# A Taxicab Fare Policy Formula Based on Fuel Consumption Observations 

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#### Abstract

A new taxicab fare collection methodology is proposed. The formulation developed is based on an urban fuel consumption study performed in Austin, Dallas, and Lubbock, Texas, and in Matamoros, Mexico. The formulation determines the fare as a function of travel distance and time with parameters related to vehicle operating cost, driver's wage, and the taxicab agency's profit and overhead cost. A survey of the 1985 fare-setting policies of taxicab agencies in some major U.S. cities has also been performed. On the basis of the survey results, a comparison is made between the currently used and the proposed fare-determination algorithms. The results of a numerical example indlcate that the current practice slightly overestimates the travel time contribution to the fare and underestimates that of the travel distance. Consequently the currently charged fare for a trip in congested traffic conditions (long travel time per unit distance) appears to be overcharging the peak-period customer, whereas the reverse holds for the offpeak traffic conditions. The proposed fare-determination algorithm may be particularly useful to regulatory agencies in inferring a taxi agency's unit profit rate embedded in its farepricing policy. In addition, the fuel consumption-based algorithm could be used by regulatory agencies to establish fare guidelines in conjunction with taxicab operating costs and revenues.


Of all the forms of urban mass transit, the taxicab industry alone generates more than 50 percent of the annual revenues in the United States. Yet few analytical relations have been explicitly established for fare calculations in metered taxis. Traditionally, taxi fares have been computed on the basis of an initial cost (flag-drop cost) plus additional charges for the distance traveled and the time elapsed. However, assignment of unit charges to distance traveled and time elapsed have not been based on a systematic framework. In this paper an attempt is made to formulate an analytical rationale for the determination of cost weights for traveled distances and times in taxi fare calculations. Recent vehicular fuel consumption studies for urban street networks (1-5) and a survey of fare policies of taxicab companies in some major U.S. cities formed the basis of this formulation.

## DEFINITION OF VARIABLES

$\delta=$ distance increment (mi) for which the taximeter is programmed to advance the fare;
$\Delta \mathrm{F}_{\mathrm{d}}=$ fare increment (cents) for each $\delta \mathrm{mi}$ of travel;
$\tau=$ time increment (cents) for which the taximeter is programmed to advance the fare;

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\(\Delta \mathrm{F}_{\mathrm{t}}=\) fare increment (cents) for each \(\tau \min\) of travel;
\(\mathrm{N}_{\mathrm{d}}=\) number of meter advancements due to travel \(\delta \mathrm{mi}\)
    before \(\tau \mathrm{min}\) is reached;
    \(\mathrm{N}_{\mathrm{t}}=\) number of meter advancements due to traveling \(\tau\)
    min before \(\delta \mathrm{mi}\) is reached;
    \(\mathrm{N}=\) total number of meter advancements in a trip ( N
        \(=\mathrm{N}_{\mathrm{t}}+\mathrm{N}_{\mathrm{d}}\) );
    \(\mathrm{F}=\) total fare for a trip (cents);
    \(\mathrm{F}_{0}=\) flag-drop charge (initial fare displayed by the
        meter) (cents);
    \(\delta_{0}=\) distance (mi) covered by \(\mathrm{F}_{0}\);
    \(\tau_{0}=\) time (min) covered by \(\mathrm{F}_{0}\);
    \(\mathrm{x}=\) trip length (mi);
    \(\mathrm{t}=\) trip duration (min);
    \(\mathrm{v}_{\mathrm{r}}=\) mean running speed ( \(\mathrm{mi} / \mathrm{min}\) );
    \(\mathbf{v}=\) mean overall speed (mph);
    \(\mathrm{T}=\) trip time per unit distance ( \(1 / \mathrm{v}\) ) \([\mathrm{min} / \mathrm{mi}(\mathrm{t} / \mathrm{x})]\);
    \(\phi=\) fuel consumed per unit distance ( \(\mathrm{gal} / \mathrm{mi}\) );
    \(\mathrm{k}_{1}=\) fuel consumption parameter (gal/mi) representing
        the fuel consumed to overcome the rolling
        resistance;
    \(\mathrm{k}_{2}=\) fuel consumption parameter ( \(\mathrm{gal} / \mathrm{min}\) )
        representing the time-related fuel losses to the
        engine;
    \(\mathrm{C}_{\mathrm{F}}=\) fuel cost (cents) for an \(\mathrm{x}-\mathrm{mi}, \mathrm{t}\)-min trip;
    \(\mathrm{g}=\) gasoline cost (cents/gal);
    \(\mathrm{C}_{\mathbf{T}}=\) total operating cost of a vehicle (cents) for an
        x-mi, t-min trip;
    \(\mathrm{R}=\) ratio of \(\mathrm{C}_{\mathrm{T}}\) to \(\mathrm{C}_{\mathrm{F}}\);
    \(\mathrm{p}=\) taxicab company's unit profit and overhead costs
        (cents/mi per taxicab);
    \(\mathrm{w}=\) unit wage of the taxicab driver (cents/min per
        taxicab);
    \(\mathrm{t}_{0}=\) average slack time ( min ) between unloading one
        passenger and loading another; and
    \(\mathrm{x}_{0}=\) average slack distance (mi) between unloading
        one passenger and loading another.
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## CONVENTIONAL TAXIMETER FARE MECHANISMS

Although taxicabs advertise their fares as a function of traveled distance alone, the taximeter itself is programmed to compute the fare as a function of both distance traveled and time elapsed. The results of a 1985 survey of the fare-pricing policy in some major U.S. cities are shown in Table 1. The distancerelated portion of the fare is computed in $\delta$-mi increments, and the time-related part is measured in $\tau$-min increments. During a trip, the meter advances once every $\delta \mathrm{mi}$ or $\tau \mathrm{min}$, whichever is reached first. The fare is then advanced by an amount $\Delta F_{t}$ every time the meter advances because of the time constraint $\tau$ and by

TABLE 1 THE 1985 FARE POLICY IN SOME MAJOR U.S. CITIES

| Clty | First Flag Drop |  |  | Each Extra Distance |  | Each Extra TYme |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { Fare } \\ & \left(\mathrm{F}_{0}, f\right) \end{aligned}$ | $\begin{aligned} & \text { TYme } \\ & \left.\tau_{0}, \text { min }\right) \end{aligned}$ | Dist. $\left.{ }_{0}, m+1\right)$ | $\begin{aligned} & \text { Fare } \\ & \left(\Delta F_{\mathrm{d}}, \stackrel{\varphi}{ }\right) \end{aligned}$ | Interval ( $\delta, \mathrm{ml}$ ) | $\begin{gathered} \text { Fare } \\ \left(\Delta \mathrm{F}_{\mathrm{t}}, \stackrel{\uparrow}{4}\right) \end{gathered}$ | $\begin{aligned} & \text { Interval } \\ & (\tau, m \mathrm{md} n) \end{aligned}$ |
| R1 chmond | 120 | 1.0 | 1/5 | 20 | 1/5 | 20 | 1.0 |
| Roanoke | 120 | 1.0 | 1/6 | 20 | 1/6 | 20 | 1.0 |
| Dallas | 130 | 0.7 | 1/10 | 10 | 1/10 | 10 | 0.7 |
| Austin | 110 | 0.67 | 1/10 | 10 | 1/10 | 10 | 0.67 |
| San Antonio | 110 | 0.75 | 1/10 | 10 | 1/10 | 10 | 0.75 |
| New York | 110 | 0.5 | 1/9 | 10 | 1/9 | 10 | 0.5 |
| Chicago | 110 | 1.0 | 1/10 | 10 | 1/10 | 10 | 1.0 |
| Los Angeles | 120 | 1.5 | 1/2 | 70 | 1/2 | 70 | 1.5 |
| San Francisco | 130 | 0.5 | 1/6 | 20 | 1/6 | 20 | 0.5 |
| St. Louis | 130 | 1.0 | 1/7 | 10 | 1/7 | 10 | 1.0 |
| Wash., D.C. | 109 | 0.15 | 1/10 | 9 | 1/10 | 9 | 0.15 |
| New Orleans | 110 | 1.0 | 1/10 | 10 | 1/10 | 10 | 1.0 |
| Seattle | 120 | 0.45 | 1/6 | 20 | 1/6 | 20 | 0.45 |
| Atlantic City | 135 | 1.5 | 1/5 | 20 | 1/5 | 20 | 1.5 |

$\Delta \mathrm{F}_{\mathrm{d}}$ every time the distant constraint $\delta$ is reached. For New York City, for example, $\delta=1 / 9 \mathrm{mi}, \tau=0.5 \mathrm{~min}, \Delta \mathrm{~F}_{\mathrm{t}}=10$ cents, and $\Delta \mathrm{F}_{\mathrm{d}}=10$ cents (Table 1). It may be noted that when the meter advances because of reaching either $\tau \min$ or $\delta \mathrm{mi}$, both the time and distance counters are reset to zero.

Based on the foregoing description, the total fare $(\mathrm{F})$ is computed as
$\mathrm{F}=\mathrm{F}_{0}+\mathrm{N}_{\mathrm{t}} \Delta \mathrm{F}_{\mathrm{t}}+\mathrm{N}_{\mathrm{d}} \Delta \mathrm{F}_{\mathrm{d}}$
where $F_{0}$ is the initial charge for the flag drop, and $N_{t}$ and $N_{d}$ are the number of times the meter advances as a result of reaching $\tau \mathrm{min}$ or $\delta \mathrm{mi}$, respectively. As may be noted in Table 1 , most taxicab agencies select the lengths of $\tau$ and $\delta$ so that $\Delta \mathrm{F}_{\mathrm{t}}$ can be considered approximately equal to $\Delta \mathrm{F}_{\mathrm{d}}$; this results in the following fare-setting relation:
$\mathrm{F}=\mathrm{F}_{0}+\mathrm{N} \Delta \mathrm{F}$
where N is the total number of times the meter advances, regardless of the cause, and $\Delta F$ is the fare increment per meter advancement. It must be noted that the flag-drop charge ( $\mathrm{F}_{0}$ ) generally covers the first $\delta_{0} \mathrm{mi}$ or $\tau_{0} \mathrm{~min}$, whichever is reached first, so that N is measured $\delta_{0} \mathrm{mi}$ or $\tau_{0} \mathrm{~min}$ after the start of a ride. The flag-drop charge in New York, for example, is 110 cents, which covers the first $1 / 9 \mathrm{mi}$ or 0.5 min (Table 1). Consequently, the fare determination formula for New York becomes F (cents) $=110+10 \mathrm{~N}$.

In a highly congested area, most of the N meter advancements would be due to reaching the time limit $\tau$, whereas in noncongested locations or off-peak periods N would consist mostly of meter advancements generated by reaching the distance constraint $\delta$. Ghahraman et al. (6) have shown that for a
ride of length x mi and duration t min, N can be approximated as
$N=\left[(1 / \delta)-\left(1 / v_{\mathbf{r}}^{\tau}\right)\right] x+(t / \tau)$
where $\mathrm{v}_{\mathrm{r}}$ is the mean running speed during a ride. The taxi fare for a ride may then be computed by combining Equations 2 and 3 to obtain
$\mathrm{F}=\mathrm{F}_{0}+\mathrm{x} \Delta \mathrm{F}\left[(1 / \delta)-\left(1 / \mathrm{v}_{\mathrm{r}}^{\tau}\right)\right]+\Delta \mathrm{F}(\mathrm{t} / \tau)$
where $\mathrm{v}_{\mathrm{r}}$ is in miles per minute.
This fare approximation (Equation 4) can be employed by the taxicab industry for policy-making purposes regarding the values of $\delta, \tau, \mathrm{F}_{0}$, and $\Delta \mathrm{F}$ through performing sensitivity analyses on the cost and revenue outcome of various strategies. The resulting policy decisions regarding initial and incremental costs $\mathrm{F}_{0}$ and $\Delta \mathrm{F}$ must, of course, fall within the limits set by regulatory agencies.

## FUEL CONSUMPTION STUDIES

Although the determination of $\mathrm{F}_{0}$ and $\Delta \mathrm{F}$ using the foregoing techniques is a sound managerial practice, a more systematic framework may be developed based on analysis of taxicab operational costs. To this end, the results of a series of vehicular fuel consumption observations in urban areas may be applied directly.

Recent studies $(1,2)$ have shown that in urban regimes of speeds less than 35 mph , some 71 percent of the variance in fuel consumption per unit distance ( $\phi$ ) is accounted for by a single variable, $T$, the trip time per unit distance (the reciprocal
of mean overall speed, v). This one-variable dependence can then be expressed as
$\phi=\mathrm{k}_{1}+\mathrm{k}_{2} \mathrm{~T}(\mathrm{v}<\sim 35 \mathrm{mph})$
where $\mathrm{k}_{1}$ and $\mathrm{k}_{2}$ are vehicle-dependent parameters. It may be noted that $T=1 / v=t / x$.

The model expressed by Equation 5 offers a simple and moderately accurate means of predicting the fuel consumption for urban speed regimes ( $\mathrm{v}<\sim 35 \mathrm{mph}$ ) and relatively flat network topography. Moreover, it has the advantage that its parameters can be physically interpreted (5). The parameter $\mathrm{k}_{2}$, for example, is related to various time-dependent losses, mainly the idle fuel flow, which operates while the vehicle is stopped and coasting; this represents 20 to 50 percent of the time spent in congested urban traffic. The parameter $k_{2}$ is affected by the engine type, size, and power. The parameter $\mathrm{k}_{1}$, on the other hand, is related to the fuel consumed per unit distance to overcome rolling resistance and is mainly a function of the vehicle mass. A set of $k_{1}$ and $k_{2}$ values is presented for various passenger cars in Table 2. In general, the heavier vehicles display greater values of $\mathrm{k}_{1}$, whereas the smaller and newer models display lower values of $\mathrm{k}_{2}$. It must be emphasized that as long as a relatively flat topography exists, the
values of the parameters $k_{1}$ and $k_{2}$ are almost entirely functions of the vehicle itself and not of the operational environment and location.
The 1983-1984 fuel consumption observations in Austin, Dallas, and Lubbock, Texas, as well as in Matamoros, Mexico, showed that in more congested locations (higher T-values) such as Matamoros, a greater amount of fuel is consumed per unit distance. However, the fuel consumption per unit distance under various traffic conditions has indeed been a linear function of T , as suggested by Equation 5 . The results of these studies are shown in Figure 1, where each data point represents a 1-mi trip for a 1983 Ford Fairmont six-cylinder automobile with a curb weight of $2,825 \mathrm{lb}$ and a measured idle fuel flow for a warmed-up engine of $0.557 \mathrm{gal} / \mathrm{hr}$. This test vehicle had an automatic transmission with three forward ratios and a $3.3-\mathrm{L}$ displacement engine. It used unleaded gasoline with a minimum octane rating of 87 . During the fuel observations the four tires were kept at the maximum allowable cold pressure of 35 psi and the air conditioner-heater was not in operation. The tires were of P175/75R14 size and type. The vehicle was equipped with a Model 1240 Fluidyne precision fuel flow indicator to determine the total fuel used for a trip of a given distance. The fuel meter was installed under the hood. The gasoline line fed through the following parts in sequence: inline

TABLE 2 FUEL CONSUMPTION CHARACTERISTICS OF VARIOUS VEHICLES

| Referenc | ace Vehicle | Model <br> Year | Test Mass (1bs) | $\underset{(\mathrm{gal} / \mathrm{mile})}{\mathrm{k}^{\mathrm{m}}}$ | Idle Fuel Flow Rate ( $\mathrm{gal} / \mathrm{min}$ ) | $\begin{gathered} \mathrm{k}_{2} \\ (\mathrm{gal} / \mathrm{min}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Present Study | Ford Fairmont | 1983 | 3125 | 0.0317 | 0.0093 | 0.0090 |
| 5,7 | British Bedford CF Van | 1978 | 3770 | 0.0347 |  | 0.0082 |
| 5,7 | British Bedford CF Van | 1978 | 4872 | 0.0438 |  | 0.0083 |
| 8 | Standard-Sized Car | 1975 | 5050 | 0.0551 | 0.0128 | 0.0153 |
| 8 | Standard-Sized Car | 1974 | 4980 | 0.0650 | 0.0139 | 0.0166 |
| 8 | Small Imported Car | 1974 | 2277 | 0.0256 | 0.0089 | 0.0105 |
| 8 | Intermediate Size Car | 1975 | 3792 | 0.0496 | 0.0111 | 0.0120 |
| 8 | Large Luxury Car | 1974 | 5474 | 0.0709 | 0.0132 | 0.0172 |
| 8 | Subcompact Station Wagon | 1975 | 2833 | 0.0420 | 0.0073 | 0.0094 |
| 2 | Subcompact Car | 1973 | 3620 | 0.0526 | 0.0044 | 0.0070 |
| 9 | Smail Van | 1956 | 2352 | 0.0209 | 0.0033 | 0.0050 |
| 9 | British Car | 1955 | 3025 | 0.0447 | 0.0059 | 0.0083 |
| 10 | Empty Minibus | 1965 | 3717 | 0.0532 |  | 0.0055 |
| 10 | Loaded Munibus | 1965 | 4592 | 0.0588 |  | 0.0063 |
| 10 | Small British Car | 1965 | 2251 | 0.0329 |  | 0.0084 |
| 10 | British Car | 1964 | 3258 | 0.0494 |  | 0.0084 |
| 11 | Australian Station Wagon | 1965 | 3200 | 0.0362 |  | 0.0094 |
| 16 | Ford Cortina |  | 2667 | 0.0240 |  | 0.0071 |
| 17 | Ford Escort |  | 2116 | 0.0172 |  | 0.0080 |
| 18 | Renault Rl2 |  | 2337 | 0.0298 |  | 0.0044 |



FIGURE 1 Fuel consumption versus trip tlme, 1983 slx-cylinder Ford Fairmont Futura with automatic transmission.
filter, auxiliary electric fuel pump, pressure regulator, glasswalled filter, Fluidyne fuel meter, original mechanical fuel pump, and carburetor.

As is evident from Figure 1, the data for the four cities spread along a fairly linear band, and the regression line that indicates the trend is given by
$\phi=0.0317+0.0090 \mathrm{~T}$
with $\phi$ in gallons per mile, T in minutes per mile, a total of 377 points, and $\mathrm{R}^{2}=0.79$. These values of $\mathrm{k}_{1}=0.0317 \mathrm{gal} / \mathrm{mi}$ and $\mathrm{k}_{2}=0.0090 \mathrm{gal} / \mathrm{min}$ can be compared with the average values over nine vehicles tested in Detroit some years ago (8), namely, $\mathrm{k}_{1}=0.0362 \mathrm{gal} / \mathrm{mi}$ and $\mathrm{k}_{2}=0.0214 \mathrm{gal} / \mathrm{min}$. The reductions in the values of these parameters over the years reflect the general improvements in fuel efficiency and idle fuel flow of later vehicle models. This point is further illustrated in Table 2 where $k_{1}$ and $k_{2}$ values for 15 vehicle models are tabulated. In addition, the values of $k_{1}$ and $k_{2}$ for the Ford test vehicle in this study fall well within the scatter of the remaining data in Table 2. The data in Table 2 are also graphically presented in a plot of $k_{1}$ versus vehicle mass (Figure 2) and $k_{2}$ versus the measured idle fuel flow (Figure 3). A linear regression of $k_{1}$ versus $M$, forced through the origin, yields a slope of $1.21 \times 10^{-5} \mathrm{gal} / \mathrm{mi}-\mathrm{lb}$ (Figure 2) and that of $\mathrm{k}_{2}$ versus I yields a slope of 1.20 (Figure 3).

## FARE DETERMINATION BASED ON FUEL CONSUMPTION

The foregoing fuel consumption results may be used to directly establish a methodology based on fuel consumption for the fare determination of an $\mathrm{x}-\mathrm{mi}$, $\mathrm{t}-\mathrm{min}$ taxi ride. In doing so, it must first be noted that the variable $T(=t / x)$ in Equation 5 by itself accounts for a large part of the traffic dependence of fuel consumption, which in turn constitutes a major portion of the operational cost of a vehicle.

Thus, the vehicle-related parameters $\mathrm{k}_{1}$ and $\mathrm{k}_{2}$ as well as the trip duration ( $t$ ) and the trip length ( x ) of a ride form a sufficient


FIGURE 2 Fuel parameter $\mathbf{k}_{1}$ versus vehicle test mass $\mathbf{M}$ for various vehicles in Table 2.
basis for determination of the fuel cost of a taxicab engaged in a trip $x$ mi long and $t \min$ in duration; namely,
$C_{F}=x g\left(k_{1}+k_{2} T\right)$
where g is the gasoline cost per gallon and $\mathrm{C}_{\mathrm{F}}$ is the total fuel cost for a trip x mi long with an average trip time of $\mathrm{T} \mathrm{min} / \mathrm{mi}$. Knowing that $T=t / x$, Equation 7 may be simplified as
$C_{F}=g\left(k_{1} x+k_{2} t\right)$
The total operational $\operatorname{cost}\left(\mathrm{C}_{\mathrm{T}}\right)$ of a vehicle includes the fuel cost as well as other major operational expenses such as oil, maintenance and repair, tire wear, and depreciation costs. The ratio $\mathrm{C}_{\mathrm{T}} / \mathrm{C}_{\mathrm{F}}$ may be denoted by R where $\mathrm{R}>1$. Results reported by Claffey et al. in 1971 (15) yield $\mathrm{R}=1.75$ for a composite passenger car operating at 30 mph average speed (including turns and speed change effects) for a relatively flat topography. A composite car was defined (15) for a vehicle mix of 20 percent large, 65 percent standard size, 10 percent compact, and 5 percent small cars. Data compiled by Zaniewski et al. in 1982 (16) imply that $\mathrm{R}=1.9$ for a medium-sized automobile operating at 20 mph average speed on a relatively flat terrain. The total cost may then be formulated as
$C_{T}=\operatorname{Rg}\left(k_{1} x+k_{2} t\right)$
To formulate a fare-setting algorithm based on the total cost $\mathrm{C}_{\mathrm{T}}$ of Equation 9, it is necessary that variables representing the profit and overhead costs of the taxicab agency as well as the driver's wage be included. The driver's unit wage per minute is


FIGURE 3 Fuel parameter $\mathbf{k}_{2}$ versus vehicle idle fuel flow I for various test vehicles in Table 2.
denoted by $w$ and the expected company profit and overhead costs per mile of operation per taxicab by $p$. Then during an $x$-mi, $t$-min ride, the accumulated fare ( $F$ ) may be computed as
$\mathrm{F}=\mathrm{F}_{0}+\left(\mathrm{x}-\delta_{0}\right)\left(\mathrm{Rgk}_{1}+\mathrm{p}\right)+\left(\mathrm{t}-\tau_{0}\right)\left(\mathrm{Rgk}_{2}+\mathrm{w}\right)$
where $F_{0}$ is as before the flag-drop charge, which also covers the fare for the initial $\delta_{0} \mathrm{mi}$ or $\tau_{0} \mathrm{~min}$ of the ride, whichever is reached first. The variables in Equation 10 are x and t .

The initial fare $F_{0}$ is usually set at a higher value than may be computed by considering unit operating costs, profit, company overhead, and driver wage for $\delta_{0} \mathrm{mi}$ and $\tau_{0} \min$ of operation. A higher value of $\mathrm{F}_{0}$ is generally used in order to discourage customers from engaging taxicabs for very short trips. Responding to calls for short trips is undesirable from an operational standpoint, because in a competitive environment this could result in losing customers in need of considerably longer and more profitable rides. In addition, the cost incurred by responding to such calls (for driving to the customer's location and making the actual trip to the destination) may indeed exceed the fare collected unless a sufficiently high value of $\mathrm{F}_{0}$ is charged.

The foregoing considerations suggest that the computation of $\mathrm{F}_{0}$ as a minimum must include the cost of a trip $\left(\mathrm{x}_{0}+\delta_{0}\right) \mathrm{mi}$ long and $\left(t_{0}+\tau_{0}\right) \min$ in duration, where $x_{0}$ and $t_{0}$ are the slack distance and time, respectively (i.e., the mean distance and time that a taxicab without passengers travels before arriving at the origin of a call). The values of slack distance $x_{0}$ and slack time $t_{0}$ must, of course, be determined by performing a statistical analysis on the relevant data available or to be collected. These values primarily would be a function of the size of the metropolitan area, the taxi fleet size, and the spatial distribution of taxicabs. Having set the values of $\delta_{0}$ and $\tau_{0}$ by policy and knowing the values of $\mathrm{x}_{0}$ and $\mathrm{t}_{0}$, the initial fare $\mathrm{F}_{0}$ may then be estimated to be
$\mathrm{F}_{0}=\left(\mathrm{x}_{0}+\delta_{0}\right)\left(\mathrm{Rgk}_{1}+\mathrm{p}\right)+\left(\mathrm{t}_{0}+\tau_{0}\right)\left(\mathrm{Rgk}_{2}+\mathrm{w}\right)$
Combining Equations 10 and 11 would then yield an analytical algorithm based on fuel consumption to determine the fare for a taxi ride x mi long and t min in duration.

## A NUMERICAL EXAMPLE

The following numerical example is presented to provide a better understanding of the magnitude of the various parameters in the proposed fare-setting formula (Equation 10) as well as the sensitivity of the fare to these parameters. In addition, the fare associated with a specific trip as determined by Equation 10 is compared with an estimate of the currently charged fare obtained through Equation 4.

For example, consider a New York City taxicab agency operating a fleet of medium-sized cars ( $\mathrm{k}_{1}=0.032 \mathrm{gal} / \mathrm{mi}, \mathrm{k}_{2}=$ $0.009 \mathrm{gal} / \mathrm{min}$ ). Let us also assume a driver's hourly wage of $\$ 9.00$ ( $\mathrm{w}=\$ 0.15 / \mathrm{min}$ ) and a profit and overhead rate of $\$ 0.25$ per mile per taxicab ( $p=\$ 0.25$ ). An average cost for unleaded gasoline of $\$ 1.35 / \mathrm{gal}(\mathrm{g}=\$ 1.35)$ and $\mathrm{R}=2$ will also be used in the computations. Note from Table 1 that in New York the flagdrop charge currently in effect covers an initial distance of $1 / 9$ $\mathrm{mi}\left(\delta_{0}=1 / 9\right)$ or an initial duration of $0.5 \mathrm{~min}\left(\tau_{0}=0.5 \mathrm{~min}\right)$. An assumption must also be made regarding the values of $x_{0}$ and $t_{0}$ in New York City. In this example $x_{0}=1 \mathrm{mi}$ and $\mathrm{t}_{0}=4 \mathrm{~min}$ are used. Hence,

$$
\begin{aligned}
\mathrm{x}_{0} & =1 \mathrm{mi} \\
\mathrm{t}_{0} & =4 \mathrm{~min} \\
\mathrm{R} & =2, \\
\mathrm{~g} & =\$ 1.35 / \mathrm{gal} \\
\mathrm{k}_{1} & =0.032 \mathrm{gal} / \mathrm{mi} \\
\mathrm{k}_{2} & =0.009 \mathrm{gal} / \mathrm{min} \\
\delta_{0} & =1 / 9 \mathrm{mi} \\
\tau_{0} & =0.5 \mathrm{~min} \\
\mathrm{p} & =\$ 0.25 / \mathrm{mi}, \text { and } \\
\mathrm{w} & =\$ 0.15 / \mathrm{mi}
\end{aligned}
$$

With these parametric values, Equation 11 yields a flag-drop charge of $\mathrm{F}_{0}=\$ 1.16$ compared with the current New York City flag-drop charge of $\$ 1.10$. Substituting a value of $\$ 1.16$ for $\mathrm{F}_{0}$ in Equation 10 and using the foregoing parameter values results in the following fare-setting relation for New York:
$F=116+33.64[x-(1 / 9)]+17.43(t-0.5)$
Therefore, a peak period 6-mi ride of 30 min duration in New York City corresponds, according to Equation 12, to a fare F = \$8.28.

For comparison purposes, the current charge for a $6-\mathrm{mi} 30-$ min ride in New York can be estimated by means of Equation 4 (6) by using the current taxicab fare structure in New York outlined in Table 1, namely,

$$
\begin{aligned}
\mathrm{F}_{0} & =\$ 1.10 \\
\Delta \mathrm{~F} & =\$ 0.10 \\
\delta & =1 / 9 \mathrm{mi}, \text { and } \\
\tau & =0.5 \mathrm{~min}
\end{aligned}
$$

Note that in using Equation 4, the average running speed ( $\mathrm{v}_{\mathrm{r}}$ ) for this $6-\mathrm{mi}, 30-\mathrm{min}$ trip must first be estimated. Observations in the New York-Newark area $(17,18)$ have shown that, on the average, a vehicle is stopped 36.8 percent of the time during the peak period. Therefore, during the $6-\mathrm{mi}, 30-\mathrm{min}$ ride, on the average, the taxicab can be assumed to have been stopped for 11.3 min and in motion for the remaining 18.7 min of the trip, yielding an average running speed $\mathrm{v}_{\mathrm{r}}=19.2 \mathrm{mph}$ or $0.32 \mathrm{mi} /$ min. Hence, Equation 4 is calibrated as
$F=110+27.5 x+20 t$
Consequently, by using Equation 13, an estimate of the fare currently charged in New York City for a $6-\mathrm{mi}, 30-\mathrm{min}$ ride is $\$ 8.75$. This is to be compared with a fare of $\$ 8.28$ for the same trip computed by using the fuel-consumption-based relation of Equation 12.

Although these fares ( $\$ 8.75$ versus $\$ 8.28$ ) are remarkably close, it must be noted that in the current fare determination practice (Equation 13) the traveled time is weighted slightly more ( $\$ 0.20 / \mathrm{min}$ ) as compared with the proposed fuel-based formula (Equation 12), in which time is weighted as $\$ 17.43 /$ $\min$. Unlike travel time, the influence of the travel distance is slightly underestimated in practice (Equation 13), particularly at higher levels of congestion. This is so because the coefficient of $x$ in Equation 4 is directly proportional to the average running speed $\left(\mathrm{v}_{\mathrm{r}}\right)$. As $\mathrm{v}_{\mathrm{r}}$ decreases with an increase in the level of concentration, the value of the coefficient of $x$ would become smaller. In order to avoid a negative coefficient for $x$, $v_{r}$ must be greater than $\delta / \tau$. Thus, the fare approximation relation of Equation 5 is only valid for $v_{r}>\delta / \tau$. For this numerical example that threshold is 13.4 mph . As a result, in uncongested traffic conditions (short trip times per mile), from the perspective of the cost of operating a taxicab, customers are slightly undercharged. On the contrary, in very congested traffic (long trip times per mile) the customers would be overcharged. It must, however, be noted that the time and distance coefficients in Equations 12 and 13, although insensitive to $\mathrm{x}_{0}$ and $t_{0}$, are rather sensitive to these assumptions regarding $p$ and w. Consequently, the foregoing conclusions are only warranted if realistic values of $p$ and $w$ are assumed. In light of which, the proposed fuel-consumption-based algorithm may be particularly useful to regulatory agencies in estimating a taxicab company's unit profit and overhead costs based on its practiced fare-setting formula.

## SUMMARY AND DISCUSSION

Any taxicab fare-setting formula must consider both travel time and travel distance. Although the taxicab in-vehicle public information bulletins may imply that the fare is only a function of the travel distance, in reality a taximeter operates as a function of distance and time. This is self-evident when a meter advances while the taxi is standing still.

The conventional taximeter increases the initial flag-drop charge by a fixed fare increment for every fixed distance or time interval, whichever is reached first. The flag-drop charge itself covers the fare for an initial specified travel distance or time, whichever is reached first.

The results of an urban fuel consumption study are presented on the basis of which a new taxicab fare-setting algorithm is formulated. The formulation considers the total operating cost of the vehicle, the driver's wage, the company's profit and overhead costs, and the cost of taxicab slack times as well as slack distances.

In the use of the developed algorithm, it must be noted that it is based on a fuel consumption relation that is valid only for urban speed regimes less than about 35 mph . This is the case because at speeds greater than 35 mph fuel consumption increases with speed due to aerodynamic drag, as shown in Figure 4. However, as may be seen in Figure 4, these increases are small up to speeds of about 50 mph . Thus the proposed algorithm would not be significantly in error if used for rides a


IIGURE 4 Fuel consumption versus speed in central business districts of Austin, Dallas, Lubbock, and Matamoros and highway data from several 3-to $5-\mathrm{mi}$, relatively flat sections of Texas freeways collected with 1983 Ford Fairmont.
portion of which takes place in nonurban speed regimes. Another limitation of this formulation is that the underlying fuel consumption model does not account for considerable changes in grade. Adjustments are needed if the relation is to be used in other than moderately rolling or flat terrain. Pelensky et al. (11) have suggested an urban fuel consumption relation similar to Equation 5 that includes a grade-adjustment term as well. However, the use of such a relation in the determination of taxicab fares would require significant changes in the taximeter operational mechanism to measure longitudinal roadway grades in the course of a ride.

The proposed fuel-consumption-based formulation has been calibrated for New York City. The resulting outcome is compared with that of the current fare-setting practice as determined from a 1985 survey of fare policies in some of the major U.S. cities. The comparison indicates that although the fare based on current practice for an average ride is reasonable, the current fare-pricing structure may be overcharging the peakperiod customers and slightly undercharging the off-peakperiod customers. The proposed algorithm may also be useful to the regulatory agencies in studying a taxicab agency's fare
policy and establishing fare guidelines in conjunction with taxicab operating costs.

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