis in BRIDGERM to determine restraint moments assumes full structural continuity. As discussed in Chapter Two and illustrated in Figure 22, this applies whether or not positive moment connections are provided at supports. Additional dead load applied shortly after establishment of continuity, such as for parapet or median strip loads, should be included in the restraint moment analysis.

For calculating support restraint moments for use in determining positive midspan service moments, the following time factors should be considered. The earliest likely girder age at which continuity would be established in the bridge based on expected construction schedule should be used. Results of the questionnaire indicated that girders are generally between 10 and 90 days old at the time of construction. An age of continuity of 17 days was used for early age analyses in the parametric study. Along with the early age of continuity, a late age at which live load is applied, 2 years or greater, should be used.

An additional consideration that could be used to calculate more conservative design moments is to include factors to account for the variability of creep and shrinkage behavior. As shown by the creep and shrinkage tests carried out in this study, the concrete time-dependent properties can vary significantly from the calculated values from analytical material behavior models. To determine the most conservative positive midspan service moments, the time-dependent analysis with BRIDGERM could be carried out with upper-bound values on girder concrete creep and shrinkage and a lower-bound value on the deck shrinkage. Considering that the time-dependent analyses are being carried out to determine service moments, and considering that no major serviceability problems have been reported related to midspan flexural behavior for this type of bridge, use of upper-bound and lower-bound time-dependent material properties would add unwarranted conservatism. It is our recommendation that, if the time-dependent material properties of the specific concrete to be used in the construction of the girders and deck are not known, values determined using ACI-209 (17) recommendations should be used for calculating time-dependent restraint moments.

Live Load Plus Impact. One of the main recommendations of this study is that positive moment reinforcement at supports not be provided because its disadvantages in construction outweigh structural and serviceability advantages. However, if positive moment reinforcement is not provided, no reliable positive moments can develop at supports. Therefore, for determination of live load plus impact moments on the continuous structure, the nature of continuity at supports must be considered for various load configurations. The following discussion presents the recommended procedure for determining design positive midspan live load plus impact service moments acting on the continuous structure with no positive moment reinforcement at supports.

Figure 27 illustrates possible load configurations. As shown in Figure 27(a) and (b) for AASHTO truck load located on one span of a multispan bridge, the continuous structure for resisting the load consists of three spans for a loaded interior span and two spans for a loaded end span. For a loaded interior span of a fully continuous bridge, negative moments occur at the two supports adjacent to the loaded span and positive moments occur at the next support in each direction. When positive moment resistance is not provided, these moments are assumed to be zero, in effect isolating the loaded span and the two adjacent spans from the rest of the bridge, as shown in Figure 27(a). Similarly, for a loaded end span of a fully continuous bridge, negative moment occurs at the first interior support and positive moment occurs at the second interior support. When positive moment resistance is not provided, the moment is assumed to be zero at the second interior support. Therefore, the effective continuous structure for an end span loaded with AASHTO truck load consists of the loaded span and the first adjacent span, as shown in Figure 27(b).

For load configurations such as additional dead load over the entire bridge and some patterns of AASHTO lane load, no
positive support moments occur. Because no positive support moments occur, the absence of positive moment reinforcement at supports does not affect continuity. Therefore, the entire bridge can be assumed to act as a continuous structure, as shown in Figures 27(c) and 27(d). Calculations of additional dead load and live load plus impact moments can be done using the program BRIDGE developed in this study. BRIDGE includes, as an option, analysis of the partially continuous bridge as described above. A more complete description of Program BRIDGE can be found in Appendix E.

**Midspan Service Moments.** The magnitudes of continuity moments at supports of a typical span are used to determine the midspan service moment for checking allowable stresses. Continuity moment is defined as the sum of restraint, additional dead load, and live load plus impact moments at a support. Calculated restraint moments from BRIDGERM for supports of each typical span of the bridge should be added to the sum of negative support moments from two load cases. The first is the live load plus impact load case, which produces maximum positive midspan moment in the corresponding span. The second load case is additional dead load over the entire continuous structure.

If the average of the continuity moments for the two supports is positive, time-dependent effects have reduced effective structural continuity for live load plus impact to 0 percent. In this case, the positive midspan moment should be determined as the sum of simple span moments for additional dead load and live load plus impact.

If the average of the continuity moments for the two supports is negative and does not exceed 125 percent of the negative cracking moment, partial or full structural continuity exists. In this case, the positive midspan moment should be determined by adding (correctly accounting for signs) the average calculated restraint moment from BRIDGERM to the calculated additional dead load, and live load plus impact midspan moment from BRIDGE for the fully continuous structure.

The recommended maximum negative continuity moment to be used for reduction of midspan positive moment is equal to 125 percent of the negative cracking moment of the section. If the average of the continuity moments for the two supports is greater than 125 percent of the cracking moment, the midspan moment should be taken as the resultant positive midspan moment from the continuous analysis (including restraint, additional dead load, and live load plus impact) plus the amount by which the negative continuity moment exceeds 125 percent of the cracking moment. This provides for the situation when negative moments are redistributed to midspan after deck cracking occurs. The summation of moments for a typical symmetrical span is illustrated in Figure 28. It should be noted that the

![Moment Diagrams](image_url)

**Figure 28. Determination of service load design moment.**
summation of moments illustrated in Figure 28 does not include simple span moments due to girder and deck dead weight.

If no analysis is conducted to determine time-dependent restraint moments and no positive moment reinforcement is provided at supports, the midspan service moment should be taken as the sum of simple span additional dead load and live load plus impact moments.

Stresses at service load, for comparison to allowable stresses in AASHTO (14) Section 9.15.2.2, should be determined in the following manner. Stresses from the simple span moment due to girder plus deck weight and stresses due to prestress force should be calculated using section properties for the girder only. Stresses from the previously described moment due to the combination of time-dependent effects, additional dead load, and live load plus impact should be calculated using section properties for the composite girder and deck section.

Negative Moment at Supports

Negative service moments at supports consists only of moments acting on the continuous structure, including those due to additional dead load, live load plus impact, and time-dependent effects. At service load, Article 9.7.2.4 of AASHTO Specifications (14) requires that compressive stress at girder ends not exceed 0.6 f’c. The section specifies consideration of “effects of prestressing and negative live load bending,” but effects of possible negative restraint moments should also be included. Because the negative moment region acts essentially as a conventional reinforced concrete section, limitations on reinforcement stresses given in Chapter 8 of AASHTO Specifications should also be met. Article 8.15.2.2 limits maximum tensile stress. This provision as well as provisions of Article 8.16.8.4 governing distribution of reinforcement should be used to minimize deck cracking. Article 8.16.8.3 limits stress range to prevent fatigue failure of reinforcement in the deck.

Time-Dependent Restraint Moments. Time-dependent support restraint moments can be determined using the program BRIDGERM developed in this study. For calculating restraint moments for use in determining negative service moments at supports, the following time factors should be considered. The latest likely girder age at which continuity would be established in the bridge, based on the expected construction schedule, should be used. Results of the questionnaire indicated that girders are generally less than 90 days old at the time of construction. However, the girders can be significantly older because of construction delays, particularly for girders intended for construction in late fall that end up being stored through the winter and erected in the spring. In combination with the late age of continuity, application of live load should be assumed to occur at an early age after establishment of continuity for determination of maximum reinforcement and concrete stresses. Results of the time-dependent analysis with BRIDGERM indicate that maximum negative moment and maximum potential for cracking in the deck occurs approximately 50 days after casting the deck and diaphragm. Therefore, use of restraint moments calculated at approximately 50 days after establishment of continuity is recommended for checking maximum tensile stress in the deck reinforcement and maximum compressive stress in the girder end.

For checking fatigue limits, the maximum negative moment at early age is essentially a transient condition. Although restraint moments can remain negative for the life of the structure, they reach a reduced and relatively constant level after approximately 2 years. Therefore, use of restraint moments calculated at a minimum of 700 days after continuity is established is recommended for checking fatigue limits.

Restraint moments at approximately 50 days and 700 days can be determined from the same run of BRIDGERM with a late age of continuity. The user may request output of restraint moments at all time steps for selection of the maximum negative restraint moment.

Live Load Plus Impact and Additional Dead Load Moments. Negative support moments from live load plus impact and additional dead load can be determined using the program BRIDGELL developed in this study. In general, maximum negative live load plus impact moments occur for patterns of AASHTO lane loading in which no positive moments occur at supports. Because no positive support moments occur, the absence of positive moment reinforcement at the supports does not affect continuity. As described previously and illustrated in Figures 27(c) and 27(d), the BRIDGELL analysis for these cases is conducted for the fully continuous structure. In some situations, maximum negative live load plus impact moments may occur for AASHTO truck loading. In this case, if no positive moment reinforcement is provided at the supports, maximum moments should be determined using the limited span continuity analysis in BRIDGELL, as illustrated in Figures 27(a) and 27(b).

No positive support moments occur with application of additional dead load over the entire length of the continuous structure. Therefore, negative support moments for additional dead load can be determined using the fully continuous analysis of BRIDGELL, as indicated by Figure 27(c).

Service Moments at Supports. The service moment to use for checking allowable stress levels at supports should consist of the sum of peak negative restraint moment, additional dead load moment, and maximum live load plus impact moment. If, under the assumed conditions, calculated restraint moments are positive, the sum of additional dead load moment and maximum live load plus impact moments should be used. Negative service moment stresses in steel and concrete should be calculated using cracked, transformed section properties. Concrete compressive stress should include stress due to prestress force at the girder end acting on the girder section only.

For checking allowable stress range for fatigue of deck reinforcement, minimum stress occurs due to the sum of restraint moment and additional dead load moment. As discussed previously, use of restraint moment calculated at a minimum of 700 days after continuity is established is recommended for checking fatigue limits. The maximum stress occurs with application of live load plus impact. Composite cracked, transformed section properties should be used for checking both minimum and maximum steel stresses.

STRENGTH DESIGN

Stresses and strains induced in the girders by volume change from creep and shrinkage are self-limited within the girder in that they are relieved by the deformations accompanying cracking in the concrete and yielding of reinforcement. As a result, presence or absence of time-dependent restraint moments has no effect on the strength of the structure. This was demonstrated by comparing tests to destruction of girders tested at approxi-
mately 2 years of age with a girder tested at 12 days after deck casting in Ref. 10. Therefore, the design of the bridge to meet strength provisions of the AASHTO Code shall not include time-dependent moments.

CONCLUSIONS

Findings and design procedures developed in this study have been incorporated into recommended revisions for Article 9.7.2 of the AASHTO "Standard Specifications for Highway Bridges" (14). A draft of the proposed revised Article 9.7.2 and a draft of the accompanying Commentary are presented in Appendix G.

PROPOSED AASHTO SPECIFICATIONS

CONSTRUCTION SEQUENCE

Continuity performance is highly dependent on the age of the girder when the diaphragm and deck are cast. High negative restraint moments can occur at the support connections when continuity is established at late girder ages. Full continuity for live load can be established, depending on the age of the girder at time of casting the deck and diaphragm and on the creep coefficient for the girder concrete.

The sequence of deck and diaphragm construction affects the development of restraint moments. Casting of the deck prior to the diaphragm increases resultant positive moments at midspan, but decreases the potential for deck cracking. Casting of the diaphragm before the deck only slightly decreases resultant midspan positive moments, and increases the potential for deck cracking. There is no major economic or structural advantage to sequencing the casting of the deck and diaphragm. Simultaneous casting is the simplest construction procedure.

The degree of continuity available in simple-span prestressed girders made "continuous" for live load plus impact by connections at the pier diaphragms can vary from zero continuity to full continuity. The degree of continuity is dependent primarily on the age of the girder at the time of casting the deck and diaphragm, and on the creep and shrinkage properties of the concrete. Full continuity can be established by delaying casting of the deck and diaphragm. However, delayed casting increases construction time and also increases negative moments required for design of reinforcement in the deck over the supports. The simplified analysis procedure developed in this project enables designers to account for the various parameters involved to find a good balance between construction timing and design moments.

CONCLUSIONS AND SUGGESTED RESEARCH

CONCLUSIONS

Based on the results of analyses presented in this report, the following conclusions were reached:

1. Practical advantages of bridges constructed of precast, prestressed concrete girders made continuous have made design and construction of bridges of this type commonplace. However, construction of the positive moment connection at supports is difficult, time consuming, and costly.
2. Current practice for analysis, design, and construction of this type of bridge varies widely within the United States. Current AASHTO Specifications (14) are vague. Most states use the PCA design procedure (12) as the basis for their design of continuity connections. However, that procedure has several uncertainties and does not address some important considerations. The PCA procedure does not adequately handle some situations which exist in current practice of construction timing and sequence.

3. Creep and shrinkage properties of steam-cured concrete were not readily available. Tests conducted in this project have added significantly to that data base. Test results indicate that ACI-209 (17) creep and shrinkage prediction procedures give reasonably accurate predictions.

4. Computer analyses of time-dependent and live load plus impact service moments and negative moment strengths were conducted using two sophisticated computer programs, PBEAM (53) and WALL-HINGE (57). Analytical results compared well to existing experimental results and, therefore, the programs were used to conduct parametric studies of bridge behavior.

5. The service moment parametric study results indicated that there is no structural advantage for providing positive moment reinforcement at the supports. With continuity established at an early girder age, positive restraint moments develop, dependent on the amount of positive reinforcement provided in the diaphragm connections at the supports. Time-dependent positive restraint moment generally induces a crack in the bottom of the diaphragm concrete. With application of live load, the positive moment crack must close prior to inducing negative moment at the continuity connection. The presence of positive moment reinforcement helps to maintain relatively small cracks, thereby increasing the apparent live load continuity. However, the positive restraint moment resulting from the presence of the reinforcement in the support connection increases the positive midspan resultant moment. The effect of the lack of apparent full continuity, caused by not providing positive reinforcement in the diaphragm and allowing the bottom diaphragm crack to open, is virtually balanced by the increased positive restraint moment that develops when positive reinforcement is provided. When negative restraint moments develop, positive moment reinforcement is in the compression zone and offers no structural advantage. Therefore, the resultant midspan moments, which include moments due to dead load, restraint moments due to creep and shrinkage, and live load plus impact moments, are virtually independent of the area of positive reinforcement provided in the diaphragm connections at the supports.

6. Continuity performance is highly dependent on the age of the girder when the diaphragm and deck are cast. There is a structural advantage gained for design of the prestressed girders for positive midspan moment by delaying casting of the deck and diaphragms. High negative restraint moments can occur at the support connections when continuity is established at late girder ages. Full continuity for live load can be established depending on the age of girder at time of casting the deck and diaphragm and on the creep coefficient for the girder concrete. However, delaying casting of deck and diaphragm may require a delay in bridge construction. Also, the design moment for negative reinforcement in the deck over the supports is increased and the potential for transverse cracking in the deck is increased by delaying construction.

7. Sequence of deck and pier diaphragm construction affects the development of restraint moments. Casting of the deck prior to diaphragms increases resultant positive moments at midspan. Casting of diaphragms before the deck only slightly decreases resultant midspan positive moments. There is no major economic or structural advantage to sequencing the casting of the deck and pier diaphragms. Simultaneous casting is the simplest construction procedure.

8. The parametric study of negative moment strength of composite sections indicated that typical sections have adequate rotational ductility to allow formation of a failure mechanism. An upper limit on deck reinforcement equal to 50 percent of \( \rho_b \) ensures that sections have sufficient ductility to develop the full failure mechanism as well as provide enough deformation to give adequate warning of failure.

9. Analysis and design procedures were developed to improve the currently used PCA method (12). The improved analysis procedure eliminates some uncertainties of the PCA method and can deal with more practical situations. The improved simplified analytical procedures were incorporated into two computer programs. The improved and more comprehensive design procedures are described. Proposed revisions to the AASHTO Specifications are outlined to include the improved analysis and design procedures.

10. The improved analysis and design procedures developed in this study will allow for more rational design and simplify construction of this type of bridge.

**SUGGESTED RESEARCH**

The difficulty and expense of constructing the positive moment connections at the supports was one of the primary problems associated with simple-span precast prestressed bridge girders made continuous. This problem is addressed in this study and a specific recommendation made to eliminate the problem by eliminating the connection. Another typical problem determined from the questionnaire is transverse cracking of the deck in negative moment areas. This problem is addressed in this study by demonstrating the combination of timing of construction and live load application that results in high negative moments. Also, tools are provided for the designer, in the form of computer programs BRIDGERM and BRIDGEILL, to quantify the expected negative moments and potential for deck cracking. However, another approach is to provide special details to accommodate the potential for cracking with preformed joints over the support and unbonding of the deck reinforcement or unbonding of the deck to girder interface for a certain length on each side of the joint. The effectiveness of these types of details and their effects on continuous behavior should be evaluated through further research.

Another area for further research is related to design and detailing of methods to increase the effective continuity. Currently, with the usual methods of construction for this type of bridge, the most efficient condition that can be attained is full continuity for additional dead load and live load plus impact. The girders must still be designed for the dead weight of the girder and deck as a simply supported member. However, a hybrid girder with partial post-tensioning in place may be feasibly designed to include more of the dead load into the continuous behavior (J). Also, there may be potential benefits of moment connections to the piers for increased continuity and efficiency in both the girder and pier design (J).

Other areas for further research concern the effects of temperature and moisture gradients within the deck-girder section
and the effects of support settlement on the continuous behavior and design moments. Evaluation of these effects was beyond the scope of the current study. However, they should be considered in the design process.

The work carried out in this study is primarily related to design for flexural behavior. However, there is also a need to improve or at least clarify procedures for design of shear reinforcement for continuous girders. The current approach for designing for shear in reinforced and prestressed concrete members is to consider a portion of the shear to be carried by the concrete, \( V_c \). The remaining shear strength is considered carried by shear reinforcement, \( V_s \). The 1983 edition of AASHTO Standard Specifications for Highway Bridges contains revised shear design provisions that include use of the smaller of \( V_{cw} \) or \( V_{ci} \) as \( V_c \). The \( V_{cw} \) strength relates to diagonal cracking strength of the web from combined shear and prestressing. The \( V_{ci} \) strength is related to the potential for diagonal cracking from combined shear and bending. The relationship for \( V_{ci} \) was taken from the ACI 318 Building Code. The relationship was developed based on tests of simply-supported girders with no consideration for continuous girders and moving loads. It includes a term \( V_i / M_{\text{max}} \) where \( M_{\text{max}} \) is the maximum factored moment at a section, and \( V_i \) is the factored shear at the section occurring simultaneously with \( M_{\text{max}} \). With different concentrated loads for lane loading specified for evaluating moment and shear along with the various combinations of load and placement of load for maximum moment or shear, the determination of \( V_{ci} \) is a nebulous and tedious task. There is a need to develop more appropriate and simplified design procedures for shear in continuous prestressed bridge girders.

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**REFERENCES**


51. USNRC, "NONSAP-C: A Nonlinear Stress Analysis Program for Concrete Containments Under Static, Dynamic..."
APPENDIXES A, B, C, D—UNPUBLISHED MATERIAL

Appendices A, B, C, and D contained in the report as submitted by the research agency are not published herein. Their titles are listed here for the convenience of those interested in the subject area. Qualified researchers may obtain loan copies, or microfiche may be purchased by written request to the NCHRP, Transportation Research Board Publications Office, 2101 Constitution Avenue, N.W., Washington, D.C., 20418.

The titles are:
Appendix A—Summary of Responses to Questionnaire
Appendix B—Results of Creep and Shrinkage Study
Appendix C—Methods of Analysis
Appendix D—Results of Parametric Study
APPENDIX E

PROGRAM DOCUMENTATION AND USER'S INSTRUCTIONS

PROGRAM BRIDGERM

Introduction
The purpose of Program BRIDGERM is to calculate restraint moments at supports of typical spans in continuous bridges constructed of precast, prestressed concrete girders and cast-in-place concrete deck. The program's restraint moment calculation method is based on the PCA method of Ref. (12) with the following modifications. The program carries out an incremental time-step solution with the capability to output the complete time-history of the restraint moments rather than just one restraint moment at a particular age. The time-dependent material properties for concrete are determined using ACI-209 Recommendations (17) including separate shrinkage functions for the deck and girder concrete, and time-dependent functions for the strength and stiffness of deck concrete. Prestress losses are determined at each time-step. The restraining effects of reinforcement on deck shrinkage are considered. The analysis is carried out on a simplified model that considers the finite length of the support regions. Details of data input and output, analysis assumptions, capabilities, and limitations of Program BRIDGERM are discussed below in the solution steps. The program was initially written in Data General Fortran 77 and implemented on CTL’s Data General MV10000 Computer. The program was then recompiled using Microsoft Fortran for use on IBM PC compatibles with MS-DOS 3.XX. A listing of the PC version of Program BRIDGERM is included starting on page E-23. An Example Problem is also given.

Solution Steps
Program BRIDGERM is divided into seven solution steps as follows:
1. Input data from girder, strand, material properties, and timing.
2. Determine time steps for incremental analysis.
3. Calculate geometric properties of noncomposite and composite cross sections.
4. Compute prestress losses up to transfer of prestress.
5. Compute prestress losses up to age at which continuity is established.
6. Calculate restraint moments.
7. Output results.

Following are detailed descriptions of each solution step.

Step 1 - Data Input
The program input is designed to be accomplished either interactively through keyboard input or through an input file. Each problem requires nine lines of input data. All data must be input. The program will not assign default values if zeros are entered. Data are input on unformatted lines. Input values must be separated by commas or blank spaces. Input values must correspond to the variable type, either Integer or Real. Real values may be input with or without a decimal point, whereas Integer values must be input without a decimal point.

Line 1 is for identification of the run. A description of up to 20 characters within single quotation marks should be entered on this line.

Lines 2 and 3 contain information to define the girder cross-section. Figure E-1 defines required dimensions for I, T, and box-girder sections. Line 2 reads horizontal dimensions B1, B2, B3, and B4. Line 3 reads vertical dimensions D1, D2, D3, D4, D5, and D6. All dimensions are in inches. Box sections may be analyzed by entering zero for B4, B3, and B2. Actual top and bottom flange dimensions should be entered and the sum of the two web thicknesses should be entered for B3 to define the box cross section. The effect on section properties of neglecting keyways and internal fillets is assumed to be negligible. All values on Lines 2 and 3 are Real variable types.

* This and any other numbered references are keyed to “References” listed following Chapter Four in the main body of the report.
Fig. E-1 Dimensions to Define Girder Cross-Section
Line 4 reads parameters NSP, SL, XLD, XDR, GS, TO, and WDL. NSP is an integer which defines the number of spans in the bridge. This controls the type of analysis done for typical spans in the bridge. SL is the span length, in feet, of each span in the bridge. The analysis is based on the assumption that all spans in the bridge are of equal length. XLD is the length, in feet, between double supports of the simplified analysis model taken as the distance between centerline of support bearings of adjacent girders over a common pier. XDR is ratio of the distance between the end of the girder and the hold-down point for the draped strands to the overall span length, as shown in Fig. E-2. If there are no draped strands in the girder, XDR should be entered as zero. GS is the center to center spacing of girders, in feet. TO is the deck thickness, in inches. WDL is the additional dead load due to parapet, wearing surface, etc., in psf. All values in Line 4, except NSP, are Real variable types.

Lines 5 and 6 read parameters which define the timing and output of the analysis. All time values are in days. The variables which control time considerations are AGRL, AGCT, and AGOK. AGRL defines the strand age after tensioning at which prestress force is transferred to the girder. This is used to calculate the initial prestress relaxation loss. AGCT defines the girder age at which continuity is established. This age is relative to the time at prestress transfer. AGOK defines the girder age at which the deck is in place relative to the time at prestress transfer. In most cases AGCT and AGOK can be assumed to be the same if the diaphragm and deck are cast within a few days of each other. These three variables are Real-valued and have units of days. NTIME and the vector UTIME are used to control program output. NTIME is an Integer value which is used to define the number of times at which calculated restraint moments are output. UTIME is a vector of dimension NTIME which contains the user-specified times at which restraint moments will be output. Time values in UTIME are added to the program's internal sequence of time steps. Times entered in UTIME must be sequential unless one of the options described in the following paragraph is

Fig. E-2 Dimensions to Define Prestressing Strand Location

XDR = L1/SL
Two additional options are available in the use of NTIME and UTIME. First, if the user wishes to output all calculated restraint moments up to a particular time, "1" should be input for NTIME. A single value should be input for UTIME equal to the negative of the last day restraint moments are to be output. For example, if the user wishes all calculated restraint moments to be output until age 650 days, "1" will be input for NTIME, and "-650." will be input for UTIME on Line 6. The second option allows the user to request output of maximum negative restraint moments calculated during the analysis. In this case, the user enters "-1" as one of the values input on Line 6 for the vector UTIME. The program will find the time at which maximum negative restraint moments, or minimum positive restraint moments, occur and output these values along with restraint moments calculated at other times requested in vector UTIME.

Line 7 reads values for the parameters SSC, DSC, WSC, NSL, NSS, NDS, ASTD, and FST. Parameters SSC, DSC, and WSC define locations of prestressing strand and are defined in Fig. E-2. SSC is the centroid of straight strands, measured in inches from the bottom of the girder. DSC is the centroid of draped strands at the end of the girder, measured in inches from the bottom of the girder. WSC is the centroid of draped strands between the hold-down points, measured in inches from the bottom of the girder. NSL is an Integer of value equal to either 1 or 2. If NSL is equal to 1, the strand is defined to be stress-relieved. If NSL is equal to 2, the strand is defined to be low-relaxation. The value of NSL determines coefficients defined in Ref. (41) used for calculating prestress losses. NSS is an Integer which defines the number of strands which are straight throughout the length of the girder. NDS is an Integer which defines the number of draped strands. If there are no draped strands, DSC, WSC, and NDS should be entered as zero. ASTD defines the cross-sectional area of a single strand in square inches. FST is the initial tensioning stress in each strand in psi. SSC, DSC, WSC, ASTD, and FST are Real-valued.

Line 8 reads values for the parameters FCI, FCG, FCD, WCG, and WCD. FCI is girder concrete compressive strength at transfer of prestress force, in psi. FCG is girder concrete compressive strength at 28 days, in psi. This value is used throughout the analysis. FCD is the 28-day compressive strength of deck concrete, in psi. Deck concrete strength varies with time according to the relationship given in Ref. (11) for moist-cured concrete with Type I cement. The time function for deck concrete strength is based on zero equal to the value specified for AGDK. WCG and WCD are concrete unit weights in pounds per cubic foot for girder and deck, respectively. All values in Line 8 are Real-valued.

Line 9 reads values of the parameters VULT, ESHUG, and ESHUD. VULT is the ultimate creep coefficient for girder concrete. If possible, the ultimate creep coefficient should be determined from actual creep tests on the concrete used in the girders. If actual data is not available, values should be determined using ACI-209 recommendations (17) using applicable correction factors. The time function for creep coefficient is that recommended by ACI-209. ESHUG and ESHUD are ultimate shrinkage strains for girder concrete and deck concrete, respectively. Values of ESHUG and ESHUD should be entered in units of millionths. For example, an ultimate shrinkage strain of 0.000600 in./in. should be entered as "600.". Values for ESHUG and ESHUD should, if possible, be taken from actual tests. Otherwise, ultimate shrinkage strains should be determined from ACI-209 recommendations (17) using applicable correction factors. Time functions for girder and deck shrinkage strains are those recommended by ACI-209 for steam-cured and moist-cured concrete, respectively. Zero time for girder creep coefficient and shrinkage strain is equal to the time of prestress transfer. Zero time for deck shrinkage strain is equal to the age specified by AGDK. No adjustments to ultimate values are made within the program. Therefore, any applicable correction factors, such as those recommended by ACI-209 (17), should be applied by the user outside the program to determine values entered for VULT, ESHUG, and ESHUD.
Step 2 - Determine Time Steps

Time steps used in the restraint moment analysis procedure are established internally using input values for AGCT and UTIME and a predetermined sequence of times in the vector BLIN. Times in BLIN were chosen with successively increasing time increments. Two time vectors are constructed. The first, TIR, is used in the prestress loss calculation from transfer of prestress to establishment of continuity at AGCT. The vector TIR consists of times from BLIN with the final value equal to AGCT. The vector TI is used in the calculation of restraint moments from AGCT onwards. Vector TI is constructed by adding AGCT to values in BLIN and merging in user-specified times from UTIME. The last time entered in UTIME will be the last time in the restraint moment analysis vector TI.

Step 3 - Calculate Section Properties

Geometric properties determined for the girder (noncomposite) and girder/slab (composite) sections are:
1. Cross-sectional area.
2. Location of center of gravity.
3. Moment of Inertia.
4. Volume to surface ratio (girder only).

For an I- or T-girder composite section, the effective top flange width is the smallest of:
1. Girder span divided by four.
2. Girder spacing.
3. Twelve times deck thickness plus web width.

For box girders, the effective flange width is the girder spacing.

In calculations of composite section properties, a transformed deck-girder section is considered. Transformed area of strand and reinforcement are neglected.

The girder volume to surface ratio is used in the prestress loss calculation.

Simple-span dead load moments are calculated for noncomposite and composite sections and include additional dead load for parapet, wearing surface, etc. For dead load moment, the deck cross-sectional area is equal to the girder spacing times the deck thickness.

Step 4 - Compute Prestress Losses up to Transfer

Prestress losses due to steel relaxation before transfer and elastic shortening of the girder at transfer are calculated. Relaxation loss is calculated using equations from Ref. (41). Appropriate coefficients for stress-relieved or low-relaxation strand are used depending on the value of NSL input by the user. The time between tensioning of the strand and transfer of prestress to the girder is given by AGRL. The prestress loss due to elastic shortening of the girder at transfer is calculated with the prestress force reduced by the relaxation loss. The girder concrete modulus of elasticity at transfer is computed from compressive strength FCI using the AASHTO Specifications (14) equation. Throughout program BRIDGERM, prestress losses and resulting strand stresses are calculated for conditions at midspan of girders.

Step 5 - Compute Prestress Losses up to Age of Continuity

Prestress losses are calculated for the period of time between transfer of prestress and establishment of continuity using a procedure based on that in Ref. (41). For each time step in vector TIR, prestress losses due to concrete creep and shrinkage and steel relaxation are calculated. For losses due to concrete creep and shrinkage, slight modifications have been made to the PCI procedure. In Ref. (41), the ultimate creep loss term, UCR, is defined in terms of steel stress per unit concrete stress. This is derived from specific creep, with units of creep strain per psi of concrete stress, multiplied by steel modulus of elasticity in psi. The parameter UCR used in the program consists of ultimate creep coefficient multiplied by the modular ratio between steel and concrete. The term PCR which expresses the amount of creep over each time step is calculated from the ACI-209 recommended time curve for creep coefficient rather than from the tabulated values in Ref. (41). The shape effect factor, SCF,
Concrete stress at the level of the strand centroid is calculated using the prestressing force from the preceding time step.

The ultimate loss due to concrete shrinkage, USH, is derived from ultimate shrinkage strain multiplied by steel modulus of elasticity in Ref. (41). In the program, USH is equal to ESHUG, with units of millionths, multiplied by 29.0, which is steel modulus of elasticity in million psi, which results in units of psi. The amount of shrinkage over each step, PSH, is calculated from the ACI-209 recommended time curve for shrinkage of steam-cured concrete rather than from the tabulated values in Ref. (41). The shape effect factor, SSF, is the same as in Ref. (41).

The loss of prestress due to relaxation of steel is calculated in the same manner as in Ref. (41). For each time step, losses are calculated with the strand stress equal to the value from the end of the preceding time interval.

When the deck is added at time AGDK, the steel stress is increased due to the additional dead load stress from the deck weight. The steel stress is increased by an amount equal to the additional concrete stress at the level of the strand centroid, multiplied by the modular ratio. It is assumed that the noncomposite section remains active until AGCT.

Step 6 - Calculate Restraint Moments

Restraint moments are calculated using the simplified analysis model shown in Fig. E-3 for three typical spans as shown in Fig. E-4. Exterior span restraint moments at the first support are calculated in variable RME. For the first interior span, restraint moments are calculated at the supports in variables RMIL and RMIR. The moments in RMIL are at the support adjacent to the exterior span. RME, RMIL, and RMIR are adjusted, if necessary, to account for the effect of the adjacent span when uplift conditions occur. Restraint moment RMII is calculated for the supports of an interior span which is adjacent to two interior spans. Restraint moment RME is applicable to bridges of

Fig. E-3 Simplified Analysis Model
two spans or more. Restraint moments RMIL and RMIR are applicable to bridges of three spans or more. Restraint moment RMII is applicable to bridges of five spans or more. Until uplift conditions occur, RMII, RMIL, and RMIR are equal and RME is approximately 1.5 times as large. Uplift conditions are assumed to occur when one of the two reactions at the first interior support region becomes negative. This occurs when one of the reactions induced by the change in restraint moment in the support region is negative and greater in magnitude than the dead load reaction.

Preliminary steps include the following. If AGDK is less than or equal to AGCT, moment of inertia, cross-sectional area, and strand eccentricity are set to composite section values. If AGDK is greater than AGCT, the analysis proceeds using noncomposite section properties. It is assumed that with the diaphragm cast before the deck, the support area is continuous for positive moments. Since differential shrinkage is not active, only positive restraint moments of relatively small magnitude will result from prestress and dead load creep acting on the girder section. When the deck is added at AGDK, the composite section properties are used, dead load moment is increased, and strand stress is increased due to the additional dead load stress. At time AGCT, the value of each of the four restraint moment variables is set to zero. The strand stress for exterior and interior spans is set to the value from the computation of strand stress up to age of continuity. Constants used throughout the analysis are calculated.

Using the PCA method in Ref. (12), restraint moments due to creep under prestress, $M_0^p$, and dead load, $M_0^d$, and due to differential shrinkage between deck slab and girder, $M_o^s$, are first calculated for a continuous girder assuming rigid connections between individual spans at the piers. The creep restraint moments are determined by multiplying the dead load and prestress moments by a coefficient $(1-e^{-\theta t})$ where:

$$\theta_t = \nu_t - \nu_{t_0}$$  \hspace{1cm} \text{[E1]}
\[ v_{T_0} = \text{Creep coefficient at time } T \text{ days, where } T \text{ is the time after prestress release at which restraint moments are being calculated, } T > T_0 \]

\[ v_{T_0} = \text{Creep coefficient at time } T_0 \text{ days, where } T_0 \text{ is the time after prestress release at which continuity is established} \]

Restraint moments due to differential shrinkage are determined using a multiplier of \((1-e^{-\Phi T})/\Phi T\).

A series of analyses were made to calculate the time history of the restraint moment for a number of bridge cross-sections, spans, and creep coefficients. This was first attempted by calculating the restraint moment at a series of discrete times, \(T\), using \(\Phi T\) as follows:

\[ M_T = (M_D + M_{PT})(1-e^{-\Phi T}) + M_{ST}(1-e^{-\Phi T})/\Phi T \quad [E2] \]

The prestress restraint moment, \(M_{PT}\), is recalculated at each discrete time \(T\) to account for prestress loss in the girder from relaxation and concrete creep and shrinkage. The relaxation loss time factor is determined using the equation from Ref. (41). The shrinkage loss is determined using the ACI-209 time curve for shrinkage of steam-cured concrete. The restraint moment from differential shrinkage between the deck slab and girder is also recalculated at each time \(T\). The shrinkage restraint moment is determined from the difference in shrinkage occurring from time \(T_0\) to time \(T\) using the ACI-209 curves for steam-cured and moist-cured concrete for the girder and deck slab, respectively. Also, the \(\Phi T\) was determined using the ACI-209 recommended curve rather than the data in Ref. (12). This approach did not result in a significant improvement in calculated restraint moments as compared to results calculated strictly following the PCA method.

As an alternate, the series of analyses were repeated using an incremental approach. Using this approach, rather than recalculate \(M_1\) at each time \(T\) with respect to \(T_0\), the change in the restraint moment \(\Delta M_I\) within each time step is calculated as follows:

\[ \Delta M_I = (M'_0 + M_{PT}'(1-e^{-\Phi I}) + M_{ST}'(1-e^{-\Phi I})/\Phi I) \quad [E3] \]

where:

\[ \Phi I = v_{T_{I-1}} - v_{T_{I-1}} \quad [E4] \]

\[ v_{T_{I-1}} = \text{Creep coefficient at time } T_{I-1} \text{ after prestress release for the } I\text{-th time step} \]

The incremental differential shrinkage moment, \(\Delta M_{ST}'\), is the change in calculated restraint moment resulting from the difference in deck shrinkage strain and girder shrinkage strain, \(\Delta \epsilon_{ST}\), occurring over the time increment, \(\Delta T = T_I - T_{I-1}\) as follows:

\[ \Delta M_{ST}' = \Delta F_d(e_c + \frac{t}{2}) \quad [E5] \]

where:

\[ \Delta F_d = \text{Tension in the deck to establish compatibility with the girder} \]

\[ E_d = \frac{\Delta \epsilon_{ST} E_d A_d}{1 + E_d A_d E_g A_g} \quad [E6] \]

\[ \Delta \epsilon_{ST} = (\epsilon_{sd1} - \epsilon_{sd1-1}) - (\epsilon_{sg1} - \epsilon_{sg1-1}) \]

\[ \epsilon_{sd1} = \text{Shrinkage strain in deck at time } T_I \]

\[ \epsilon_{sg1} = \text{Shrinkage strain in girder at time } T_I \]

\[ E_d = \text{Modulus of elasticity of deck concrete at time } T_I \]

\[ E_g = \text{Modulus of elasticity of girder concrete (constant)} \]

\[ A_d = \text{Cross-sectional area of deck slab} \]

\[ A_g = \text{Cross-sectional area of girder} \]

\[ (e_c + \frac{t}{2}) = \text{Distance between middepth of deck slab and centroid of the composite section} \]

In determining the deck shrinkage strain, after an age of 30 days, the ultimate shrinkage strain is reduced by the Dischinger effect factor (69) to account for the restraint from the reinforcing steel.
within the deck. The creep coefficient $v_{fi}^{i}$ is determined from the ACI-209 recommendations for the girder concrete modified by the ACI-209 recommended correction factor for age of loading for each time $T_{avg}$ as follows:

$$v_{fi}^{i} = \frac{v_{fi}^{i} (1.13 T_{avg}^{0.094})}{T_{avg}}$$  \[E7\]

$$T_{avg} = \frac{T_{i} + T_{i+1}}{2}$$  \[E8\]

Restraint moment increment $\Delta M_{i}$ is used in an elastic analysis for the simplified model. If induced reactions at the support region between an exterior and interior span do not cause uplift, the elastic analysis is done for the unmodified simplified model. If induced reactions cause uplift, the model is modified by including the full length of the adjacent span rather than the distance between supports. Restraint moment increments are then calculated by distributing the moments from the two spans using the modified model. RME, RMIL, and RMIR are affected by the uplift analysis. Moment RMII is calculated for interior spans not adjacent to an exterior span. In this situation, moments in the support region will not cause uplift. Therefore, in bridges where uplift cannot occur due to support details, RMII can be used for interior spans, and 1.5 times RMII can be used for exterior span restraint moments. Calculated restraint moment increments are added to the summation from the preceding time step to determine restraint moments at the end of the current time step.

If AGDK is greater than AGCT, the adjustment from noncomposite to composite section described previously is made when the end time of the time step is greater than or equal to AGDK. Therefore, the analysis of composite section behavior begins on the succeeding time step. If output of the minimum restraint moment is called for, the time at which the minimum RMII occurs is stored for later output.

Using this incremental approach, the resulting calculated time-dependent restraint moments represented a significant improvement as compared to the PCA method. The comparisons are presented in Chapter Two of this report. The incremental approach is incorporated in BRIDGERM.

**Step 7 - Output Results**

The program outputs values for RME, RMIL, RMIR, and RMII restraint moments at user-selected times. If the user requests output of all calculated restraint moments, values are output at each time step. Otherwise, values are output at times contained in the user-specified vector UTIME.

Additional information which may be useful to output are the following. Strand stress, in psi, is contained in variables FST up to age of continuity and FST1 and FST2 after age of continuity for exterior and interior spans, respectively. Differential shrinkage restraint moment component is contained in vector XMS. Prestress creep restraint moment component is contained in vectors XMPS1 and XMPS2 for exterior and interior spans, respectively.

**User's Input Instructions**

This section presents instructions for running Program BRIDGERM. For each case problem, data input consists of nine lines containing the information shown in Table E1. Each variable is described below. All variables should be entered as Real values unless otherwise noted. Character data must be entered within single quotation marks.

**Line 1:**

| TITLE - Identification of case problem (Character) |

**Line 2:**

| B1, B2, B3, and B4 - Horizontal dimensions defining girder profile as identified in Fig. E-1, in. |

**Line 3:**

| D1, D2, D3, D4, D5, and D6 - Vertical dimensions defining girder profile as identified in Fig. E-1, in. |
Line 4:
NSP - Number of spans in bridge (Integer)
SL  - Length of typical span, ft
XLD - Distance between supports, ft
XDR - Ratio defining length of strand draping, ft/ft
GS  - Girder spacing, ft
TD  - Deck thickness, in.
WDL - Uniform load due to additional dead load, psf

Line 5:
AGRL - Time between tensioning and prestress transfer, days
AGCT - Time between prestress transfer and establishment of continuity, days
AGDK - Time between prestress transfer and placement of deck, days
NTIME - Number of user-specified times for output of restraint moments (Integer)

Line 6:
UTIME - Vector of times for output of restraint moments, days (NTIME values)

Line 7:
SSC - Centroid of straight strands, in.
DSC - Centroid of draped strands at end of girder, in.
WSC - Centroid of draped strands between hold-down points, in.
NSL - Equal to 1 for stress-relieved strands, equal to 2 for low-relaxation strands (Integer)
NSS - Number of straight strands (Integer)
NDS - Number of draped strands (Integer)
ASTD - Cross-sectional area of one strand, in.²
FST - Initial strand prestress, psi

Line 8:
FCI - Girder concrete compressive strength at transfer, psi
FCG - Girder concrete compressive strength at 28 days, psi
FCO - Deck concrete compressive strength at 28 days, psi
WCG - Unit weight of girder concrete,pcf
WCD - Unit weight of deck concrete, pcf

Line 9:
VULT - Ultimate creep coefficient for girder concrete, dimensionless
ESHUG - Ultimate shrinkage strain for girder concrete, millionths
ESHUD - Ultimate shrinkage strain for deck concrete, millionths

The program may be run interactively or in batch mode. To run interactively, type "BRIDGERM" and execute. The input prompts will then appear for each of the nine lines described previously. Input data for TITLE should be enclosed within single quotation marks. Data should be separated by commas or blank spaces. To obtain a hard copy of input and output, while running interactively, use CTRL P to direct all data to the printer.

In Batch mode, an input file must be set up containing all required data. Following is example data contained in a file "DATA2" on the disc:

```
'AASHTO-IV 85 FT'
20.26.8.0
54.86.0.9.9
4.95.0.20.0.41.8.0.8.0.30.0
1.14.14.1
-7500.0
3.43.50.0.4.0.12290.153159000.0
5000.6000.4000.150.0.150.
23.600.0.600.
```

To view the data, enter "TYPE DATA2" and execute. To run this example, type the name of the batch file, in this case "RUN2.BAT," and execute. File "RUN2.BAT" contains the command "BRIDGERM <DATA2> OUT2." This command runs BRIDGERM with input file "DATA2" and creates...
output file "OUT2." To view results enter "TYPE OUT2" and execute. To obtain a hard copy of the input or output file, use CTRL P when using the "TYPE" command. The output of this example is given on page E-22. On pages E-23 through E-31 is a listing of Program BRIDGERM.

<table>
<thead>
<tr>
<th>Line Number</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>TITLE</td>
</tr>
<tr>
<td>2</td>
<td>B1, B2, B3, B4</td>
</tr>
<tr>
<td>3</td>
<td>D1, D2, D3, D4, D5, D6</td>
</tr>
<tr>
<td>4</td>
<td>NSP, SL, XLD, XOR, GS, TD, WDR</td>
</tr>
<tr>
<td>5</td>
<td>AGRL, AGCT, AGDX, NTIME</td>
</tr>
<tr>
<td>6</td>
<td>UTIME (1...NTIME)</td>
</tr>
<tr>
<td>7</td>
<td>SSC, DSC, WSC, NSL, NSS, NDS, ASTD, FST</td>
</tr>
<tr>
<td>8</td>
<td>FCI, FCG, FCD, WCG, WCD</td>
</tr>
<tr>
<td>9</td>
<td>VULT, ESHUG, ESHUD</td>
</tr>
</tbody>
</table>

**Table E1 - Data Input for BRIDGERM**

<table>
<thead>
<tr>
<th>STRAND TENSION AT TRANSFER</th>
</tr>
</thead>
<tbody>
<tr>
<td>TIME</td>
</tr>
<tr>
<td>(days)</td>
</tr>
<tr>
<td>14.</td>
</tr>
<tr>
<td>17.</td>
</tr>
<tr>
<td>20.</td>
</tr>
<tr>
<td>25.</td>
</tr>
<tr>
<td>32.</td>
</tr>
<tr>
<td>42.</td>
</tr>
<tr>
<td>56.</td>
</tr>
<tr>
<td>60.</td>
</tr>
<tr>
<td>100.</td>
</tr>
<tr>
<td>125.</td>
</tr>
<tr>
<td>150.</td>
</tr>
<tr>
<td>200.</td>
</tr>
<tr>
<td>250.</td>
</tr>
<tr>
<td>300.</td>
</tr>
<tr>
<td>400.</td>
</tr>
<tr>
<td>500.</td>
</tr>
<tr>
<td>600.</td>
</tr>
<tr>
<td>800.</td>
</tr>
<tr>
<td>1000.</td>
</tr>
<tr>
<td>1250.</td>
</tr>
<tr>
<td>1500.</td>
</tr>
<tr>
<td>1800.</td>
</tr>
<tr>
<td>2100.</td>
</tr>
<tr>
<td>2500.</td>
</tr>
<tr>
<td>3000.</td>
</tr>
<tr>
<td>3500.</td>
</tr>
<tr>
<td>4000.</td>
</tr>
<tr>
<td>5000.</td>
</tr>
<tr>
<td>6000.</td>
</tr>
<tr>
<td>7500.</td>
</tr>
</tbody>
</table>

Stop - Program terminated.
PROGRAM BRIDERM
C PROGRAM TO COMPUTE RESTRAINT MOMENTS AS FUNCTION OF TIME
C USING CTL METHOD. NCHRP PROJECT 12-29 CTL PROJECT CR9907/621
C
DIMENSION TI(100), TIR(100), RME(100), RMIL(100), RMIR(100), RMI(100),
1 XMS(100), XMPS1(100), XMPS2(100), FSTI(100), FST2(100)
REAL KV, KSD, KSG
DIMENSION A(7), Y(7), XJ(7), X(3)
DIMENSION BLIN(36), UTIME(64), NT(64)
CHARACTER*20 TITLE
DATA BLIN/1,3,6,11.18.28,42.60.80.100,125,150,175,200,250,300,400,
1500,600,800,1000,1250,1500,1800,2100,2500,3000,3500,4000,5000,
5500,7500,10000,15000,20000,30000,40000,50000/

INPUT DATA
RUN TITLE OF UP TO 20 CHARACTERS: TITLE
WRITE(*,*) 'ENTER: TITLE.'
READ (*,*) TITLE
GIRDER SECTION HORIZONTAL DIMENSIONS: B1, B2, B3, B4 (in)
WRITE(*,*) 'ENTER: GIRDER HORIZONTAL DIMENSIONS. (in)' READ (*,*) B1, B2, B3, B4
GIRDER SECTION VERTICAL DIMENSIONS: D1, D2, D3, D4, D5, D6 (in)
WRITE(*,*) 'ENTER: GIRDER VERTICAL DIMENSIONS. (in)' READ (*,*) D1, D2, D3, D4, D5, D6
NUMBER OF SPANS: NSP (-)
SPAN LENGTH FOR TYPICAL SPAN: SL (*ft)
LENGTH OF SUPPORT: XLD (ft)
RATIO OF DRAPED STRAND LENGTH TO SPAN LENGTH: XDR (-)
GIRDER SPACING: GS (ft)
DECK THICKNESS: TD (in)
ADDITIONAL DEAD LOAD: WDL (psf)
WRITE(*,*) 'ENTER: NUMBER OF SPANS.'
WRITE(*,*) ' 	 SPAN LENGTH. (*ft)
WRITE(*,*) ' 	 DISTANCE BETWEEN ADJACENT GIRDER SUPPORTS. (ft)
WRITE(*,*) ' 	 RATIO OF STRAND DRAPING LENGTH TO SPAN LENGTH.'
WRITE(*,*) ' 	 GIRDER SPACING. (ft)
WRITE(*,*) ' 	 DECK THICKNESS. (in)
WRITE(*,*) ' 	 ADDITIONAL DEAD LOAD. (psf)
READ (*,*) NSP, SL, XLD, XDR, GS, TD, WDL
STRAND AGE AT PRESTRESS RELEASE: AORL (days)
GIRDER AGE AT ESTABLISHMENT OF CONTINUITY: AGCT (days)
GIRDER AGE AT TIME DECK IS IN PLACE: AGDK (days)
NUMBER OF TIMES FOR OUTPUT OF RESULTS: NTIME (-)
WRITE(*,*) 'ENTER: STRAND AGE AT PRESTRESS RELEASE. (days)
WRITE(*,*) ' 	 GIRDER AGE AT CONTINUITY. (days)
WRITE(*,*) ' 	 GIRDER AGE AT TIME DECK IS IN PLACE. (days)
WRITE(*,*) ' 	 NUMBER OF TIMES FOR OUTPUT OF RESULTS.'
READ (*,*) AORL, AGCT, AGDK, NTIME
C TIMES AT WHICH RESULTS ARE OUTPUT: UTIME (days)
WRITE(*,*) 'ENTER: TIMES FOR OUTPUT OF RESULTS. (days)
READ (*,*) (UTIME(I), I=1, NTIME)
C CENTROID OF STRAIGHT STRANDS: SSC (in)
C CENTROID OF DRAPED STRANDS AT GIRDER END: DSC (in)
C CENTROID OF DRAPED STRANDS AT MIDSPAN: WCS (in)
C TYPE OF STRAND: NSL (1=SR, 2=LR)
C NUMBER OF STRAIGHT STRANDS: NSS (-)
C NUMBER OF DRAPED STRANDS: NDS (-)
C CROSS-SECTION AREA OF STRAND: ASTD (sq in)
C INITIAL STRAND TENSION: FST (psi)
WRITE(*,*) 'ENTER: CENTROID OF STRAIGHT STRANDS. (in)
WRITE(*,*) 'CENTROID OF DRAPED STRANDS AT GIRDER ENDS. (in)

E-23
C UP TO CONTINUITY AGE
I=1
8 IF (BLIN(I).GT.AGCT) GO TO 9
TIR(I)=BLIN(I)
I=I+1
GO TO 8
9 NAGESR=I
TIR(NAGESR)=AGCT
C AFTER CONTINUITY AGE
IBL=1
ICT=1
I=1
TIR(I)=AGCT
ITMIN=0
C 10 I=I+1
ADAO=AGCT
IF (IBL.LE.2) THEN
IF ((BLIN(IBL)+AGCT).LT.BLIN(IBL)) ADAO=0.
IF ((BLIN(IBL)+AGCT).GE.BLIN(IBL)) ADAO=AGCT
END IF
C IF (UTIME(ICT).EQ.-1) THEN
ITMIN=ICT
ICT=ICT+1
END IF
C IF ((BLIN(IBL)+ADAO).LT.UTIME(ICT)) THEN
TIR(I)=BLIN(IBL)+ADAO
IBL=IBL+1
GO TO 10
END IF
C IF (UTIME(ICT)+TIR(IBL)+AGCT).LT.UTIME(ICT)) THEN
TIR(I)=TIR(IBL)+AGCT
IBL=IBL+1
GO TO 10
END IF
C 70 CONTINUE
NAGES=I
C 3. CALCULATE GEOMETRIC PROPERTIES OF SECTION
C CIRCUMFERENCE OF GIRDER CROSS-SECTION
C I- OR T- SECTION
CIRG=BI+B2+2*(D1-D3-D4-D5)+2*SQRT(B4**2+D4**2)
CIRC=BI+2*SQRT(D2**2+B2**2)+(B2-B3)**2
CIRC=CIRG-B1
C BOX SECTION
IF ((D3,EQ.0.0),AND.(D5,EQ.0.0)) THEN
CIRG=BI+B2+2*(B1-B3)+(B2-B3)+2*(D1-D2-D6)
CIRC=CIRG-B1
ENDIF
C NONCOMPOSITE SECTION
A(7)=AREA OF EACH ELEMENT OF SECTION
A(1)=B1*2
A(2)=(2.*B4+B3)*D3
A(3)=(B1-B2*2)*D3/2.
A(4)=2.*B4*D4/2.
A(5)=(B3+D1-D2-D3-D6)
A(6)=(B2-B3)*D5/2.
A(7)=B2*6
C Y(I)=DISTANCE FROM BOTTOM FIBER TO CENTROID OF EACH ELEMENT
Y(I)=D1-D2-D3/2.
Y(I)+D1-D2-D3-3/2.
Y(I)=D1-D2-D3-D6/2.+D6
Y(I)+D5/3.*D6
Y(I)+D6/2.
C X(I)=MOMENT OF INERTIA OF EACH ELEMENT
X(I)=D1-D2-D3-D6/12.
X(I)=(B1+2.*B4+B3)**3/2.
X(I)=2.*B4*D4**3/36.
X(I)=(B3+D1-D2-D3-D6)**3/36.
X(I)=(B2-B3)*D5**3/36.
X(I)+D2*6**3/12.
AO=0.
DO 470 1=1,7
470 AG=AO+A(I)
TJ=0.
DO 480 1=1,7
480 TJ=TJ+X(I)
VB=0.
DO 490 1=1,7
490 VB=VB+A(I)*Y(I)
V=VB/AG
YT=D1-YB
X100=0.
DO 500 1=1,7
500 X100=X100+A(I)*(Y(I)-YB)**2
X10=XI0+X100
VS=AG/CIRG
VSc=AG/CIRC
E=VSc**CE
C COMPOSITE SECTION
C EFFECTIVE TOP FLANGE WIDTH
X(I)=SL*12./4.
X(2)=GS*12.
X(3)=TD*12.+B3
BE=10000.
DO 520 1=1,3
520 IF (BE.GT.X(I)) BE=X(I)
520 CONTINUE
IF ((D3,EQ.0.0),AND.(D5,EQ.0.0)) BE=GS*12.
ANE=SQRT(FCD/FCO)
A(I)=ANE*BE+TD
A(2)=AO
Y(1) = D1 + TD/2.
Y(2) = YB
X(J)(1) = XNE + BE + TD*3/12.
X(J)(2) = XIG
AC = A(1) + A(2)
YBC = (A(1)*Y(1) + A(2)*Y(2))/AC
YTG = D1 - YBC
XIGC = X(J)(1) + X(J)(2) + A(i)*(Y(1) - YBC) + A(2)*(Y(2) - YBC)**2
EC = YBC - CE

C COMPUTE DEAD LOAD MOMENTS
XMO = 12.*(AO/144.)*WCO*SL**2/8.
WDLT = ((AO*WCG + OS*12.*TD*WCD)/144 + WDL*GS)/1000.
XMC = 12000.*WDLT*SL**2/8.

C COMPUTE LOSSES FROM TENSIONING OF STRAND TO TRANSFER OF PRESTRESS
IF (NSL.EQ.1) THEN
  C STRESS-RELIEVED STRAND
  RETCON = 10
  FPY = 230000
ENDIF
IF (NSL.EQ.2) THEN
  C LOW-RELAXATION STRAND
  RETCON = 45
  FPY = 243000
ENDIF
TEMP = FST/FPY - 0.55
IF (TEMP.LT.0.05) TEMP = 0.05
FST = (LOG10((24.*NSL*1,76*OMR)/LOG10((24.*OMR)))*TEMP + RETCON
RST = FST + RET

C ADDED STRESS DUE TO DECK DEAD LOAD
ADDBACK = XC* (XMC - XMO) * EC/XIGC
FST = FST + ADDBACK

C LOSS DUE TO CONCRETE SHRINKAGE
UPLT = WDLT*SL*XLD/2.
BET = XLD/SL

C COMPUTE RESTRAINT MOMENTS AFTER CONTINUITY
OUTALL = 1
IF (OUTALL.EQ.1) GO TO 16
16 WRITE(*,110) TI(1),0.0,0.0,0.0,FST/1000.

C 17 RME(1) = 0.0
RMIL(1) = 0.0
RMIR(1) = 0.0
FST(1) = FST2 - FST
FST2 = FST2*FST
XNID = 290000000./133.*(WCD**1.5)*SQRT(FCD)
USH = ESHUG+29.0
SSF = 1.13-0.086*VS
XMM = XMO
XI = XIG
ES = E
AS = AQ
DO 72 1 = 2.NAGESR
T1 = TIR(1-1)
T2 = TIR(1)
C LOSS DUE TO CONCRETE CREEP
72 CONTINUE
PSH=T2*KSG/(DSO+T2*KSG)-T1*KSG/(T1*KSG+DSO)
SH=USH*SSF*PSH

TEMP=(0.5*(FST1(I-1)+FST2(I-1)))/FPY-0.55
IF (TEMP.LT.0.05) TEMP=0.05

LABEL=2.*L1

LA=USH*SSF*PSH
C 00
TEMP(0.5*(FST1(I-1)+FST2(I-1)))/FPY-0.55
IF (TEMP.LT.0.05) TEMP=0.05

TEM2=LO010(24*(T2+AGRL)-LOG10(24*(T1+AGRL)))*TEMP/RETCUN

CLA=1.13*TAVG**(-0.094)

PHI FACTOR
PHI=VULT*PCR

CREEP EFFECT FACTOR FOR PRESTRESS AND DEAD LOAD CREEP
CMFC=EXP(-PHI*CLA)

CREEP EFFECT FACTOR FOR DIFFERENTIAL SHRINKAGE
CMFS=CMFC/(CLA*PHI)

COMPUTE COMPONENTS FOR RERAINT MOMENTS

1. DIFFERENTIAL SHRINKAGE STRAIN
IF (T2.LT.AODK) THEN
XMS(I)=0.0
END IF
T2D=T2-AODK
T1D=T1-AODK
TAVOD=(T2D+T1D)/2.
EDCK=FCD*TAVOD/(ALPHD+BETAD*TAVOD)
EDCK=33.5*WCD*1.5*5*QR(T) /1000.
XND=29000./EDCK

DISCHINGER MODIFICATION AFTER AGDISCH DAYS
IF (T1D.GE.AODISCH) THEN
XMOD=1.1-EXP(-VULT*XND/1+DHD/(1+DHD+XND))
END IF

ELSE
EMSHEMD*XMOD
END IF

ELSE
EMHSD=EMHSMD
END IF

2. DEAD LOAD CREEP
XMDL=XMM/12000.

3. PRESTRESS CREEP
E1=YBC-DSC
E2=YBC-SCS
IF (T2.LE.AODK) THEN
E1=SB-DSC
E2=SB-SCS
END IF
E3=DSC-WSC
L1=XDR*SL

L2=SL-2.*L1

3A. END SPANS
CALCULATE PRESTRESS LOSS
XMR1=12000.*RME(I-1)/2.
FS1=FST1(I-1)
FC1=AST*FS1*(1/AS*ES**2/2XI)-(XMM*XMR1)*ES/XI
CR1=FC1*UCR*SCF*PCR
RET1=TEM2*FS1
FST1(I)=FST1(I-1)-(CR1+SH+RET1)
FPE1=AST*DST1(I)+FST1(I)*2.2.
P11=ND*FPE1/1000.
P21=NS*FPE1/1000.

XMP5(I)+(P11*E1+E3*(L1+L2)/SL)+P21*E2/12

3B. INTERIOR SPANS
CALCULATE PRESTRESS LOSS
XMR2=12000.*RME(I-1)
FS2=FST2(I-1)
FC2=AST*FS2*(1/AS*ES**2/2XI)-(XMM*XMR2)*ES/XI
CR2=FC2*UCR*SCF*PCR
RET2=TEM2*FS2
FST2(I)=FST2(I-1)-(CR2+SH+RET2)
FPE2=AST*FST(I)+FS2/2.
*P12=ND*FPE2/1000.
P22=NS*FPE2/1000.

XMP5(I)+(P12*E1+E3*(L1+L2)/SL)+P22*E2/12

CALCULATE RESTRAINT MOMENTS

IF (NSP.EQ.2) BET=1.5*XLD/SL
CEND=-1/(1+BET/ALPHA)
TEMP=CMFS*1.5*XMS(I)+CMFC*(XMDL-1.5*XMS2(I))
IF (NSP.EQ.2) THEN
RME(I)=RME(I-1)+TEMP*CEND
END IF

CINT=(-3.+6.*(1+BET/ALPHA))/(1.-4.*(1.+BET/ALPHA)*(1.+BET/ALPHA))
CINT=-CMFS*XMS(I)+CMFC*(2.*XMDL/3.-XMP52(I))
RHI1(RH1(I-1)+TEMP+CINT

UPLIFT ANALYSIS
IF (((XMR1+XMR2)/2.).GE.0.0) SIGN1=1.0
IF (((XMR1+XMR2)/2.).LT.0.0) SIGN1=-1.0
IF (((XMR1+XMR2)/2.).LE.0.0) SIGN1=0.0
IF (((1+BET*SIGN1+ABS(RME(I-1)))+ABS(RMIL(I-1)))+GE.ULPT) THEN
TEMP=2.4.*(1.+BET/ALPHA)+TEMP3=3.*(1.+2.*BET/ALPHA)+TEMP1
TEMP=TEMP2(1,-B.*1+BET/ALPHA)
TEMP2=2.*TEMP-3.*TEMP1-4.*TEMP2
IF (NSP.EQ.3) THEN
TEMP2=(TEMP+TEMP)
TEMP3=(TEMP+TEMP)
END IF
RMI1(RH1(I-1)+TEMP2
RMIII(RM1(I-1)+TEMP3
RMII(RM1(I-1)+TEMP2
ELSE
PROGRAM BRIDGELL

Introduction

The purpose of Program BRIDGELL is to calculate maximum moments and shears for girders in multispan continuous bridges subject to AASHTO truck and lane loading. Load magnitudes and patterns are according to 1983 AASHTO Specifications (14) for HS loading. The program is capable of analyzing the continuous bridge neglecting continuity for positive moment for the situation in which positive reinforcement is not provided at supports. Also included in the program is analysis for additional dead load acting on the continuous bridge. Details of data input and output, analysis assumptions, capabilities and limitations of Program BRIDGELL are discussed below in the solution steps. The program was initially written in Data General Fortran 77 and implemented on CTL’s Data General MV10000 Computer. The program was then recompiled using Microsoft Fortran for use on IBM PC Compatibles with MS-DOS 3.XX. A listing of the PC version of Program BRIDGELL is included starting on page E-48. An Example Problem is also given.

Solution Steps

Program BRIDGELL is divided into six solution steps as follows:

1. Input data for bridge configuration and load generation.
2. Compute information for elastic analysis.
3. Generate additional dead load and AASHTO HS loadcases.
4. Conduct elastic analysis for each loadcase.
5. Store extreme values.
6. Output results.

Each step is described in detail below.

Step 1 - Data Input

The program input is designed to be accomplished either interactively through keyboard input or through an input file. Each problem requires four lines of input data. All data must be input.
The program will not assign default values. Data is input on unformatted lines. Input values must be separated by commas or blank spaces. Input values must correspond to the variable type, either Integer or Real. Real values may be input with or without a decimal point. Integer values must be input without a decimal point.

Line 1 is for identification of the run. A description of up to 20 characters within single quotation marks should be entered on this line.

Line 2 contains the variables OTCD, GS, NSP, and WDL. Program output is controlled by the specified value of OTCD. If "1" is entered, generated loads, shears, and moments for each loadcase, extreme shears, and moments for live load only, and extreme shears and moments for live load plus impact are output. If "2" is entered, extreme shears and moments for both live load and live load plus impact are output. An input value of "3" results in output of extreme shears and moments from live load only. An input value of "4" results in output of extreme shears and moments from live load plus impact only. OTCD is an integer variable. The girder spacing in feet is entered for the Real variable GS. NSP contains the number of spans in the continuous bridge. NSP is an Integer variable. WDL is the additional dead load due to parapet, wearing surface, etc. in psf. If WDL is set equal to zero, the analysis for additional dead load is not done.

Line 3 contains the vector SL. The lengths, in feet, of each of the NSP spans in the bridge are to be entered for this variable. SL is a Real variable. The number of values entered on Line 3 must equal NSP.

Line 4 contains the variables XLD, NPTS, NAXSP, NLPTS, NPTINC, and NPSCON. XLD is a Real variable used to establish the magnitude of the AASHTO HS truck and lane loads. The live load is determined by multiplying AASHTO HS20-44 load magnitudes by XLD. Therefore, with XLD equal to 1.0, live load will be HS20-44. A multiplier of 1.25 entered for XLD will result in HS25 live load.

The variables NPTS and NAKSP control the quantity and configuration of HS truck loads applied to each span of the bridge, as shown in Fig. E-5a. NPTS is the number of locations of the HS truck within each span. Truck location is controlled by the position of the truck's central axle. In addition to truck locations within the span, the central axle is placed at each support. NAXSP controls the number of axle spacings for variable spacing from 14 to 30 ft of the third axle, as shown in Fig. E-5b. The minimum value for NAXSP is two. In this case the HS truck's third axle is placed at 14 and 30 ft. For each truck location, the bridge is analyzed with NAKSP axle spacings for both directional orientations of the truck.

The variables NLPTS and NPTINC control the locations of point loads applied in conjunction with AASHTO HS lane loads. For each span in which a point load is applied in addition to uniform load, NLPTS specifies the number of locations for the point load, as shown in Fig. E-6. The locations of point loads are controlled by NPTINC. The spacing of the point loads is equal to the span length divided by NPTINC. The loads are arranged such that the distribution of point loads is centered about midspan of the subject span. NLPTS should be entered as an odd number in order that an equal number of locations are provided on each side of midspan. If NLPTS is greater than NPTINC, the program adjusts the value of NLPTS such that point loads fall within the length of the subject span.

The variable NPSCON controls the method of analysis used for loadcases in which positive moments occur at supports of the continuous bridge. For determination of live load plus impact moments on the continuous structure, the nature of continuity at supports must be considered for various load configurations. If positive moment reinforcement is not provided, no reliable positive moments can develop at supports. For AASHTO truck loads occurring on one span of a multispans bridge, this implies that the continuous structure for resisting the load consists of three spans for a loaded interior span and two spans for a loaded end span. For a loaded interior span of a fully continuous bridge, negative moments occur at the two supports adjacent to the loaded span and positive moments occur at the next...
Ex. NPTS = 4
X = Truck locations controlled by NPTS
+ = Truck locations at supports

(a) Truck Central Axle Locations

Ex. NAXSP = 3

(b) Variable Axle Spacing

Figure E-5 AASHTO HS20-44 Truck Loading

Figure E-6 AASHTO HS20-44 Lane Loading
support in each direction. Since positive moment resistance is not provided, these moments are assumed to be zero, in effect isolating the loaded span and the two adjacent spans from the rest of the bridge, as shown in Fig. E-7a. Similarly, for a loaded end span, negative moment occurs at the first interior support and positive moment occurs at the second interior support. Since positive moment is not accounted for, the moment is assumed to be zero at the second interior support. Therefore, the effective continuous structure for an end span loaded with AASHTO truck load consists of the loaded span and the first adjacent span, as shown in Fig. E-7b. An input value of zero for NPSCON allows analysis assuming continuity for negative moment only as described above. Continuity for positive moment can be analyzed by using an input value of one for NPSCON.

Step 2 - Preliminary Calculations for Elastic Analysis

The elastic analysis used in BRIDGEFL is based on the three moment equation method for analysis of continuous beams. In Step 2, the three moment flexibility equations for calculating moments at redundant supports are formed into a matrix, FMAT. This matrix is algebraically triangularized for later solution of the system of equations in subroutine ANALYZE. For purposes of the elastic analysis, modulus of elasticity and moment of inertia are assumed to be constant for all spans. Since deflections are not calculated in BRIDGEFL, their values are set to one. Also, in Step 2, matrices in which extreme shears and moments will be stored are initialized.

Step 3 - Generate Additional Dead Load and AASHTO HS Loadcases

Loads are generated in Subroutine LOADGEN. The first loadcase is for additional dead load acting on the continuous bridge. If WDL is greater than zero, the input value is multiplied by the girder spacing, GS, to produce the uniform load. The uniform load is applied to all spans in the bridge and Subroutine ANALYZE is called to perform the elastic analysis.

AASHTO standard HS truck and lane loads are generated over the
length of the continuous bridge. For each loadcase, the bridge is analyzed and extreme shears, midspan moments, and support moments are stored if extremes from previous loadcases are exceeded. The analysis is described in Step 4 below. Generation of truck and lane loads is done in subroutine LOADGEN. The magnitude of HS20-44 loads are modified by the factors XLD, described previously, and 0.5 to reduce axle load to wheel load. The lateral distribution of wheel loads is accounted for using the fraction of wheel load term for bridges with two or more lanes of traffic and a concrete deck supported on prestressed concrete girders.

AASHTO HS truck loads are applied to each span with quantity and location determined by user input values of NPTS and MAXSP. As shown in Fig. E-5a, truck loads are placed throughout each span by locating the central axle at evenly spaced points along the span. For each location of the central axle, the truck is configured with various axle spacings for both directional orientations. When the truck is located over interior supports such that axles are loading separate spans, the point loads are correctly located by subroutine LOCATE. Point loads which fall outside the length of the bridge when the truck is near either end are ignored.

Lane loadcases are applied in various patterns over the length of the bridge. For most lane load patterns, the lane load is made up of uniform load plus a single point load applied in different patterns. For patterns configured to produce maximum negative moments at supports, the lane load consists of uniform load plus two point loads applied to selected spans. For each span in which a point load is applied, the number of point load applications and their locations are controlled by the variables NLPTS and NPTINC, as described previously. Six categories of lane load patterns shown in Fig. E-8 are used in the program.

The first load pattern shown in Fig. E-8a, involves loading each individual span with uniform load plus point load. For the second and third patterns, shown in Figs. E-8b and c, the entire bridge is loaded with uniform load and point loads are placed sequentially in each span.

Fig. E-8 AASHTO Lane Load Patterns Analyzed in BRIDGELL
and near each support, respectively. The fourth pattern, shown in Fig. E-8d, produces maximum positive midspan moments. The span in which maximum midspan moment is to be induced is loaded with uniform and point loads and alternate spans are loaded with uniform load. The fifth pattern, shown in Fig. E-8e, causes maximum positive moment to occur at an interior support. The two spans immediately adjacent to the support are not loaded. The second span away from the support and alternate spans in each direction are loaded with uniform load. The point load is placed separately in each of the loaded spans nearest the support. The last load pattern, shown in Fig. E-8f, causes maximum negative moment to occur at an interior support. The two spans adjacent to the support are loaded with both uniform and point loads. Alternate spans are also loaded with uniform load.

Lane load patterns are generated to produce maximum positive midspan moments in each of the spans as well as maximum negative and positive moments at each interior support. For the third loadcase, in which point loads are placed near supports to produce maximum shear forces, the heavier point load specified by AASHTO Section 3.7.1.3 is applied. For each lane load configuration in which a point load is applied within a span, the pattern of uniform load is repeated for each point load location specified by the variables NLPTS and NPTINC. For the sixth load pattern, two point loads are applied as given in AASHTO specifications and the locations of both point loads are varied for each pattern of uniform loading. For each application of uniform load, the entire span length is loaded.

Step 4 - Elastic Analysis
For each loadcase generated in subroutine LOADGEN, subroutine ANALYZE is called to conduct an elastic analysis of the continuous beam under the applied loads. The first step of the analysis is to calculate simple span end rotations under the applied loads. The moments at redundant supports which result from restoring continuity of adjacent spans are calculated using the information generated in Step 2. Shear forces for each span due to imposed loads and redundant moments are then calculated. Reactions at each support are calculated from shear forces and the overall equilibrium of the bridge is checked. The next step is to determine maximum midspan moments for each span. If a span is not loaded or has end shears of the same sign, the average of end moments is stored. If the span has end shears of opposite sign, the location of maximum midspan moment is found by locating the point within the span where shears is zero. The magnitude of maximum midspan moment is then calculated from support moment, shear, and applied loads.

For AASHTO truck load cases and AASHTO lane load on an individual span, the elastic analysis is conducted for the reduced continuous structure if the user enters zero for NPSCON. For a loaded exterior span, the loaded span and adjacent span are analyzed. For a loaded interior span, the loaded span and the two adjacent spans are analyzed. If the user enters one for NPSCON, the full structure is analyzed for all load cases. Regardless of the value of NPSCON, the full structure is analyzed for the AASHTO lane loadcases shown in Fig. E-8 b through f.

Step 5 - Store Extreme Moments and Shears
After the elastic analysis in subroutine ANALYZE is completed for each loadcase, resulting shears and moments are compared to extreme values from preceding loadcases. Maximum end shears, maximum midspan moments, and maximum and minimum support moments are updated after each analysis. Locations of maximum midspan moments are also stored.

Step 6 - Output Results
Depending on the user-specified value of OTCD, varying amounts of information are output by Program BRIDGELL. If OTCD is entered as 1, all information generated by the program is output. During load generation, subroutine OUTPUT2 outputs each loadcase. Loads are specified by loaded span, load magnitude in kips or kips per ft, and load location. Point load locations are in feet from the left support of the loaded span. Uniform loads are indicated by "-1" output for
load location. After a set of loads is output, results of the elastic
analysis for those loads are output at the end of subroutine ANALYZE.
Support reactions and moments, span lengths, end shears, maximum
midspan moments, and locations of maximum midspan moments are output
for the entire bridge.

After all loadcases have been analyzed, maximum and minimum
support moments, maximum shears, and maximum midspan moments and
locations are output for each support and each span. Extreme values
are output for live load only and live load plus impact. Impact
factors for shears and midspan moments are calculated from the length
of the subject span. Impact factors for support moments are
calculated from the average of the lengths of the two adjacent spans.
If 2 is entered for OTCD, extreme values for live load and live load
plus impact are output. For OTCD equal to 3, extreme results for live
load only are output. For OTCD equal to 4, extreme results for live
load plus impact are output.

If WDL is greater than zero, results of the analysis for
additional dead load are output. Included in this output are
reaction, shear, and moment for each support, and maximum moment and
location for each span.

Support moments and midspan moments are output for each span for
the loadcase which causes maximum midspan moment. The support moments
are for use in determining the degree of continuity for the bridge as
described in Chapter Three of this report.

User's Input Instructions

This section contains instruction for running Program BRIDGELL.
For each case problem, data input consists of four lines containing
the information in Table E2. Each variable is described below. All
variables should be entered as Integer values unless otherwise noted.
Character data must be entered within single quotation marks.

Line 1:
   TITLE - Identification of case problem (Character)

Line 2:
   OTCD - Control for program output, equal to 1, 2, 3, or 4
   GS  - Girder spacing, ft (Real)
   NSP - Number of spans in bridge
   WDL - Uniform load due to additional dead load, psf

Line 3:
   SL  - Vector of span lengths, ft (NSP Real values)

Line 4:
   XLD - Multiplier for magnitude of HS loads (Real)
   NPTS - Number of central axle locations per span for HS truck
   NAXSP - Number of axle spacings for HS truck
   NLPTS - Number of point load locations for HS lane load
   NPTINC - Control for spacing of point loads for HS lane load
   NPSCON - Control for continuity analysis, equal to zero for
             negative continuity only, equal to one for positive and
             negative continuity

The program may be run interactively or in Batch mode. To run
interactively, type "BRIDGELL" and execute. The input prompts will
then appear for each of the four lines described previously. Input
data for TITLE should be enclosed within single quotation marks. Data
should be separated by commas or blank spaces. To obtain a hard copy
of input and output while running interactively, use CTRL P to direct
all data to the printer.

In Batch mode, an input file must be set up containing all
required data. Following is data contained in a file "DATA1" on the
disc:

'100 FT. 4 SPAN'
2.3.0.4.30.
100. 100. 100. 100
1.14.7.7.10.0
To view the data enter "TYPE DATA1" and execute. To run the example, type the name of the batch file, in this case "RUN1.BAT", and execute. File "RUN1.BAT" contains the command "BRIDGELL <DATA1> OUT1." This command runs BRIDGELL with input file "DATA1" and creates output file "OUT1." To view results enter "TYPE OUT1" and execute. The output of this example is given on page E-46. On pages E-48 through E-62 is a listing of Program BRIDGELL.

---

**TABLE E2 - DATA INPUT FOR BRIDGELL**

<table>
<thead>
<tr>
<th>Line Number</th>
<th>Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>TITLE</td>
</tr>
<tr>
<td>2</td>
<td>OTCD, GS, NSP, WDL</td>
</tr>
<tr>
<td>3</td>
<td>SL (1..NSP)</td>
</tr>
<tr>
<td>4</td>
<td>XLD, NPTS, NAXSP, NLPTS, NPTINC, NPSCON</td>
</tr>
</tbody>
</table>

---

**ENTER: TITLE.**

**ENTER: SPAN LENGTHS. (ft)**

**ENTER: MULTIPLIER FOR HS20-44 LOAD.**

---

**TABLE E2 - DATA INPUT FOR BRIDGELL**

<table>
<thead>
<tr>
<th>SPAN</th>
<th>SPRT</th>
<th>LENGTH</th>
<th>LEFT SPAN REACTION</th>
<th>RIGHT SUPPORT SHEAR</th>
<th>MAX SPAN LOCATION MAXIMUM MOMENT</th>
<th>MINIMUM MOMENT</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>9.43</td>
<td>100.00</td>
<td>9.43</td>
<td>-14.57</td>
<td>0.00</td>
<td>185.20</td>
</tr>
<tr>
<td>2</td>
<td>27.43</td>
<td>100.00</td>
<td>12.86</td>
<td>-11.14</td>
<td>87.34</td>
<td>53.57</td>
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<tr>
<td>3</td>
<td>22.29</td>
<td>100.00</td>
<td>11.14</td>
<td>-12.86</td>
<td>87.24</td>
<td>46.43</td>
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<tr>
<td>4</td>
<td>27.43</td>
<td>100.00</td>
<td>14.57</td>
<td>-9.43</td>
<td>185.20</td>
<td>60.71</td>
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<tr>
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<td>9.43</td>
<td>100.00</td>
<td>9.43</td>
<td>0.00</td>
<td>185.20</td>
<td>60.71</td>
</tr>
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</table>

**AASHTO HS TRUCK LOAD CASES BEING ANALYZED.**

**NUMBER OF TRUCK LOADCASES = 854**

**AASHTO HS LANE LOAD CASES BEING ANALYZED.**

**NUMBER OF LANE LOADCASES = 269**

**TOTAL NUMBER OF LOADCASES = 1123**

---

**CALCULATED EXTREME SHEARS AND MOMENTS FOR LL.**

**SPAN**

**SPRT**

**MAXIMUM LEFT SHEAR**

**MAXIMUM RIGHT SHEAR**

**MINIMUM SUPPORT MOMENT**

**MAXIMUM SUPPORT MOMENT**

**MINIMUM MIDSPAN MOMENT**

**MAXIMUM MIDSPAN MOMENT**

**LOCATION**

---

**E-45**

---

**E-46**
SUPPORT MOMENTS FOR MAXIMUM MIDSPAN MOMENTS.

<table>
<thead>
<tr>
<th>SPAN</th>
<th>LEFT SPT</th>
<th>MIDSPAN</th>
<th>RIGHT SPT</th>
</tr>
</thead>
<tbody>
<tr>
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<td>MOMENT</td>
<td>MOMENT</td>
<td>MOMENT</td>
</tr>
<tr>
<td>It-Rip</td>
<td>It-Rip</td>
<td>It-kip</td>
<td>It-Rip</td>
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<tr>
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<td>.00</td>
<td>896.20</td>
<td>-453.32</td>
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<td>729.41</td>
<td>-384.68</td>
</tr>
<tr>
<td>3</td>
<td>-372.85</td>
<td>729.41</td>
<td>-334.68</td>
</tr>
<tr>
<td>4</td>
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<td>896.20</td>
<td>.00</td>
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</table>

CALCULATED EXTREME SHEARS AND MOMENTS FOR LL+I.

<table>
<thead>
<tr>
<th>SPAN</th>
<th>MAXIMUM SHEAR</th>
<th>MAXIMUM SUPPORT MOMENT</th>
<th>MINIMUM SHEAR</th>
<th>MINIMUM SUPPORT MOMENT</th>
<th>LOCATION</th>
</tr>
</thead>
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<td>ft-kip</td>
<td>ft-kip</td>
<td></td>
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<td>110.48</td>
<td>-976.46</td>
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</tr>
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<td>-56.05</td>
<td>247.06</td>
<td>-883.01</td>
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</tr>
<tr>
<td>4</td>
<td>56.05</td>
<td>-56.05</td>
<td>110.48</td>
<td>-976.46</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>58.51</td>
<td>-53.76</td>
<td>1095.35</td>
<td>40.00</td>
<td></td>
</tr>
</tbody>
</table>

PROGRAM BRIDGELL

PROGRAM FOR ANALYSIS OF CONTINUOUS BEAM WITH HS LOADING FOR USE IN NCHRP PROJECT 12-29 CTL PROJECT CR9907/821

REAL MAXPM(30), MAXPMLOC(30), MINPM(30), MINPMLOC(30), MGMT(30), 1
MAXNM(30), MINNM(30), MAXSHR(30), LMP(30), LDLLOC(30), 1
DIMENSION SL(30), FACT(30), ETA(31), FAT(30,2), RACT(31), LDLI(30), 1
PHMT(30), XMLOC(30), LDMA(30), PTLD(20), PTLOC(20)

CHARACTER(20) TITLE
COMMON/BLK1/ NSP, SL, GS, WL, XIQC, EC, CITCD, NSPT, NRED, NIMP
COMMON/BLK2/ MAXSHR, MAXPM, MXPMLOC, MINPM, MINPMLOC, MAXNM
COMMON/BLK3/ MAXNM, MINNM, SI, S2, MAXPM1, MAXPM2
COMMON/BLK4/ N1, N2, NSPTR, NPTON

1095.35 WRITE(.,*)'ENTER: 
991.50 READ(...) 'TITLE'
891.50 WRITE(.,*)'ENTER TO OUTPUT ALL RESULTS' 
744.01 WRITE(.,*)'ENTER: 
691.50 WRITE(.,*)'ENTER TO OUTPUT EXTREMES FOR LL ONLY' 
647.00 WRITE(.,*)'ENTER TO OUTPUT EXTREMES FOR LLI ONLY'

C GIRDERS SPACING, GS
WRITE(.,*) 'ENTER: 
ANGLE CONTROLS PROGRAM OUTPUT'
WRITE(.,*) 'ENTER: 11 TO OUTPUT ALL RESULTS'
WRITE(.,*) '21 TO OUTPUT EXTREMES FOR LL AND LL+I'
WRITE(.,*) '31 TO OUTPUT EXTREMES FOR LL ONLY'
WRITE(.,*) '41 TO OUTPUT EXTREMES FOR LLI ONLY'

C NUMBER OF SPANS, NSP
WRITE(.,*) 'ENTER: 
READ(.,*) TITLE'

C ADDITIONAL DEAD LOAD, WDL
WRITE(.,*) 'ENTER: 
READ(.,*) ADDITIONAL DEAD LOAD. 

C SPAN LENGTHS, SL
READ(*,*) SL(1), SL(2), ..., NSP

C ILD IS MULTIPLIER APPLIED TO HS20-44 (EX. ILD1.25 FOR HS25)
C FOR HS TRUCK LOAD: NPTS IS NUMBER OF LOCATIONS FOR TRUCK'S CENTRAL AXLE
C PER SPAN. NAXSP IS NUMBER OF AXLE SPACINGS BETWEEN 14' AND 30'
C FOR EACH CENTRAL AXLE LOCATION. NAXSP SHOULD BE GREATER THAN OR
C EQUAL TO 2.
C FOR HS LANE LOAD: NLPTS IS NUMBER OF POINT LOAD LOCATIONS FOR EACH
C SPAN. SL DIVIDED BY NPTINC IS THE SPACING BETWEEN DIFFERENT POINT
C LOAD APPLICATIONS, THE NLPTS LOCATIONS FOR POINT LOAD APPLICATION
C ARE CENTERED ABOUT MIDSPAN OF THE LOADED SPAN. AN ODD NUMBER SHOULD
C BE ENTERED FOR NLPTS.
C FOR CONTINUOUS BEAM ANALYSIS: NPSCON CONTROLS POSITIVE MOMENT
C CONTINUITY AT SUPPORTS. NPSCON EQUAL TO 1 IMPLIES BEAM IS
C CONTINUOUS FOR POSITIVE MOMENTS ONLY. NPSCON EQUAL TO 0
C IMPLIES BEAM IS CONTINUOUS FOR NEGATIVE MOMENTS ONLY.
C
WRITE(.,*) 'ENTER: 
READ(.,*) MULTIPLIER FOR HS20-44 LOAD.'
WRITE(.,*) 'FOR HS TRUCK LOAD.'
WRITE(.,*) 'NUMBER OF CENTRAL AXLE LOCATIONS PER SPAN.'
WRITE(.,*) 'NUMBER OF AXLE SPACINGS. NAXSP GE 2.'
WRITE(.,*) 'FOR HS LANE LOAD.'
WRITE(.,*) 'NUMBER OF POINT LOAD LOCATIONS PER SPAN.'
WRITE(.,*) 'LOCATION INCREMENT.'
WRITE(.,*) 'I FOR + . I FOR - ONLY CONTINUITY.'

READ(.,*) SL(1), SL(2), ..., NSP, NAXSP, NPSCON

STOP - Program terminated.
C 2. COMPUTE INFORMATION NECESSARY FOR ELASTIC ANALYSIS.
C FOR ELASTIC ANALYSIS, MOMENT OF INERTIA=1, MODULUS=1 FOR ALL SPANS
XIGC=1, EC=1.
C NUMBER OF SUPPORTS
NSPT=NSP+1
C NUMBER OF REDUNDANT SUPPORTS
NRED=NSP-1
C INITIALIZE MATRICES FOR EXTREME VALUES
DO 22 I=1,NSP
MAXPM(I)=1000000
MINPM(I)=0
MAXHN(I)=1000000
MINHN(I)=0
MAXSHR(I,1)=1000000
MAXSHR(I,2)=1000000
22 CONTINUE
DO 23 I=1,NRED
MAXNM(I)=1000000
MINNM(I)=1000000
23 CONTINUE
C COMPUTE "FLEXIBILITY" MATRIX
DO 60 I=1,NRED
DO 60 J=1,2
FMAT(I,J)=0
60 CONTINUE
DO 70 I=1,NRED
FMAT(I,1)=((2/EC)*SL(I)/XIGC+SL(I+1)/XIGC)
FMAT(I,2)=SL(I+1)/(EC*XIGC)
IF (I.EQ.NRED) FMAT(I,2)=0
70 CONTINUE
C SOLVE SYSTEM OF EQUATIONS
C TRIANGULARIZE "FLEXIBILITY" MATRIX
DO 90 I=2,NRED
FACT(I)=FMAT(I-1,2)/FMAT(I-1,1)
FMAT(I,1)=FMAT(I,1)-FACT(I)*FMAT(I-1,1)
FMAT(I,2)=FMAT(I,2)-FACT(I)*FMAT(I-1,2)
90 CONTINUE
C NSPNZ=NSP
DO 605 I=1,NSP
IF (SL(I).EQ.0) NSPNZ=NSPNZ-1
605 CONTINUE
C 3. ANALYZE DL, GENERATE AASHTO HS LOADS. SUBROUTINE LOADGEN.
C 4. ELASTIC ANALYSIS OF EACH LOADCASE. SUBROUTINE ANALYZE CALLED FROM
C SUBROUTINE LOADGEN.
C 5. STORE EXTREME VALUES. IN SUBROUTINE ANALYZE.
C CALL LOADGEN
C 6. OUTPUT RESULTS. ALSO IN SUBROUTINES LOADGEN AND ANALYZE.
IF (OTCD.NE.4) THEN
NIMP=0
CALL OUTPR1
END IF
C IF (OTCD.NE.3) THEN
NIMP=1
CALL OUTPR1
END IF
C STOP
END
C SUBROUTINE LOADGEN
SUBROUTINE LOADGEN
DIMENSION TEMP(3),LDSP(30),N99(2),SL(30),FACT(30),FMAT(30,2)
REAL LDMAO(30),LDLOC(30)
COMMON/BLK1/ NSP,SL,GS,WDL, XIGC,EC,OTCD,NSPT,NRED,NIMP
COMMON/BLK3/ KLD,NL,DSP,LDMAG,LDLOC,NPTS,NAXSP
COMMON/BLK4/ NI,N2,NSPTR,NPSCON
C ANALYZE FOR ADDITIONAL DEAD LOAD ON CONTINUOUS GIRDER
IF (WDL.GT.0.) THEN
KLD=0
N1=1
N2=NSP
NSPTR=NSP
ULOAD=WDL*GS/1000.
KTR=NSPNZ
KTR=0
DO 888 I=1,NSP
IF (SL(I).EQ.0) GO TO 888
KTR=KTR+1
LDSP(KTR)=ULOAD
LDLOC(KTR)=0
888 CONTINUE
CALL ANALYZE
END IF
C FACTLD EQUALS COMBINED MULTIPLIER FOR HS20-44 LOADS.
FACTLD=KLD*0.5*(GS/5.5)
C GENERATION AND ANALYSIS OF HS TRUCK LOADCASES
WRITE(*,*) 'AASMTO HS TRUCK LOAD CASES BEING ANALYZED.
KSP=1
KTR=1
NL=1
KLD=0
TLDO=0
TOTAL=0
DO 625 I=1,NSP
IF (SL(I).EQ.0) GO TO 625
TOTAL=TOTAL+SL(I)
625 CONTINUE
TLDO=TOTAL/SL(1)
C NSPNZ=NSP*(NPTS+1)
672 IF (KTR.GT.NSP) GO TO 671
IF (KTR.LE.(NPTS+1)*KSP) THEN
C 8 9 0 0
KSP=KSP+1
TLDINC=SL(KSP)/(NPTS+1)
ENDIF
DO 660 I=1,NAXSP
KLD=KLD+1
LDLOC(2)=TLDLOC
LDMAO(1)=0.*FACTLD
LDMAO(2)=32.*FACTLD
LDMAO(3)=32.*FACTLD
TEMP(1)=TLDLOC-14.0
TEMP(3)=TLDLOC+14.0*(30.-14.)*(I-1)/(NAXSP-1)
DO 640 J=1,3
IF ((TEMP(J).LT.TOTLN).OR.(TEMP(J).LT.0.0)) THEN
LDLOC(J)=0
LDMAO(J)=0
GO TO 640
ELSE
LDLOC(J)=TEMP(J)
GO TO 640
ENDIF
640 CONTINUE
CALL LOCATE(NSP,SL,LDSP,LDLOC,LDMAO)
CALL ANALYZE
KLD=KLD+1
LDLOC(2)=TLDLOC
LDMAO(1)=32.*FACTLD
LDMAO(2)=32.*FACTLD
LDMAO(3)=32.*FACTLD
TEMP(1)=TLDLOC-14.0*(30.-14.)*(I-1)/(NAXSP-1)
TEMP(3)=TLDLOC+14.0
DO 650 J=1,3
IF ((TEMP(J).LT.TOTLN).OR.(TEMP(J).LT.0.0)) THEN
LDLOC(J)=0
LDMAO(J)=0
GO TO 650
ELSE
LDLOC(J)=TEMP(J)
GO TO 650
ENDIF
650 CONTINUE
CALL LOCATE(NSP,SL,LDSP,LDLOC,LDMAO)
CALL ANALYZE
KLD=KLD+1
LDLOC(2)=TLDLOC
LDMAO(1)=0.*FACTLD
LDMAO(2)=32.*FACTLD
LDMAO(3)=32.*FACTLD
TEMP(1)=TLDLOC-14.0
TEMP(3)=TLDLOC+14.0
DO 670 J=1,3
IF ((TEMP(J).LT.TOTLN).OR.(TEMP(J).LT.0.0)) THEN
LDLOC(J)=0
LDMAO(J)=0
GO TO 670
ELSE
LDLOC(J)=TEMP(J)
GO TO 670
ENDIF
670 CONTINUE
C
NTLD=KLD
WRITE(*,*) 'NUMBER OF TRUCK LOAD CASES = ',NTLD
C
999 CONTINUE
C
GENERATION AND ANALYSIS OF HS LANE LOAD CASES.
WRITE(*,*) 'AERIAL HS LANE LOAD CASES BEING ANALYZED.'
UNILDO,64*FACTLD
PTLDM=19.0*FACTLD
PTLDS=26.0*FACTLD
C
UNIFORM AND POINT ON INDIVIDUAL SPANS
DO 746 I=1,NSP
IF (SL(I).EQ.0) GO TO 746
DO 745 J=1,NLPTS

E-51
770 CONTINUE
LDMAG(NSP+1)=PTLD
IF (II.EQ.1) THEN
LDSP(NSP+1)=1
END IF
IF (II.EQ.2) THEN
LDSP(NSP1)=1
END IF
IF (OTCD.EQ.1) CALL OUTFR2(KLD,NLD,LDSP,LDMAG,LDLOC)
CALL ANALYZE
780 CONTINUE

C PATTERNS FOR MAXIMUM POSITIVE MIDSPAN MOMENT
N99(1)=INT(NSP/2)+MOD(NSP,2)
N99(2)=INT(NSP/2)
DO 800 I=1,NSP
IF (MOD(I,2).EQ.1) IND1=1
IF (MOD(I,2).EQ.0) IND2=2
DO 800 I1=1,NLPTS
KLD=KLD+1
NLD=N99(IND)+1
DO 790 J=1,N99(IND)
LDSP(J)=IND2*(J-1)
LDMAG(J)=UNILD
LDLOC(J)=1
END IF
IF (OTCD.EQ.1) CALL OUTFR2(KLD,NLD,LDSP,LDMAG,LDLOC)
CALL ANALYZE
800 CONTINUE

C PATTERNS FOR MAXIMUM POSITIVE SUPPORT MOMENT
DO 840 I=2,NSP
DO 840 I1=1,NLPTS
DO 970 I2=1,NLPTS
KLD=KLD+1
KTRL=0
KTMP=0
IF (I.EQ.1) THEN
IF (KTMP.LE.NSP) THEN
KTRL=KTRL+1
LDSP(KTRL)=KTMP
LDMAG(KTRL)=PTLD
LDLOC(KTRL)=SL(KTMP)*(0.5-(1.0*(INT(NLPTS/2)+1.))/NPTINC)
ELSE
KLD=KLD-1
GO TO 830
ENDIF
900 CONTINUE
LDSP(KTRL)=I-1
KTMP=KTMP+1
IF (J.EQ.2) THEN
IF (KTMP.GT.0) THEN
KTRL=KTRL+1
LDSP(KTRL)=KTMP
LDMAG(KTRL)=PTLD
LDLOC(KTRL)=SL(KTMP)*(0.5-(1.0*(INT(NLPTS/2)+1.))/NPTINC)
ELSE
KLD=KLD-1
GO TO 830
ENDIF
910 CONTINUE
IF (J.EQ.2) THEN
IF (KTMP.LE.0) GO TO 820
KTRL=KTRL+1
LDSP(KTRL)=KTMP
LDMAG(KTRL)=UNILD
LDLOC(KTRL)=1
KTMP=KTMP+2
GO TO 821
820 CONTINUE
NLD=KTRL
IF (OTCD.EQ.1) CALL OUTFR2(KLD,NLD,LDSP,LDMAG,LDLOC)
CALL ANALYZE
840 CONTINUE
C PATTERNS FOR MAXIMUM NEGATIVE SUPPORT MOMENT
DO 870 I=2,NSP
DO 870 I1=1,NLPTS
DO 970 I2=1,NLPTS
KLD=KLD+1
KTRL=I
KTMPI=1
IF (KTMPI.NE.NSP) GO TO 850
KTRL=KTRL+1
LDSP(KTRL)=KTMPI
LDMAG(KTRL)=PTLD
LDLOC(KTRL)=SL(KTMPI)*(0.5-(1.0*(INT(NLPTS/2)+1.))/NPTINC)
ELSE
KLD=KLD-1
GO TO 830
ENDIF
960 CONTINUE
NLD=KTRL+2
LDSP(KTRL+I)=I-1
LDMAG(KTRL+I)=PTLD
LDLOC(KTRL+I)=SL(I-1)*(0.5-(1.0*(INT(NLPTS/2)+1.))/NPTINC)
ELSE
LDSP(KTRL+I)=I-1
LDMAG(KTRL+I)=PTLD
LDLOC(KTRL+I)=SL(I-1)*(0.5-(1.0*(INT(NLPTS/2)+1.))/NPTINC)
END IF
IF (OTCD.EQ.1) CALL OUTFR2(KLD,NLD,LDSP,LDMAG,LDLOC)
CALL ANALYZE
870 CONTINUE
890 CONTINUE
SUBROUTINE LOCATE  

SUBROUTINE LOCATE(NSP, ILD, LDSP, LDLOC, LDMAG)
DIMENSION SL(30), LDSP(30)
REAL LDLOC(30), LDMAG(30)
COMMON/BLK4/ N1, N2, NSPTR, NPSCON

DO 700 J=1, NSP
TEMLEN = 0
DO 680 I = 1, NSP
TEMLEN = TEMLEN + SL(I)
KSP = 11
IF ((LDLOC(J) .GE. TEMLEN).AND. (LDLOC(J) .LT. TEMLEN)) GO TO 690
680 CONTINUE
690 LDLOC(J) = LDLOC(J) - TEMPLEND
LDSP(J) = KSP
700 CONTINUE

IF (NPSCON.GE.1) THEN
Ni = Ni - 1
N2 = N2 - NSP
NSPTR = NSPTR - NSP
RETURN
END IF

IF (LDMAG(3).LE.LDMAG(1)) ILDM = 3
IF (LDMAG(1).LE.LDMAG(3)) ILDM = 1
IF (LDSP(2).EQ.2).AND. (LDLOC(2).EQ.0).AND. (LDSP(ILDM).EQ.1)
1 .OR. (LDSP(2).EQ.1)) THEN
NSPTR = 2
N1 = N1 - 1
N2 = N2 - 2
RETURN
END IF

IF (LDSP(2).EQ.NSP) THEN
IF ((LDSP(ILDM).EQ.NSP-1).AND. (LDLOC(2).EQ.0)) THEN
NSPTR = 3
N1 = NSPTR - N2
RETURN END IF
N3 = NSPTR - 2
RETURN
END IF

IF (LDLOC(2).EQ.0) THEN
NSPTR = 3

SUBROUTINE OUTPR2  

SUBROUTINE OUTPR2(KLD, NLD, LDSP, LDMAG, LDLOC)
DIMENSION LDSP(30)
REAL LDLOC(30), LDMAG(30)

WRITE(*, 10) 'LOAD CASE:', KLD
WRITE(*, 15) 'SPAN MAGNITUDE LOCATION'
DO 720 J = 1, NLD
WRITE(15, 730) LDSP(J), LDMAG(J), LDLOC(J)
720 CONTINUE

C
END

SUBROUTINE ANALYZE  

SUBROUTINE ANALYZE
REAL MAXPM(30), MAXPMLOC(30), MINPM(30), MINPMLOC(30), MDTM(30),
1 MAXPM(30), MAXPM2(30),
2 MAXPM(30), MAXPM2(30),
DIMENSION SL(30), FACT(30), TEMO(31), FMAT(30, 2), REACT(31), LDLOC(30),
1 PMMT(30), XLOC(30), SHEAR(30, 2), PTLD(20), PTLOC(20),
2 COMMON/BLK1/ NSP, SL, LDSP, LDLOC, LDMAG, LDSP, LDLOC, LDMAG, LDSP, LDLOC,
3 COMMON/BLK2/ MAXPM, MAXPMLOC, MINPM, MINPMLOC, MAXPM, MINPM,
4 COMMON/BLK3/ NSP, SL, LDSP, LDLOC, LDMAG, LDSP, LDLOC, LDMAG, LDSP, LDLOC,
5 COMMON/BLK4/ N1, N2, NSPTR, NPSCON
C
IF (NSP.EQ.1) GO TO 91
C
C INITIALIZE VARIABLES
DO 30 J = 1, NSPF
THETO(J) = 0
REACT(J) = 0
MOMT(J) = 0
30 CONTINUE
DO 35 J = 1, NSP
SHEAR(J, 1) = 0
SHEAR(J, 2) = 0
PMMT(J) = 0
35 CONTINUE
C
C COMPUTE SIMPLE SPAN END ROTATIONS
DO 42 J = 1, NSP
L = SL(I)
IF (L.EQ.0.0) 00 TO 42
DO 40 J = 1, NSP

E-55
IF (I.NE.LDSP(J)) GO TO 40
IF (LDLOC(J).EQ.-1) THEN
  TEMP=LDMA(J)+4*(32*EC*XIOC)
  THETO(I)=THETO(I)+TEMP
  THETO(I+1)=THETO(I+1)+TEMP
ELSE
  P=LDMA(J)
  A=LDLOC(J)
  B=L-LDLOC(J)
  THETO(I)=THETO(I)+P*A*B/(6*L*EC*XIOC)
  THETO(I+1)=THETO(I)+P*A*B/(L*B)/6*L*EC*XIOC)
ENDIF
40 CONTINUE
42 CONTINUE
C
IF (NSPTR.EQ.NSP) THEN
  COMPUTE -6 THETO MATRIX
DO 50 I=1, NRED
  THETO(I)=6*THETO(I+1)
50 CONTINUE
55 CONTINUE
C
COMPUTE SHEARS, REACTIONS AND CHECK EQUILIBRIUM
91 DO 162 J=N1, N2
  L=SL(J)
  IF (L.EQ.0) GO TO 162
  SHEARS FROM EXTERNAL LOADS
  DO 160 I=1, NLDO
    IF (J.NE.LDSP(I)) GO TO 160
    TEMP=LDMA(I)+4*(32*EC*XIOC)
    SHEAR(J,1)=SHEAR(J,1)+TEMP
    SHEAR(J,2)=SHEAR(J,2)+TEMP
  160 CONTINUE
  ELSE
    P=LDMA(I)
    A=LDLOC(I)
    B=L-LDLOC(I)
    THETO(J)=THETO(J)+P*A*B/(6*L*EC*XIOC)
    THETO(J+1)=THETO(J)+P*A*B/(L*B)/6*L*EC*XIOC)
ENDIF
END IF
160 CONTINUE
C
SHEARS FROM REDUNDANT MOMENTS
IF (J.EQ.N1) THEN
  XMT1=0
ELSE
  XMT1=MOMT(J-1)
ENDIF
IF (J.EQ.N2) THEN
  XMT2=0
ELSE
  XMT2=MOMT(J)
ENDIF
SHEAR(J,1)=SHEAR(J,1)+(XMT2-XMT1)/L
SHEAR(J,2)=SHEAR(J,2)+(XMT2-XMT1)/L
162 CONTINUE
C
MODIFY THETO MATRIX TO OBTAIN REDUNDANT MOMENTS
DO 90 I=NRED-1, 1, -1
  MOMT(I)=THETO(I)+FACT(I)*THETO(I-1)
90 CONTINUE
C
BACK SUBSTITUTE TO OBTAIN REDUNDANT MOMENTS
DO 95 I=1, NRED
  MOMT(I)=THETO(I)-FACT(I)*THETO(I-1)
95 CONTINUE
C
MODIFY SHEARS TO IMPROVE CONVERGENCE
DO 190 I1=1, NLD
  PTLD(I1)=0
  PTLOC(I1)=0
190 CONTINUE
DO 200 J1=NLDO
  IF (I.NE.LDSP(J)) GO TO 200
  IF (LDLOC(U).EQ.-1) THEN
    UN[I]=UN[I]+LDMA(J)
  ELSE
    KTR=KTR+1
  ENDIF
200 CONTINUE
166 CONTINUE
DO 168 I=1, NLD
  IF (LDLOC(I).EQ.-1) THEN
    TLOAD=TLOAD+LDMA(I)*SL(LDSP(I))
  ELSE
    TLOAD=TLOAD+LDMA(I)
  ENDIF
168 CONTINUE
IF (TREACT-TLOAD.OT.O.1) WRITE(*,170) KLO
170 FORMAT(5X, '*** EQUILIBRIUM NOT SATISFIED FOR LOADCASE:',1:3,
1 '***',//)
C
END
PTLD(KTR)=LDMAG(J)
PTLOC(KTR)=LDLOC(J)
ENDIF
200 CONTINUE
C
IF (I.EQ.N1) THEN
XMT=0
ELSE
XMT=MOMT(I-1)
ENDIF
IF (I.EQ.N2) THEN
XMT2=MOMT(I)
ENDIF
SPAN NOT LOADED OR END SHEARS OF SAME SIGN
A=SIGN(1.0,SHEAR(I,1))
B=SIGN(1.0,SHEAR(I,2))
IF (((UNILD.EQ.0).AND.(KTR.EQ.0)).OR.(A.EQ.B)) THEN
PMOMT(I)=(XMT+XMT2)/2.
XMLOC(I)=SL(I)/2.
GO TO 270
ENDIF
C
UNIFORM LOAD ONLY
IF (((UNILD.NE.0).AND.(KTR.EQ.0)) THEN
XMLOC(I)=SHEAR(I,1)/UNILD
PMOMT(I)=SHEAR(I,1)*XMLOC(I)-UNILD*XMLOC(I)**2/2*XMT1
ENDIF
C
POINT LOAD(S) ONLY
ELSE IF (((UNILD.EQ.0).AND.(KTR.EQ.1)) THEN
XMT=0
GO TO 220
ENDIF
210 CONTINUE
PMT(I)=SHEAR(I,1)*XMLOC(I)*XMT1
DO 230 I=1,KTRST
PMOMT(I)=PMOMT(I)-PTLD(I)*(XMLOC(I)-PTLOC(I))
230 CONTINUE
C
UNIFORM LOAD AND POINT LOAD(S)
ELSE IF (((UNILD.EQ.0).AND.(KTR.EQ.1)) THEN
TEMP=SHEAR(I,1)
DO 240 I=1,KTR
TEMP=TEMP-PTLD(I)
IF (SIGN(1.0,TEMP).NE.SIGN(1.0,TEMP)) THEN
XSTART=XMT1
KTRST=I1
GO TO 250
ENDIF
TEMP1=TEMP
TEMP=TEMP-PTLD(I)
IF (SIGN(1.0,TEMP1).NE.SIGN(1.0,TEMP)) THEN
XSTART=PTLOC(I-1)
ENDIF
IF (I.EQ.KTR) THEN
XDIST=SL(I)-XSTART
ELSE
XDIST=PTLOC(I)-XSTART
ENDIF
TEMP=TEMP-UNILD*XDIST
IF (SIGN(1.0,TEMP).NE.SIGN(1.0,TEMP)) THEN
XMLOC(I)=XSTART+TEMP/UNILD
KTRST=I1
GO TO 250
ENDIF
TEMP=TEMP-PTLD(I)
IF (SIGN(1.0,TEMP).NE.SIGN(1.0,TEMP)) THEN
XMLOC(I)=PTLOC(I-1)
KTRST=I1
GO TO 250
ENDIF
240 CONTINUE
250 PMOMT(I)=SHEAR(I,1)*XMLOC(I)-UNILD*XMLOC(I)**2/2*XMT1
IF (KTRST.EQ.0) GO TO 265
DO 260 I=1,KTRST
PMOMT(I)=PMOMT(I)-PTLD(I)*(XMLOC(I)-PTLOC(I))
260 CONTINUE
265 ENDIF
270 CONTINUE
C
UNIFORM LOAD ONLY
IF (I.EQ.1) THEN
I=1
ELSE
I=PTLOC(I-1)
ENDIF
IF (I.EQ.N1) THEN
GO TO 250
ENDIF
IF (I.EQ.N2) THEN
GO TO 250
ENDIF
C
OUTPUT RESULTS
IF (OTCD.EQ.1).OR.(KLD.EQ.0)) THEN
IF ((KLD.EQ.0) WRITE(*,450) KLD
ELSE
WRITE(*,454) WDL
ENDIF
E-59
ELSE
  XMT=MOMT(I-1)
ENDIF
WRITE(*,480) I,REACT(I),XMT
WRITE(*,490) I,SL(I),SHEAR(1),SHEAR(2),PMOMT(I),
  XMLOC(I)
430 CONTINUE
WRITE(*,480) N2+1,REACT(N2+1),0.0
ENDIF
C 450 FORMAT(5X, '***** LOADCASE ', '(13, ****' )
45A FORMAT(5X, '***** ADDITIONAL DEAD LOAD: ', 'F6.2, *** ***' )
460 FORMAT(5X, 'SPAN', '2X', 'SPT', '2X', 'MAX SPAN', '2X', 'LOCATION', /
  1 5X, 'RIGHT', '3X', 'SUPPORT', '2X', 'MAX SPAN', '2X', 'LOCATION', /
  2 15X, 'LENGTH', '5X', 'SHEAR', '5X', 'SHEAR', '4X', 'MOMENT', '4X', /
  3 'MOMENT', '19X', 'FT', '7X', 'KIP', '7X', 'KIP', '7X', 'KIP', '4X', '
  4 'FT-KIP', '8X', 'FT', '/')
480 FORMAT(8X, 'CALCULATED EXTREME SHEARS AND MOMENTS FOR LL.' )
C WRITE(*,510)
490 FORMAT(2X, 'CALCULATED EXTREME SHEARS AND MOMENTS FOR LL.' )
C RETURN
ENDIF
C SUBROUTINE OUTPR1 ****************************
C Output Extreme Values for Live Load Only or
C Live Load Multiplied By Appropriate Impact Factor.
C REAL MAXPM(30), MAXLOC(30), MINPM(30), MINLOC(30), MAXNM(30), MINNM(30),
C DIMENSION SL(30)
C COMMON/BLK1/ NSP, SL, GS, WDL, XIQC, EC, OTCD, NSPT, NRED, NIMP
C COMMON/BLK2/ MAXSHR, MAXPM, MAXLOC, MINPM, MINLOC, MAXNM,
C 1 MINNM, S1, S2, MAXPM1, MAXPM2
C WRITE(*,*)
C IF (NIMP.EQ.0) WRITE(*,500)
C IF (NIMP.EQ.1) WRITE(*,505)
C WRITE(*,510)
C DO 495 I=1,NSP
C IF (NIMP.EQ.0) THEN
C 1XMPN=1.+50./(SL(I-1)+SL(I))/2.+125.)
C XIMPP=1.+50./(SL(I)+125.)
C END IF
C IF (NIMP.EQ.0) THEN
C XIMPP=1.
C XMPN=1.
C END IF
C IF (I.EQ.1) THEN
C XMT=0
C XMT=0
C ELSE
C XMT=MAXNM(I-1)*XIMPN
C XMT=MINNM(I-1)*XIMPP
C ENDIF
C SHR=MAXSHR(I)*XIMPP
C SHR=2*MAXSHR(I)*XIMPP
C WRITE(*,540) I, XMT, XMT1
C WRITE(*,545) 1, SHR, SHR2, MAXPM(I)*XIMPP, MAXLOC(I)
C 495 CONTINUE
C WRITE(*,540) NSPT, 0.0, 0.0
C WRITE(*,515)
APPENDIX F

DESIGN EXAMPLES

Two design examples are presented in this Appendix. Calculations for service and strength design are performed according to procedures outlined in Chapter Three. These design examples are intended to illustrate application of results of this project to bridge design. They do not necessarily set out all the conditions which may need to be considered by the designer, but are presented as a guide to proposed design procedures.

DESIGN EXAMPLE 1

This design example is for an interior girder of a bridge with four equal 100-ft spans as shown in Fig. F-1. The girder type is chosen to be AASHTO Type IV with girder spacing equal to 8 ft. Design criteria are listed below:

Material Properties:

Girder Concrete (Normal weight: 150 pcf)
- $f'_{c1}$ (at transfer) = 5000 psi
- $f'_{c}$ (at 28 days) = 6500 psi
- $\lambda_{c}$ (Creep Coefficient) = 2.70
- $\varepsilon_{s/u}$ (Shrinkage) = 600 millionths

Deck and Diaphragm Concrete (Normal weight: 150 pcf)
- $f'_{c}$ (at 28 days) = 4500 psi
- $\varepsilon_{s/u}$ (Shrinkage) = 600 millionths

*Time-dependent concrete properties may be determined either from testing of the specific concrete mixes to be used in construction or from coefficients determined using ACI-209 Recommendations (17).

Fig. F-1 Four Span Bridge for Design Example 1
Prestressing Strand:
1/2" \phi, 270 ksi, Area = 0.153 in.²
Stress-Relieved
Initial Strand Tension = 189,000 psi

Loading:
25 psf uniform load for wearing surface, parapet, etc.
AASHTO HS 20-44 live load

Construction Schedule:
As an example, based on expected construction schedule, it is estimated that the continuity could be established by casting the diaphragms and deck during a period ranging from 17 to 67 days after prestress transfer. Live load could be applied at the earliest 30 days after casting deck and diaphragm. Therefore:
- For determination of maximum positive design moments within the spans, use 17 day age at continuity combined with application of live load at 1800 days (5 years).
- For determination of maximum negative design moments at the supports, use 67 day age at continuity combined with application of live load at the earliest 30 days after establishment of continuity. Live load should be applied at the time maximum negative restraint moment occurs, as determined from the time-dependent analysis using BRIDGERM.

Preliminary Design
A preliminary design was done disregarding restraint moments. Simple span moments were used for girder plus deck dead load. Full continuity was assumed for determination of live load plus impact and additional dead load moments. This step is not documented here. Details of results of the preliminary design are given below:

Deck thickness: 7.5 in.

Section properties:

<table>
<thead>
<tr>
<th></th>
<th>Girder</th>
<th>Composite*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area</td>
<td>789 in.²</td>
<td>1,388 in.²</td>
</tr>
<tr>
<td>( \bar{Y} )</td>
<td>24.73 in.</td>
<td>38.98 in.</td>
</tr>
<tr>
<td>ST</td>
<td>8,909 in.³</td>
<td>42,269 in.³</td>
</tr>
<tr>
<td>SB</td>
<td>10,542 in.³</td>
<td>16,282 in.³</td>
</tr>
<tr>
<td>I</td>
<td>260,741 in.⁴</td>
<td>634,741 in.⁴</td>
</tr>
</tbody>
</table>

*Properties for girder plus deck transformed by the modular ratio of deck and girder concretes.

Prestressing Strand:
38 strands in four rows
<table>
<thead>
<tr>
<th>No. of Strands</th>
<th>Centroid from Bottom</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>8.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>6.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>4.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>2.0 in.</td>
</tr>
</tbody>
</table>

30 Straight Strands: at 4.00 in.
8 Draped Strands: at 5.0 in. (midspan)
               at 49.0 in. (girder ends)
Hold-down Points at 40 and 60 ft

Service Moments in ft-kips:
Deck plus girder dead load moments are for the simply supported structure. Additional dead load moments are for the fully continuous structure. Live load plus impact moments are computed for the structure continuous for negative moment only using Program BRIDGELL.

<table>
<thead>
<tr>
<th></th>
<th>Support A</th>
<th>Midspan</th>
<th>Support B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deck plus Girder DL</td>
<td>0</td>
<td>1965</td>
<td>0</td>
</tr>
<tr>
<td>Additional DL</td>
<td>0</td>
<td>154</td>
<td>-214</td>
</tr>
<tr>
<td>LL+I*</td>
<td>0</td>
<td>1095</td>
<td>-554</td>
</tr>
</tbody>
</table>
Design for Positive Midspan Moments

Using results of the preliminary design, time-dependent restraint moments are calculated for the fully continuous structure using BRIDGERM. For 17 day continuity and assuming no uplift, the following moments (ft-kip) are obtained. Restraint moment at B is obtained by multiplying restraint moment at C (RMII from BRIDGERM) by 1.5 to give restraint moment at the first interior support. The factor 1.5 is related to the relative stiffness of end and interior spans. This factor is to be used to determine end span restraint moments when uplift cannot occur as discussed on page E-17 of Appendix E of this report.

<table>
<thead>
<tr>
<th>Support</th>
<th>B*</th>
<th>C*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deck plus Girder DL</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Additional DL</td>
<td>-214</td>
<td>-143</td>
</tr>
<tr>
<td>LL+I*</td>
<td>-456</td>
<td>-470</td>
</tr>
</tbody>
</table>

*For loadcase producing maximum positive moment in given span.

Restraint Moment at 1800 days

Support B* | 629 ft-kip
Support C* | 419 ft-kip

Although reinforcement need not be provided to resist the positive restraint moments, the rotations and cracks opening at the ends of the girder from time-dependent deformations have the same effect on the resultant midspan moment as if the positive reinforcement had been present. This behavior is illustrated in Fig. 22 of this report.

The negative cracking moment is calculated next:

\[ M_{Cr}^- = I_c \times 7.5 \times \sqrt{F_{cd}/\gamma_T} \]

\[ = 634,741 \times 7.5 \times \sqrt{5400/(54 + 7.5 - 38.98)/12,000} \]

\[ = 1182 \text{ ft-kip} \]

\[ 1.2 \times M_{Cr}^- = 1418 \text{ ft-kip} \]

Service Moments - Trial 1

1. End Span
   a. Continuity Moments
      Support B
      Additional DL | -214 ft-kip
      LL+I | -554 ft-kip
      Restraint | 629 ft-kip
      -139 ft-kip
   b. Girder Midspan Moments
      Deck plus Girder DL | 1965 ft-kip (girder section only)
      Additional DL | 154 ft-kip
      LL+I | 1095 ft-kip
      Restraint | 315 ft-kip
      1564 ft-kip (composite section)

   Negative service moment is less than 125% of \( M_{Cr}^- \). Midspan service moment from full continuity is increased by \( 1/2 \times 629 = 315 \text{ ft-kip} \) to obtain time-dependent service moment.

2. Interior Span
   a. Continuity Moments
      Support B
      Additional DL | -214 ft-kip
      LL+I | -456 ft-kip
      Restraint | 629 ft-kip
      -41 ft-kip
   b. Girder Midspan Moments
      Deck plus Girder DL | 1965 ft-kip (girder section)

   Negative service moments at Supports B and C are less than 125% of \( M_{Cr}^- \). Midspan service moment from full continuity is increased by \( (629 + 419)/2 = 524 \text{ ft-kip} \) to obtain time-dependent service moment.
Addition DL 73 ft-kip
LL+I 892 ft-kip
Restraint 524 ft-kip
1489 ft-kip (composite section)

3. Check service stresses after losses have occurred for end span.

At 1800 days, prestress is 145,000 psi (from BRIDGERM).

\[ F_{pe} = 38 \times 0.153 \times 145,000 = 843,000 \text{ lb} \]

\[ e = 24.73 - (30 \times 4.00 + 8 \times 5.00)/38 = 20.52 \text{ in.} \]

Bottom Stress for Midspan Moment in End Span:

\[ f_B = \frac{843,000 + 843,000 \times 20.52}{10,542} - \frac{1,965 \times 12,000}{10,542} - \frac{1,564 \times 12,000}{16,282} = -680 \text{ psi} \]

Allowable tension = \( 6 \sqrt{f_c} \)

\[ = 6 \sqrt{6500} = 484 \text{ psi} \]

Bottom tension is greater than allowable.

Trial 2

More prestress force is required to reduce bottom tension under service moments. Therefore, add six strands to Row 4.

<table>
<thead>
<tr>
<th>No. Strands</th>
<th>Centroid</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>0.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>6.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>4.0 in.</td>
</tr>
<tr>
<td>12</td>
<td>2.0 in.</td>
</tr>
</tbody>
</table>

36 Straight Strands: at \((30 \times 4 + 6 \times 8)/36 = 4.67 \text{ in.}\)

8 Draped Strands: at 5.0 in. (midspan)

at 49.0 in. (girder ends)

Recheck Initial Stresses:

Initial Strand Stress = 167,000 psi (from BRIDGERM)

\[ F_{pl} = 44 \times 0.153 \times 167,000 = 1,124,000 \text{ lb} \]

For Midspan Stresses:

\[ M_{DL} \text{ (girder only)} = \frac{789/144}{0.150 \times 100^2/8} = 1028 \text{ ft-kip} \]

\[ e = 24.73 - (36 \times 4.67 + 8 \times 5.00)/44 = 20.00 \text{ in.} \]

Bottom Stress:

\[ f_B = \frac{1,124,000 + 1,124,000 \times 20.00}{10,542} - \frac{1,028 \times 12,000}{10,542} = 2387 \text{ psi} \]

Allowable Compression = \( 0.6 f_c \)

\[ = 0.6 \times 5000 = 3000 \text{ psi} \]

\( F_{pl} > F_{pl} \) OK

Top Stress:

\[ f_T = \frac{1,124,000 + 1,124,000 \times 12.00}{8,909} = 286 \text{ psi} \]

\( F_{pl} \) OK

For End Stresses:

\[ e = 24.73 - (36 \times 4.67 + 8 \times 49.0)/44 = 12.00 \text{ in.} \]

*Note: These computations conservatively assume transfer length is zero.

Bottom Stress:

\[ f_B = \frac{1,124,000 + 1,124,000 \times 12.00}{10,542} = 2704 \text{ psi} \]

\( < 3000 \text{ psi} \) OK

Top Stress:

\[ f_T = \frac{1,124,000 + 1,124,000 \times 12.00}{8,909} = -89 \text{ psi} \]
 Allowable Tension = \(-7.5 \sqrt{f'_{ct}}\)  
\(= -7.5 \times \sqrt{5000}\)  
\(= -530 \text{ psi}\) OK

Repeat run of BRIDGERM with new strand configuration gives following restraint moments at 1800 days:

<table>
<thead>
<tr>
<th>Support</th>
<th>Moment</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>1005 ft-kip</td>
</tr>
<tr>
<td>C</td>
<td>670 ft-kip</td>
</tr>
</tbody>
</table>

**Service Moments - Trial 2**

1. **End Span**
   a. **Continuity Moments**
      - Additional DL  -214 ft-kip
      - LL+I  -554 ft-kip
      - Restraint 1005 ft-kip
   b. **Girder Midspan Moments**
      (Same as End Span)

2. **Interior Span**
   a. **Continuity Moments**
      - Support B
   b. **Girder Midspan Moments**
      (Same as End Span)

The positive resultant moments at Supports B and C indicate that time-dependent effects reduce the effective continuity for service load to zero (the cracks at the bottom of the diaphragms will remain open under 100% of service load). Therefore, the interior girder will also behave as a simply-supported girder under service load.

3. **Check midspan service stresses after losses.**

At 1800 days, prestress is 141,000 psi (from BRIDGERM).

\[ F_{pe} = 44 \times 0.153 \times 141,000 \]
\[ = 949,200 \text{ lb} \]
\[ e = 24.73 - (36 \times 4.67 + 8 \times 5.00) / 44 \]
\[ = 20.00 \text{ in.} \]

**Bottom Stress:**

\[ f_B = \frac{949,200}{789} + \frac{949,200 \times 20.00}{10,542} - \frac{1,965 \times 12,000}{10,542} - \frac{1,604 \times 12,000}{16,282} \]
\[ = -415 \text{ psi (tension)} < -484 \text{ psi OK} \]

**Top Stress (girder):**

\[ f_{T,g} = \frac{949,200}{789} + \frac{949,200 \times 20.00}{8,909} + \frac{1,965 \times 12,000}{8,909} + \frac{1,604 \times 12,000}{42,269} \]
\[ = 2174 \text{ psi (compression)} \]

Allowable compression = 0.4 \times f'_{ct} (AASHTO 9.15.2.2)
\[ = 0.4 \times 6500 \]
\[ = 2600 \text{ psi} > f_{T,g} \text{ OK} \]
Top Stress (deck):

\[ f_{T,d} = \frac{1,604 \times 12,000}{28,186} = 683 \text{ psi (compression)} \]

Allowable compression = 0.4 \times f'_c \quad \text{(AASHTO 9.15.2.2)}

\[ = 0.4 \times 4500 = 1800 \text{ psi} > f_{T,d} \quad \text{OK} \]

Design is OK for Midspan Service Moments

Flexural Strength

Required Strength at Midspan: Using LL+1 Moments from BRIDGELL for full continuity.

End Span:

\[ M_u = 1.3 \times (1965 + 154 + 1.67 \times 1095) = 5132 \text{ ft-kip} \]

Interior Span:

\[ M_u = 1.3 \times (1965 + 73 + 1.67 \times 892) = 4586 \text{ ft-kip} \]

End span governs, assuming one prestress design applies for all spans.

Provided Strength:

\[ f^*_{su} = f'_c (1 - 0.5 \times \frac{p^*}{f'_c}) \quad \text{(AASHTO 9.17.4)} \]

\[ p^* = 44 \times \frac{.153}{(96 \times 56.77)} = 0.00124 \]

\[ b = 8 \times 12 = 96 \text{ in.} \]

\[ d = 54 - (36 \times 4.67 + 8 \times 5.0)/44 + 7.5 = 56.77 \text{ in.} \]

\[ f'_c = 4500 \text{ psi} \Rightarrow 4.5 \text{ ksi for deck} \]

\[ f'_s = 270 \text{ ksi} \]

\[ f^*_{su} = 270 \left(1 - 0.5 \times \frac{0.00124}{270}ight) = 260 \text{ ksi} \]

For rectangular section:

\[ \phi M_n = \phi A_f^* f^* d (1 - 0.6 \times \frac{p^*}{f'_c}) \]

\[ = 1.0 \times 6.73 \times 260 \times 56.77 \times \frac{(1 - 0.6 \times 0.00124 \times 260/4.5)/12}{7922 \text{ ft-kip} > 5132 \text{ ft-kip}} \]

\[ \phi = 1.0 \text{ for factory produced girder} \quad \text{(AASHTO 9.14)} \]

Check depth of compression zone, a:

\[ a = A_f^* f^* / 0.85 f'_c \]

\[ = 6.73 \times 260 / 0.85 \times 4.5 \times 96 = 4.77 \text{ in.} < 7.5 \text{ in.} \quad \text{(Neutral Axis is in the Deck)} \]

Check Maxi mum Steel:

\[ \text{Reinforcement Index} = \frac{p^* f^*_c}{f'_c} \leq 0.3 \]

\[ = 0.00124 \times 260/4.5 = 0.072 \leq 0.3 \quad \text{OK} \]

Check Minimum Steel:

\[ \phi M_n \geq 1.2 \frac{M_{cr}^*}{M_{cr}} \]

\[ M_{cr}^* = (f_{cr} + F_{se} + \frac{F_{se} x e}{A_g}) \frac{S_B - M_{DL}(S_{B_c} - 1)}{S_{B_c}} \]

\[ f_{cr} = 7.5 \sqrt{6500/1000} = 0.605 \text{ ksl} \]

\[ F_{se} = 949.2 \text{ kips.} \]

\[ M_{DL} = 1,965 \text{ ft-kip} \]

\[ S_B = 10,542 \text{ in.}^3 \]

\[ S_{B_c} = 16,282 \text{ in.}^3 \]

\[ \phi M_n \geq 1.2 \frac{M_{cr}^*}{M_{cr}} \]
Design for Negative Support Moments

Using resulting girder section from the design for positive midspan moment, time-dependent restraint moments are calculated for the fully continuous structure using BRIDGERM. For 67 day continuity and assuming no uplift, the following restraint moments (ft-kip) are obtained. Restraint moment at B is obtained by multiplying restraint moment at C (RMII from BRIDGERM) by 1.5 to give restraint moment at the first interior support. The factor 1.5 is related to the relative stiffness of end and interior spans. This factor is to be used to determine end span restraint moments when uplift cannot occur as discussed on page E-17 of Appendix E of this report.

<table>
<thead>
<tr>
<th>Support</th>
<th>B (109 days)</th>
<th>C</th>
<th>1800 days</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maximum Negative</td>
<td>-1245</td>
<td>-830</td>
<td>-483</td>
<td>-322</td>
<td></td>
</tr>
</tbody>
</table>

From BRIDGE analysis, the following support moments (ft-kip) were obtained:

<table>
<thead>
<tr>
<th>Support</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>Additional Dead Load</td>
<td>-214</td>
<td>-143</td>
</tr>
<tr>
<td>Maximum LL+I*</td>
<td>-976</td>
<td>-884</td>
</tr>
</tbody>
</table>

*For loadcases producing maximum negative moments.

Service Moments

Support B:

- Additional DL -214 ft-kip

Support C:

- Additional DL -143 ft-kip
- LL+I -884 ft-kip
- Restraint (Maximum) -830 ft-kip

An area of reinforcement must be determined to limit service load stresses to below allowable:

- Compression: $0.6 \times f'_c$ (Current AASHTO 9.7.2.4)
- Tension: 24,000 psi for Grade 60 (AASHTO 8.15.2.2)

Try maximum reinforcement $= 0.5 \rho_b$ (New Requirement)

\[
\rho_b = \frac{0.85 f'_c (A_f + (x_b - h_f) t_w)}{f_y bd} \\

\begin{align*}
\beta_1 &= 0.85 - 2.5 \times 0.05 \quad \text{for } f'_c = 6500 \text{ psi} \\
&= 0.725 \\

x_b &= 24.78 \text{ in.} \\

\rho_b &= \frac{0.85 \times 6.5 \times (26 \times 8 + 2.25 \times 9 + (24.78 - 17) \times 8)}{60 \times 26 \times 57.75} \\
&= 0.0260 \\

0.5 \rho_b &= 0.0130 \\
A_{st}, \text{ max} &= 0.0130 \times 26 \times 57.75 \\
&= 19.5 \text{ in.}^2 
\]
Calculate cracked section moment of inertia with 19.5 in.² deck reinforcement.

\[ n_{A_{st}} = 6.3 \times 19.5 \]
\[ = 122.85 \text{ in.}^2 \]

Assume neutral axis in web.

\[ 122.85 (57.75 - x) = \frac{8}{2} (x - 8)^2 + 26 \times 8 (x - 4) + 9^2 (x - 11) \]
\[ x = 20.01 \text{ in.} > 9 + 8 = 17 \text{ in.} \quad \text{Neutral Axis Is In Web} \]

\[ I_{cr} = 122.85 (57.75 - 20.01)^2 + \frac{1}{3} x 8 x (20.01 - 8)^3 \]
\[ + \frac{1}{12} x 26 x 8^3 + 26 \times 8 (20.01 - 4)^2 \]
\[ + 2 \times 9^4/36 + 9^2 (20.01 - 11)^2 \]
\[ = 240,959.7 \text{ in.}^4 \]

\[ S_{cr,C} = I_{cr}/x = 240,959.7/20.01 \]
\[ = 12,042 \text{ in.}^3 \]

\[ S_{cr,T} = I_{cr}/(d - x) \]
\[ = 240,959.7/(57.75 - 20.01) \]
\[ = 6385 \text{ in.}^3 \]

Check Concrete Stress*:

At 109 days, \( f_{pe} = 148,000 \text{ psi} \) (from BRIDGER)

\[ F_{se} = 44 \times 0.153 \times 148,000 \]
\[ = 996,300 \text{ lb} \]

\[ f_b = \frac{996,300}{789} + \frac{996,300}{10,542} \times 12,000 + \frac{2,435 \times 12,000}{12,042} \]
\[ = 4823 \text{ psi} > 6 f_c = 3900 \text{ psi} \quad \text{exceeds limit} \]

*Note: These computations conservatively assume transfer length is zero.

Check Steel Stress:

\[ f_s = 6.3 \times 2,435 \times 12,000/6,385 \]
\[ = 28,800 \text{ psi} > 24,000 \text{ psi} \quad \text{exceeds limit} \]

Therefore, for this section, span, spacing, and timing combination, negative service moments are excessive. In this situation, transverse deck cracking is likely. The bridge configuration must be adjusted to reduce these high negative moments. If this combination had been satisfactory, the calculation would have been continued to check reinforcement stress range limits of AASHTO 8.16.8.3 and check strength design criteria. See Example 2 in this Appendix for sample strength calculations.

A span of 100 ft with a girder spacing of 8 ft is near the upper limit for which an AASHTO Type IV girder might be used. The bridge was redesigned with girder spacing of six feet and all other parameters identical. With the smaller girder spacing, the negative service moment is reduced. Further calculations showed that the allowable stresses for concrete compression and reinforcement tension under maximum negative service moment could be satisfied with a reinforcement ratio less than 0.5 \( P_b \). Also, the stress range from application of maximum live load plus impact moment is within the permissible stress range of AASHTO 8.16.8.3. Although the resulting design meets current and proposed specifications, a large amount of deck reinforcement, approximately 18 sq in. over each girder, is required. This may be an impractical design. Therefore, a further trial with a deeper girder section may be needed to improve the design.
DESIGN EXAMPLE 2

This design example is for an interior girder of a bridge with four spans of 90, 110, 110, and 90 ft. as shown in Fig. F-2. The girder type is chosen to be BT72/6 (cross-section shown in Fig. 17 of the report) with girder spacing equal to 6 ft. Design criteria are listed below:

Material Properties:
- Girder Concrete (Normal weight: 150 pcf)
  - $f'_{ct}$ (at transfer) 5000 psf
  - $f'_{c}$ (at 28 days) 6500 psf
  - $v$ (Creep Coefficient) 2.85
  - $(e_s)v$ (Shrinkage) 550 millionths
- Deck and Diaphragm Concrete (Normal weight: 150 pcf)
  - $f'_{c}$ (at 28 days) 3500 psf
  - $(e_s)v$ (Shrinkage) 550 millionths

*Time-dependent concrete properties may be determined either from testing of the specific concrete mixes to be used in construction or from coefficients determined using ACI-209 Recommendations (11).

Prestressing Strand
- 1/2" @, 270 ksi, Area = 0.153 in.$^2$
- Low-Relaxation
- Initial Strand Tension 189,000 psi

Loading:
- 20 psf uniform load for wearing surface, parapet, etc.
- AASHTO HS 20-44 live load

Construction Schedule:
As an example, based on expected construction schedule, it is
estimated that the continuity could be established by casting the
diaphragms and deck during period ranging from 15 to 40 days after
prestress transfer. Live load could be applied at the earliest 30
days after casting deck and diaphragm. Therefore:
- For determination of maximum positive design moments within
  the spans, use 15 day age at continuity combined with
  application of live load at 1800 days (5 years).
- For determination of maximum negative design moments at the
  supports, use 40 day age at continuity combined with
  application of live load at the earliest 30 days after
  establishment of continuity. Live load should be applied at
  the time maximum negative restraint moment occurs, as
determined from the time-dependent analysis using BRIDGERM.

Preliminary Design

A preliminary design was done disregarding restraint moments.
Simple span moments were used for girder plus deck dead load. Full
continuity was assumed for determination of live load plus impact and
additional dead load moments. This step is not documented here.
Details of results of the preliminary design are given below:

Deck thickness: 7.0 in.

Section properties:

<table>
<thead>
<tr>
<th>Property</th>
<th>Girder</th>
<th>Composite*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Area</td>
<td>701 in.²</td>
<td>1,071 in.²</td>
</tr>
<tr>
<td>$\bar{y}_b$</td>
<td>36.36 in.</td>
<td>49.87 in.</td>
</tr>
</tbody>
</table>
| ST        | 13,606 in.³  | 30,756 in.³ (girder),
            | 29,436 in.³ (deck) |
| SB        | 13,340 in.³  | 17,193 in.³       |
| I         | 484,993 in.⁴ | 857,484 in.⁴      |

Prestressing Strand:

End Span (90 ft):
- 18 strands in two rows
  - No. of Strands 8 4.0 in.
  - Centroid from Bottom 10 2.0 in.
  - 16 Straight Strands at 3.00 in.
  - 2 Draped Strands at 70.0 in. (girder ends)
  - Hold-down Points at 27 and 63 ft

Interior Span (110 ft):
- 20 Strands in two rows
  - No. of Strands 10 4.0 in.
  - Centroid from Bottom 10 2.0 in.
  - 16 Straight Strands at 3.00 in.
  - 4 Draped Strands at 69.0 in. (girder ends)
  - Hold-down Points at 44 and 66 ft

Service Moments in ft-kips:

Deck plus girder dead load moments are for the simply supported
structure. Additional dead load moments are for the fully continuous
structure. Live load plus impact moments are computed for the
structure continuous for negative moment only using Program BRIDGELL.

<table>
<thead>
<tr>
<th>End Span</th>
<th>Support A</th>
<th>Midspan</th>
<th>Support B</th>
</tr>
</thead>
<tbody>
<tr>
<td>Deck plus Girder DL</td>
<td>0</td>
<td>1271</td>
<td>0</td>
</tr>
<tr>
<td>Additional DL</td>
<td>0</td>
<td>68</td>
<td>-121</td>
</tr>
<tr>
<td>LL+I*</td>
<td>0</td>
<td>744</td>
<td>-339</td>
</tr>
</tbody>
</table>

*Properties for girder plus deck transformed by the modular ratio of deck and girder concretes.
Design for Positive Midspan Moments

Using results of the preliminary design, time-dependent restraint moments are calculated for the fully continuous structure using BRIDGERM. Restraint moment at B is obtained by analyzing a 90-ft span and using 1.5 times restraint moment RMII for the first interior support. Restraint moment at C is obtained by multiplying restraint moment at C (RMII from BRIDGERM) by 1.5 to give restraint moment at the first interior support. The factor 1.5 is related to the relative stiffnesses of end and interior spans. This factor is to be used to determine end span restraint moments when uplift cannot occur as discussed on Page E-17 of Appendix E of this report. Restraint moment at C is obtained by analyzing a 110-ft span and using restraint moment RMII for the central support. For 15 day continuity and assuming no uplift, the following moments (ft-kip) are obtained.

Support B*  Support C*

<table>
<thead>
<tr>
<th>Moment</th>
<th>Support B*</th>
<th>Support C*</th>
</tr>
</thead>
<tbody>
<tr>
<td>Restraint Moment at 1800 days</td>
<td>792</td>
<td>214</td>
</tr>
</tbody>
</table>

*Although reinforcement need not be provided to resist the positive restraint moments, the rotations and cracks opening at the ends of the girder from time-dependent deformations have the same effect on the resultant midspan moment as if the positive reinforcement had been present. This behavior is illustrated in Fig. 22 of this report.

The negative cracking moment is calculated next:

\[ M_{cr} = \frac{I_c \times 7.5 \sqrt{F_{cd}}}{w_T} \]

\[ = 857,484 \times 7.5 \times \sqrt{3,500/(72 + 7.0 - 49.87)/12,000} \]

\[ = 1088 \text{ ft-kip} \]

The positive resultant moment at Support B indicates that time-dependent effects reduce the effective continuity for service load to zero (the crack at the bottom of the diaphragm will remain open under 100% of service load). Therefore, the girder will behave as simply-supported at Support B under service load. The midspan service moments for the end girder are the simple-span moments.

The positive resultant moment at Support C is less than 125% of \( M_{cr} \). The positive resultant moment at Support B indicates that time-dependent...
effects reduce the effective continuity for service load to zero at Support B (the cracks at the bottom of the diaphragms will remain open under 100% of service load). Therefore, the design moments for the interior span will consist of the simple span moments for additional dead load and live load plus impact reduced by 274/2 = 137 ft-kip to account for remaining continuity at Support C.

b. Girder Midspan Moments

Deck plus Girder DL
Additional DL
LL+I
Restraint

1899 ft-kip (girder section)
182 ft-kip
1128 ft-kip
-137 ft-kip

1173 ft-kip (composite section)

3. Check service stresses after losses have occurred.

a. End Span

At 1800 days, prestress is 158,000 psi (from BRIDGERM).

\[ F_{pe} = 18 \times 0.153 \times 158,000 \]
\[ = 435,000 \text{ lb} \]
\[ e = 36.36 - \frac{(16 \times 3.00 + 2 \times 2.00)}{18} \]
\[ = 33.47 \text{ in.} \]

Bottom Stress for Midspan Moment in End Span:

\[ M_B = \frac{435,000 \times 33.47 - 1,271 \times 12,000 - 1,026 \times 12,000}{701 \times 13,340} \]
\[ = -147 \text{ psi (tension)} \]

Allowable tension = \(-6 \sqrt{f_c^*}\) (AASHTO 9.15.2.2)
\[ = -6 \sqrt{6500} \]
\[ = -484 \text{ psi} \]

Top Stress (girder):

\[ f_{T,g} = \frac{435,000 \times 33.47 + 1,271 \times 12,000 + 1,026 \times 12,000}{701 \times 13,606} \]
\[ = 989 \text{ psi (compression)} \]

b. Interior Span

At 1800 days, prestress is 161,000 psi (from BRIDGERM).

\[ F_{pe} = 20 \times 0.153 \times 161,000 \]
\[ = 492,700 \text{ lb} \]
\[ e = 36.36 - 3.00 \]
\[ = 33.36 \text{ in.} \]

Bottom Stress for Midspan Moment in Interior Span:

\[ M_B = \frac{492,700 \times 33.36 - 1,271 \times 12,000 - 1,173 \times 12,000}{701 \times 13,340} \]
\[ = -27 \text{ psi (tension)} \leq -484 \text{ psi} \]

Top Stress (girder):

\[ f_{T,g} = \frac{492,700 \times 33.36 + 1,271 \times 12,000 + 1,173 \times 12,000}{701 \times 13,606} \]
\[ = 979 \text{ psi (compression)} \leq 2600 \text{ psi} \]

Top Stress (deck):

\[ f_{T,d} = \frac{1,173 \times 12,000}{29,436} \]
\[ = 478 \text{ psi (compression)} \leq 1400 \text{ psi} \]

Design is OK for Midspan Service Moments.
Flexural Strength

Required Strength at Midspan: Use LL+1 Moments from BRIDGELL for full continuity.

1. End Span:

\[ M_u = 1.3 \times (1271 + 68 \times 1.67 \times 744) \]
\[ = 3356 \text{ ft-kip} \]

Provided Strength:

- \( f_{su}^* = f_s^* \left(1 - 0.5 \frac{p^*}{f_s^*} \right) \)
- \( p^* = 18 \times 0.153/(72 \times 76.11) \)
- \( b = 6 \times 12 = 72 \text{ in.} \)
- \( d = 72 - (16 \times 3.00 + 2 \times 2.0)/18 + 7.0 = 76.11 \text{ in.} \)
- \( f_c^* = 3500 \text{ psi} = 3.5 \text{ ksi for deck} \)
- \( f_s^* = 270 \text{ ksi} \)
- \( f_{su}^* = 270 \times (1 - 0.5 \times 0.00050 \times \frac{270}{3.5}) \)
- \( = 265 \text{ ksi} \)

For rectangular section:

\[ \phi M_n = \phi f_{su}^* d \left(1 - 0.6 \frac{p^*}{f_{su}^*} \right) \]
\[ = 1.0 \times 2.75 \times 265 \times 76.11 \times (1 - 0.6 \times 0.00050 \times 265/3.5)/12 \]
\[ = 4517 \text{ ft-kip} > 3356 \text{ ft-kip} \text{ OK} \]

Check depth of compression zone, \( a: \)

- \( a = A^* f_{su}^* / 0.85 f_c^* \)
- \( = 2.75 \times 265/0.85 \times 3.5 \times 72^2 \)
- \( = 3.40 \text{ in} < 7.0 \text{ in.} \) (Neutral Axis Is in the Deck)

Check Maximum Steel:

\[ \text{Reinforcement Index } = \frac{p^* f_{su}^*}{f_c^*} \leq 0.3 \]

2. Interior Span:

\[ M_u = 1.3 \times (1899 + 60 \times 1.67 \times 585) \]
\[ = 4134 \text{ ft-kip} \text{ OK} \]

Provided Strength:

- \( f_{su}^* = f_s^* \left(1 - 0.5 \frac{p^*}{f_s^*} \right) \)
- \( p^* = 20 \times 0.153/(72 \times 76.00) \)
- \( b = 6 \times 12 = 72 \text{ in.} \)
- \( d = 72 - 3.00 + 7.0 = 76.00 \text{ in.} \)
- \( f_c^* = 3500 \text{ psi} = 3.5 \text{ ksi for deck} \)
- \( f_s^* = 270 \text{ ksi} \)

Check Minimum Steel:

\[ \phi M_n \geq 1.2 M_{cr}^* \]
\[ M_{cr}^* = \left( \frac{f_c^* + f_{se} + f_{se} x e}{A_g} \right) \frac{S_B}{S_B^C} - M_{DL} \left( \frac{S_B^C}{S_B} - 1 \right) \]
\[ F_{cr} = 7.5 \sqrt{6500/1000} = 0.605 \text{ ksi} \]
\[ F_{se} = 435.0 \text{ kips} \]
\[ M_{DL} = 1,271 \text{ ft-kip} \]
\[ S_B = 13,340 \text{ in.}^3 \]
\[ S_B^C = 17,193 \text{ in.}^3 \]
\[ M_{cr}^* = \left( \frac{0.605 + 435.0 \times 33.47}{701} \right) \times 13,340 \times 12 - 1,271 \left( \frac{17,193}{13,340} - 1 \right) \]
\[ = 2953 \text{ ft-kip} \]
\[ 1.2 \times M_{cr}^* = 3544 \text{ ft-kip} \text{ OK} \]

\[ \phi M_n = 4517 \times 3544 \text{ ft-kip} \text{ OK} \]
\[ f^* = 270 \left(1 - 0.6 \times 0.00056 \times \frac{270}{3.5}\right) \]
\[ = 264 \text{ ksi} \]

For rectangular section: (AASHTO 9.17.2)
\[ \phi M_n = \phi A^* f^* d \left(1 - 0.6 \frac{f^*}{f'_c}\right) \]
\[ = 1.0 \times 3.06 \times 264 \times 76.00 \left(1 - 0.6 \times 0.00056 \times 264/3.5\right)/12 \]
\[ = 4987 \text{ ft-kip} > 4134 \text{ ft-kip} \quad \text{OK} \]
\[ \phi = 1.0 \text{ for factory produced girder} \quad \text{(AASHTO 9.14)} \]

Check depth of compression zone, a:
\[ a = A^* f^* / 0.85 f'_c \]
\[ = 3.06 \times 264/0.85 \times 3.5 \times 72 \]
\[ = 4.77 \text{ in.} < 7.5 \text{ in.} \quad \text{(Neutral Axis is in the Deck)} \]

Check Maximum Steel: (AASHTO 9.18.1)
Reinforcement Index = \( p f^* / f'_c \leq 0.3 \)
\[ = 0.00056 \times 264/3.5 \]
\[ = 0.042 \leq 0.3 \quad \text{OK} \]

Check Minimum Steel: (AASHTO 9.18.2)
\[ \phi M_n \geq 1.2 M^+_{cr} \]
\[ M^+_{cr} = \left(f_{cr} + \frac{f_{se} + f_{se} x e}{A_g}\right) S_B - \frac{M_{DL}(S_B - 1)}{S_B} \]
\[ f_{cr} = 7.5 \sqrt{5500/1000} = 0.605 \text{ ksi} \]
\[ F_{se} = 492.7 \text{ kips} \]
\[ M_{DL} = 1,899 \text{ ft-kip} \]
\[ S_B = 13,340 \text{ in.}^3 \]
\[ S_B = 17,193 \text{ in.}^3 \]
\[ M^+_{cr} = \left(0.605 \times 492.7 \times \frac{492.7 	imes 33.36 - 17,193}{701} \times 13,340\right) - 1,899(13,340 - 1) \]
\[ = 3091 \text{ ft-kip} \]
\[ 1.2 \times M^+_{cr} = 3709 \text{ ft-kip} \]
\[ \phi M_n = 4987 > 3709 \text{ ft-kip} \quad \text{OK} \]

Design is OK for Positive Midspan Flexural Strength

Design for Negative Support Moments
Using resulting girder section from the design for positive midspan moment, time-dependent restraint moments are calculated for the fully continuous structure using BRIDGERM. Restraint moment at B is obtained by analyzing a 90-ft span and using 1.5 times restraint moment RMII for the first interior support. Restraint moment at B is obtained by multiplying restraint moment at C (RMII from BRIDGERM) by 1.5 to give restraint moment at the first interior support. The factor 1.5 is related to the relative stiffnesses of end and interior spans. This factor is to be used to determine end span restraint moments when uplift cannot occur as discussed on page E-17 of Appendix E of this report. Restraint moment at C is obtained by analyzing a 110-ft span and using restraint moment RMII for the central support. For 40 day continuity and assuming no uplift, the following restraint moments (ft-kip) are obtained:

<table>
<thead>
<tr>
<th>Support</th>
<th>Maximum Negative (82 days)</th>
<th>1800 days</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>-696</td>
<td>+109</td>
</tr>
<tr>
<td>C</td>
<td>-550</td>
<td>-213</td>
</tr>
</tbody>
</table>

From BRIDGELL analysis, the following support moments (ft-kip) were obtained:

<table>
<thead>
<tr>
<th>Support</th>
<th>Additional Dead Load</th>
<th>Maximum LL+I*</th>
</tr>
</thead>
<tbody>
<tr>
<td>B</td>
<td>-121</td>
<td>-722</td>
</tr>
<tr>
<td>C</td>
<td>-121</td>
<td>-760</td>
</tr>
</tbody>
</table>

*For loadcases producing maximum negative moments.

Service Moments
Support B:
Additional DL: -121 ft-kip
Try $A_s = 6.00$ in.$^2$ for deck reinforcement. Check if service load stresses are within allowable.

Stress limits:
- Compression: $0.6 \times f'_c$ (Current AASHTO 9.7.2.4)
- Tension: $24,000$ psi for Grade 60 (AASHTO 8.15.2.2)

Calculate cracked section moment of inertia with 6.0 in.$^2$ deck reinforcement.

\[
n = \frac{29,000}{57} \sqrt[5]{500} = 6.3
\]

\[
n_{st} = 6.3 \times 6.00 = 37.8 \text{ in.}^2
\]

Assume neutral axis in web.

\[
37.8 \times (75.5 - x) = \frac{6}{2} (x - 6)^2 + 24 \times 6 (x - 3) + 3 \times 9 (x - 7)
\]

\[
x = 15.38 \text{ in.} > 6 + 3 = 9 \text{ in.}
\]

Neutral Axis is in Web

\[
I_c = 164,582 \text{ in.}^2
\]

\[
S_{cr,B} = I_c / x = 164,582/15.38 = 10,701 \text{ in.}^3
\]

\[
S_{cr,T} = I_c / (d - x) = 164,582/(75.5 - 15.38) = 2738 \text{ in.}^3
\]

Check Concrete Stress:

\[
a. \text{ End Span}
\]

At 82 days, $f_{pe} = 165,000$ psi (from BRIDGERM)

\[
e = 36.36 - (16 \times 3.0 + 2 \times 70.0)/18 = 25.92 \text{ in.}
\]

\[
f_{se} = 18 \times 0.153 \times 165,000
\]

\[
f_B = 454,400 \text{ lb}
\]

\[
F_{se} = 454,400 + 454,400 \times 25.92 + 1,539 \times 12,000
\]

\[
e = 3257 \text{ psi} < 0.6 f'_c = 3900 \text{ psi} \quad \text{OK}
\]

\[
b. \text{ Interior Span}
\]

At 82 days, $f_{pe} = 167,000$ psi (from BRIDGERM)

\[
e = 36.36 - (16 \times 3.0 + 4 \times 69.0)/20 = 20.16 \text{ in.}
\]

\[
f_{se} = 20 \times 0.153 \times 167,000
\]

\[
f_B = 511,000 \text{ lb}
\]

\[
F_{se} = 511,000 + 511,000 \times 20.16 + 1,539 \times 12,000
\]

\[
e = 3227 \text{ psi} < 3900 \text{ psi} \quad \text{OK}
\]

*Note: These computations conservatively assume transfer length is zero.

Check Steel Stress:

\[
f_s = 6.3 \times 1,539 \times 12,000/2,738
\]

\[
= 42,500 \text{ psi} > 24,000 \text{ psi}
\]

Exceeds limit

Service load steel stresses are greater than allowable. A new area of reinforcement must be determined to reduce steel stress to below 24,000 psi.

Try: $A_{st} = 10.80$ in.$^2$ (18 - #7 bars)

\[
n_{st} = 6.3 \times 10.8
\]

\[
= 68.04 \text{ in.}^2
\]
Calculate section properties.
\[ x = 21.19 \text{ in.} > 9.00 \]  
Neutral Axis is in Web
\[ I_{cr} = 266,665 \text{ in}^4 \]
\[ S_{cr,B} = \frac{266,665}{21.19} = 12,584 \text{ in}^3 \]
\[ S_{cr,T} = \frac{266,665}{(75.5 - 21.19)} = 4910 \text{ in}^3 \]
By inspection, concrete stress is OK

Check Steel Stress:
\[ f_s = 6.3 \times 1,539 \times 12,000/4,910 = 23,700 \text{ psi} < 24,000 \text{ psi} \text{ OK} \]
Use 18 = #7 bars in deck over each girder.

Check stress range for Support C.
Minimum stress occurs under restraint moment plus additional dead load moment. Maximum stress occurs with application of live load. Use restraint moment at 1800 days.
\[ M_{min} = -213 - 121 = -334 \text{ ft-kip} \]
\[ < M_{cr} = -1088 \text{ ft-kip (from p. F-22)} \]

Calculate stress using cracked section properties.
\[ S_{steel} = 4,910 \text{ in}^3 \]
\[ f_{min} = 6.3 \times 334 \times 12,000/4,910 = 5,100 \text{ psi} \]
\[ M_{max} = -213 - 121 - 760 = -1094 \text{ ft-kip} \]
\[ < M_{cr} = -1088 \text{ ft-kip (from p. F-22)} \]

\[ f_{max} = 6.3 \times 1094 \times 12,000/4,910 = 16,800 \text{ psi} \]
\[ f_f = (16,800 - 5,100)/1000 = 11.7 \text{ ksi} \]

Maximum allowable stress range (ksi)
\[ f_f = 21 - 0.33 f_{min} + 8 \times 0.3 \text{ (AASHTO 8.16.8.3)} \]
\[ = 21 - 0.33 \times 5.1 + 8 \times 0.3 \]
\[ = 21.7 \text{ ksi} > 11.7 \text{ ksi} \text{ OK} \]
By inspection Support B is also OK.

Design is OK for Negative Service Moments

Flexural Strength

Use Grade 60 deformed reinforcing bars.

Required Strength:
Support B:
\[ M_u = 1.3 \times (121 + 1.67 \times 722) \]
\[ = 1775 \text{ ft-kip} \]
Support C:
\[ M_u = 1.3 \times (121 + 1.67 \times 760) \]
\[ = 1807 \text{ ft-kip} \]

Check capacity for Support C with 10.8 in.\(^2\) deck steel.

For rectangular sections:
\[ \phi M_n = \phi (A_s f_y (d-a/2)) \text{ (AASHTO 8.16.3.2)} \]
\[ a = A_s f_y/(0.85 f'_c b) \]
\[ = 10.8 \times 60/(0.85 \times 6.5 \times 24) \]
\[ = 4.89 \text{ in.} < 6.0 \text{ in.} \text{ (Compression Area is in the Bottom Flange)} \]
Provided Flexural Strength:

\[ \phi M_n = 0.9 \times (10.8 \times 60 \times (75.5 - 4.89/2))/12 \]

\[ = 3550 \text{ ft-kip} > 1807 \text{ ft-kip} \quad \text{OK} \]

\[ 1.20 \times M_{cr} = 1306 \text{ ft-kip} < 3550 \text{ ft-kip} \quad \text{OK} \]

Provided reinforcement gives flexural strength greater than required strength, \( M_U \), and greater than 120% of \( M_{cr} \). (New Requirement)

Check maximum reinforcement, \( \rho_{max} = 0.5 \rho_b \) (New Requirement)

\[ x_b = 0.725 \times 87 \times 75.5/(87 + 60) \]

\[ \rho_b = 0.05 \times 6.5 \times (24 \times 6 + 6 + 24/2) \times 3 + (32.40 - 9) \times 6 \]

\[ = 0.0167 \]

\[ 0.5 \rho_b = 0.0084 \]

\[ A_{st, max} = 0.0084 \times 24 \times 75.5 \]

\[ = 15.2 \text{ in.}^2 > 10.8 \text{ in.}^2 \quad \text{OK} \]

Design is OK for Negative Moment Flexural Strength
APPENDIX G
PROPOSED AASHTO PROVISIONS

NEW DEFINITION

Add the following definition to Article 9.1.3:

Effective Restraint Moments—Moments occurring at continuity supports of bridges composed of simple-span precast, prestressed girders made continuous, due to creep and shrinkage of precast girders and cast-in-place deck concrete. The effective restraint moments shall be computed assuming full structural continuity for negative and positive moments at continuity supports. See Article 9.7.2.

REVISED AASHTO SPECIFICATIONS

Delete current Article 9.7.2 and replace with the following:

9.7.2 Bridges Composed of Simple-Span Precast Prestressed Girders Made Continuous

9.7.2.1 General

When structural continuity is assumed in calculating live load plus impact and composite dead load moments, the effects of creep and shrinkage shall be considered in the design of bridges incorporating simple-span precast, prestressed girders and deck slabs continuous over two or more spans.

9.7.2.2 Positive Moment Connection at Supports

9.7.2.2.1. Provision of a positive moment connection at continuity supports to resist effective restraint moments that may develop shall be optional.

9.7.2.2.2. If positive moment reinforcement is not provided at supports, live load plus impact moments for positive moment within the span and negative moment at or near continuity supports shall be determined from an analysis that accounts for lack of positive moment continuity.

9.7.2.2.3. If positive moment reinforcement is provided for structural continuity, such reinforcement shall be designed for the combination of effective restraint moments, and moments due to composite dead loads, and live load plus impact in remote spans. Shrinkage and elastic shortening of the piers shall also be considered when significant. Calculated service load stress in nonprestressed positive moment connection reinforcement at continuity supports shall not exceed 0.6 f_y or 36 ksi. The limiting stress of 36 ksi applies to both deformed reinforcing bars and unstressed prestressing strand reinforcement.

9.7.2.2.4. Irrespective of whether or not positive moment reinforcement is provided at supports, effective restraint moments required in Articles 9.7.2.3 and 9.7.2.5 shall be computed assuming full structural continuity for negative and positive moments at continuity supports.

9.7.2.3 Positive Moments Within Span—Service Load Design

9.7.2.3.1. Restraint moments shall be considered in order to determine effective structural continuity and to compute service moments within the span due to live load plus impact and composite dead load.

9.7.2.3.2. Positive service moments within the span shall be determined from superposition of moments from analyses of the girders as continuous structures for live load plus impact, composite dead load, and effective restraint moments.

9.7.2.3.3. The contribution to positive service moments from live load plus impact shall be determined from an analysis of the girders as continuous structures for the load case that produces maximum positive midspan moment in the span under consideration.

9.7.2.3.4. The contribution to positive service moments from restraint moments shall be determined from conditions that produce maximum positive or least negative effective restraint moment. The effects of shrinkage and elastic shortening of the piers shall also be considered in the analysis for effective restraint moment when significant.

9.7.2.3.5. The effective continuity moment at a support shall consist of the sum of support moments from continuous analyses for live load plus impact and composite dead load, and the effective restraint moment. If positive moment reinforcement is not provided at supports, only negative effective continuity moments shall be considered.

9.7.2.3.6. Magnitude of the maximum negative effective continuity moment at a support, used to determine the positive service moments within the span, shall be limited to 125 percent of the calculated negative cracking moment of the composite section at the face of the support.

9.7.2.3.7. Concrete stresses due to minimum and maximum service moments shall not exceed the allowable stresses of Article 9.15.2.2. Calculation of maximum and minimum concrete stresses shall include effects of prestressing and simple span moment due to girder and deck weight acting on the girder section alone. The effects of live load plus impact and composite dead load moments, adjusted to account for effective structural continuity, shall be determined from analyses of the composite girder and deck section.

9.7.2.4 Positive Moments Within Span—Strength Design

Strength design of prestressed girders for positive moments within the span shall be done in accordance with appropriate Articles of Part C of Section 9. Time-dependent effects of creep and shrinkage of deck and girder concrete shall not be considered for strength design of girders even if positive moment reinforcement is provided at supports.

9.7.2.5 Negative Moments At Supports—Service Load Design

9.7.2.5.1. Negative service moments at supports shall be determined from superposition of moments from analyses of the girders as continuous structures for live load plus impact, composite dead load, and effective restraint moments.

9.7.2.5.2. The contribution to negative service moments from live load plus impact shall be determined from an analysis of the girders as continuous structures for the load case that produces maximum negative moment at the support under consideration.

9.7.2.5.3. The contribution to negative service moments from restraint moments shall be determined from conditions that produce the maximum negative or least positive effective restraint moment, except as required for determination of fatigue stress range in Article 9.7.2.5.6.

9.7.2.5.4. Compressive stress in ends of girders at piers resulting from summation of effects of prestressing, composite dead
The presence of negative moment connections at supports produces restraint moments that either subtract from or add to the continuity moments. Therefore, the term effective continuity moments is used in the provisions of Article 9.7.2 to denote the moments resulting from the combined effects of live load plus impact, composite dead load, and restraint moment.

Analytical studies indicate that effective continuity for this type of bridge can range between 0 and 100 percent of full continuity. An effective continuity of 0 percent means that the composite girders are behaving essentially as simple spans for all loads. An effective continuity of 100 percent indicates that the composite girders are acting together as a fully continuous elastic structure for live load plus impact and composite dead load moments.

The relative influences of concrete creep and shrinkage on effective continuity are highly dependent on the construction timing of the bridge. If the prestressed girders are relatively new at the time that the deck and diaphragms are cast, creep will predominate the behavior, causing positive restraint moments and a probable reduction of full continuity at late ages. If the girders are relatively old at the time of casting the deck and diaphragm, differential shrinkage between the deck and girder concrete will predominate the behavior. Differential shrinkage between the deck and girder concretes causes negative restraint moments to occur at the supports and thereby tends to increase effective continuity. However, differential shrinkage also increases the potential for negative moment cracking of the deck concrete over the supports. With deck cracking over the support, the rotational stiffness in the negative moment region is significantly reduced and effective continuity decreases. Therefore, in order to take advantage of structural continuity in this type of bridge for live load plus impact and composite dead load moments, the effects of creep and shrinkage must be considered in the design. If no analysis is conducted to determine time-dependent restraint moments at supports, and no positive moment reinforcement is provided at supports, as further discussed in Article 9.7.2.2, the midspan service moment should be taken as the sum of simple span additional dead load and live load plus impact moments.

9.7.2.2 Positive Moment Connection at Supports

Results of an analytical study of time-dependent restraint moments and service load moments at supports in prestressed concrete girders made continuous indicate that there is little structural advantage gained by providing positive moment reinforcement at supports. With the deck and diaphragm concrete cast at an early girder age, time-dependent creep deformations cause positive restraint moments at supports that will generally induce a crack in the bottom of the diaphragm concrete. With application of live load, the positive moment crack must close prior to inducing negative moment at the continuity connection. There is a loss of negative continuity moment associated with the closing of cracks in the bottom of the diaphragm. The presence of positive moment reinforcement in the diaphragm helps to maintain a relatively small crack, thereby increasing apparent live load continuity. However, the positive restraint moment resulting from the presence of the reinforcement in the bottom of the diaphragm increases the...
positive moments within the span. This increase in positive moment when bottom reinforcement is used at supports is virtually equal to the loss of negative moment continuity if the positive reinforcement is not used. The net result on the effective continuity moment is the same, irrespective of whether or not positive moment reinforcement is provided at supports. Therefore, providing positive moment reinforcement has no significant benefit for reducing service load moments for this type of bridge. Also, a survey of State Departments of Transportation (G-1) indicated several states allow construction of bridges with continuous decks without requiring positive reinforcement in diaphragms. No serviceability problems associated with the practice of not using the positive moment reinforcement were reported by these states. Therefore, the use of positive moment reinforcement is optional.

9.7.2.2.2. In addition to positive restraint moments from effects of girder creep, positive moments at supports can occur in continuous bridges due to loading on remote spans. If positive moment reinforcement is not provided at supports, the connection at supports will act as a hinged connection for positive moments. This limits the nature of the continuity of the bridges for some load cases. As illustrated in Figure G-1 for AASHTO truck load occurring in one span of a multispans bridge, the continuous structure for resisting load consists of three spans for a loaded interior span, as shown in Figure G-1(a), and two spans for a loaded end span, as shown in Figure G-1(b). For load configurations in which no positive moments occur at supports, such as composite dead load over the entire bridge and some patterns of AASHTO lane loads, the entire bridge can be assumed to act as a continuous structure, as shown in Figures G-1(c) and G-1(d).

9.7.2.2.3. There is a minor structural advantage for transfer of positive moments resulting from the effects of loads in remote spans if positive moment reinforcement is provided at supports. If the designer wants to take advantage of this increased structural continuity, the positive moment reinforcement must be designed for all of the load effects contributing to positive moments in the connection. The 36 ksi allowable stress corresponds with an approximate slip of 0.01 in. in the reinforcement at the ends of the girders. This allowable stress is recommended to maintain a small crack width at the interface of the diaphragm and girder concrete. The amount of slip is approximately the same whether mild steel reinforcing bars or unstressed prestressing strand is used for the positive moment reinforcement. Therefore, the limiting stress of 36 ksi applies to both mild steel reinforcement and unstressed prestressing strand reinforcement.

9.7.2.2.4. While the nature of continuity is affected to a small degree for some cases of live load plus impact, research has indicated that the presence or absence of positive moment reinforcement at supports does not affect the nature of continuity for determination of time-dependent restraint moments. As previously stated, the loss of some effective continuity due to cracking in the bottom of the diaphragm, when positive reinforcement is not provided, is virtually balanced by the increased positive restraint moment when the reinforcement is provided. Analyses made to determine the resultant service load moment, which include moments due to dead load, restraint moments due to creep and shrinkage, and live loads, are independent of the presence or absence of positive moment connection in the diaphragm. This behavior is shown in Figure G-2. With positive moment reinforcement provided at supports, the inclusion of a positive restraint moment is required in the summation of moments to determine the resultant moment diagram. Without positive reinforcement provided at supports, no positive restraint moment is included in the resultant moment diagram.
moment develops from time-dependent effects because of diaphragm cracking. However, the continuity moments at supports for live load plus impact are reduced because the diaphragm cracks must close before continuity is established at the negative moment connection. The lack of full continuity for live load plus impact without positive reinforcement at the supports is balanced by the need to include a restraint moment when positive moment reinforcement is provided at the supports. Therefore, the resultant mid-span moments, as shown in Figure G-2, are virtually identical whether or not positive moment reinforcement is provided at the supports.

The analyses to determine design moments assuming full structural continuity for both negative and positive moments at supports, as illustrated in the left-hand summation of moments in Figure G-2, are more straightforward than calculations to determine the effects of crack opening and closing when positive moment reinforcement is not provided, as illustrated in the summation of moments on the right hand-side of Figure G-2. It is therefore recommended that analyses to determine restraint moments be carried out assuming full continuity for both positive and negative moments whether or not the positive moment reinforcement is provided at the support. The calculated positive restraint moment is not an actual restraint moment when the positive moment reinforcement is not used. For this case, calculation of a restraint moment is simply a method to account for the opening of the cracks in the bottom of the diaphragm. Therefore, the calculated restraint moments are defined as effective restraint moments.

9.7.2.3 Positive Moment Within Span—Service Load Design

9.7.2.3.1. A main structural advantage for this type of bridge with negative continuity at supports as compared to bridges consisting of simply supported girders is the reduction in positive moments within the span for service live load plus impact and composite dead load. However, time-dependent behavior influences the continuity of this type of bridge such that the effective continuity for live load plus impact can vary from 0 to 100 percent. Therefore, the effective continuity moments must include the restraint moments that result from creep and shrinkage of the composite structure.

9.7.2.3.4. Analysis for positive moments within the span for service design should be carried out for conditions including time-dependent effects that produce the maximum positive or least negative restraint moment. The maximum positive or least negative restraint moment occurs after 2 to 5 years in bridges that were constructed with girders that were relatively young when the deck and diaphragms were cast. Therefore, the design should be based on a time-dependent analysis using the youngest likely girder age at casting of the deck and diaphragm. The time-dependent analysis should be carried out to determine restraint moments when bridges are at least 2 years old.

9.7.2.3.5. If no positive reinforcement is provided at supports, only negative effective continuity moments need be considered. That is, if the calculated restraint moments are positive and larger than the summation of negative moments from continuous analyses for live load plus impact and composite dead load, the cracks in the bottom of the diaphragm resulting from creep in the girder will remain open under full service design loads. Under this condition, the girders are effectively simply supported girders for all loading and the effective continuity is essentially 0 percent. Therefore, any net positive effective continuity moment at a support, calculated from the summation of support moments due to live load plus impact, composite dead load, and the effective restraint moment, need not be added to the resultant moment diagram. However, if positive reinforcement is used at the supports, net positive effective continuity moments shall be included in the resultant moments.

9.7.2.3.6. If time-dependent analyses predict negative restraint moments, the girders may behave as fully continuous for live load plus impact and composite dead load. However, the maximum negative effective continuity moment, for determination of positive service load moments within the span, is limited to a value of 125 percent of the calculated negative cracking moment of the composite section. This limit provides for a situation when negative moments cause deck cracking over the supports. Deck cracking reduces effective continuity. The reduction in continuity results from the softening of the negative moment region after cracking, along with an accompanying redistribution of moments to the mid-span region. Figure G-3 illustrates that the amount by which the calculated effective continuity moments at the supports exceeds 125 percent of the cracking moment should be redistributed to the positive moment region for design of the girders for service loads.

9.7.2.4 Positive Moments Within Span—Strength Design

Stresses and strains induced in the girders by volume change from creep and shrinkage are self-limiting within the girder in that they are relieved by the deformations accompanying cracking in the concrete and yielding of reinforcement. As a result, presence or absence of time-dependent restraint moments has no effect on the flexural strength of the structure. This was demonstrated by comparing the results of tests to destruction of continuous composite girders tested at approximately 2 years of age with a continuous composite girder tested at 12 days after deck casting (G-2).

9.7.2.5 Negative Moments at Supports—Service Load Design

9.7.2.5.1. Negative moment connections at supports shall be designed for the maximum negative continuity moment including the continuity moment from live load plus impact and composite dead load and the maximum negative or least positive restraint moment from creep and shrinkage effects.

9.7.2.5.3. Dependent on age of girders when deck and diaphragm concrete is cast, the restraint moment from time-dependent effects could increase or decrease the negative continuity moment. The maximum negative or least positive restraint moment occurs with early age loading on bridges constructed with girders that are relatively old when the deck and diaphragm are cast. Therefore, the design should be based on a time-dependent analysis using the oldest likely girder age at casting of the deck and diaphragm. The time-dependent analyses should be carried out to determine the maximum negative restraint moment during the time period shortly after casting the deck and diaphragm. If the bridge will be open to traffic within the time period at which the maximum negative restraint mo-
9.7.2.5. For checking fatigue limits for deck reinforcement, the maximum negative moment at early age is essentially a transient condition. Although restraint moments can remain negative for the life of the structure, they reach a reduced and relatively constant level after approximately 2 years. Therefore, use of a restraint moment calculated at approximately 700 days after casting of deck and diaphragms is recommended for checking fatigue limits.

9.7.2.6 Negative Moments at Supports—Strength Design

9.7.2.6.1. The composite girder cross section in negative moment regions will behave as a reinforced concrete section rather than a prestressed concrete section. Therefore, the strength of this cross section should be determined in accordance with the appropriate requirements of Article 8.16 for reinforced concrete. Stresses and strains induced in the girders by volume change from creep and shrinkage are self-limiting within the girder in that they are relieved by deformations accompanying cracking in the concrete and yielding of reinforcement. As a result, presence or absence of time-dependent restraint moment has no effect on the strength of the structure.

9.7.2.6.2. Effects of prestress in the ends of the girder induce an initial compression in the bottom flange of the girder. However, analytical studies (G-1) indicate that the initial precompression has negligible effect on the maximum flexural or shear strength within a hinging region that forms at the support as the bridge girders are loaded to the strength of the structure. Therefore, the initial precompression due to prestress may be neglected in calculation of the negative moment strength at the diaphragm.

9.7.2.6.3. The critical section for concrete compression in the girders occurs away from the support pier and diaphragm concrete. Therefore, the compressive strength of the girder concrete should be used in the strength calculation for the negative moment capacity at the support. This recommendation is made based on use of typical girder design concrete compressive strengths between 5,000 psi to 6,500 psi. If the design concrete
strength for a girder is significantly above the typical range, further consideration should be given to the design strength of the diaphragm concrete.

9.7.2.7 Deck Reinforcement

9.7.2.7.1. Reinforcement provided in the deck for negative moment capacity at the supports should be sized to meet minimum reinforcement requirements and requirements for adequate distribution of reinforcement for crack width control.

9.7.2.7.2. To ensure ductile behavior in the negative moment region and develop full strength of the bridge girders, analytical studies (G-1) indicate that the deck reinforcement ratio shall not exceed 50 percent of $p_b$ as defined in Article 9.7.2.7.2. The bottom flange or bulb of girder cross sections typically used in this type of bridge construction may be relatively small compared to the area of reinforcement provided in the deck. Therefore, the neutral axis may be in the web region of the cross section. The area of compression concrete, $A_c$, used in the calculations for the balanced condition, must be the actual area of the girder bottom flange and web in compression. As with calculations to determine the negative moment strength of the cross section at the supports, the effect of initial precompression due to prestress may be neglected in determination of the strain conditions for balanced reinforcement.

REFERENCES


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