

Investigating Preference Heterogeneity in Value of Time (VOT) and Value of Reliability (VOR) Estimation for Managed Lanes

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- **Roadway pricing:** A popular active transportation and demand management (ATDM) tool
 - Congestion levels, environmental issues, fiscal constraints
- **Managed lanes:** A set of lanes where operational strategies are proactively implemented and managed in response to changing conditions
- **Challenges of Managed lanes facility**
 - Pricing structure, revenue generation, transit operations, social equity concerns, access control, vehicle eligibility, design flexibility, enforcement etc.
- **Understanding travel behavior of managed lane users is essential for prescribing solutions**

- **VOT and VOR Estimation: Substantial variations**
 - VOT Estimation Range: \$3.88/hour ~ \$47.50/hour
 - VOR Estimation Range: \$2.31/hour ~ \$57.45/hour
 - Estimation variation range: VOT = 0.55 to 3.22 VOR
- **Treatment of user heterogeneity: current practice**
 - User heterogeneity aspect of choice behavior is seldom incorporated to the full extent
 - Assume single estimate to represent the entire population
- **Addressing User Heterogeneity**
 - Identify what attributes lead to higher or lower VOT and VOR
 - Quantify the extent of influence on VOT and VOR estimation

- **Data Source**

- South Florida Expressway Stated Preference Survey

- **Survey Period**

- 11/16/2011 – 12/15/2011

- **Observations**

- 2,041 respondents
- 16,327 SP observations (8 different scenarios)

- **Study Corridors and Respondent Share**

- I-95 between Golden Glades & SR 112
- I-75 between I-595 and SR 826
- SR 826 between SR 836 and I-95

Corridor	Number	Percentage
I-95	1060	52%
I-75	521	25.5%
SR 826	460	22.5%
Total	2041	100%

- Source
 - Regional Integrated Transportation Information Systems (RITIS)
- Survey Period
 - 01/01/2012 - 12/31/2012
- Study Corridors
 - I-95 between Golden Glades & SR 112
- Travel Time Distribution
 - 24 by 365 for each facility type by direction

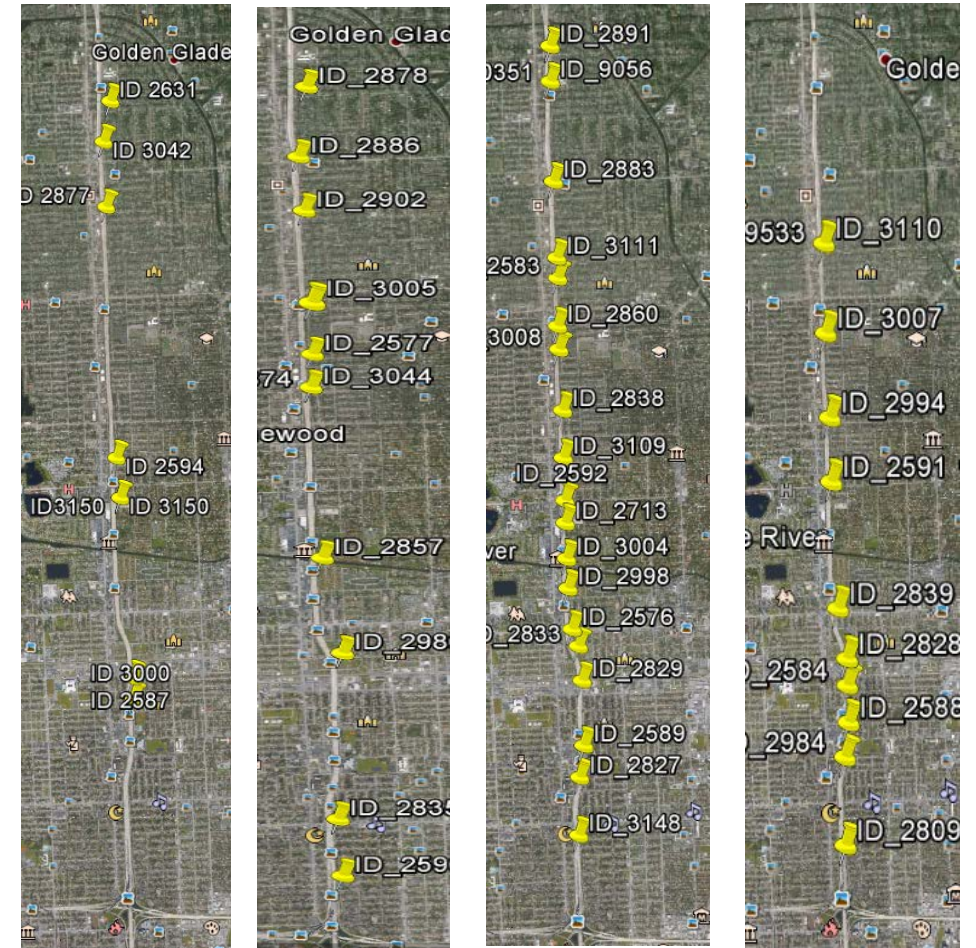


Figure: a) I-95 NB GP b) I-95 NB ML c) I-95 SB GP d) I-95 SB ML

- Semi-standard deviation
- Expected to capture unique benefits offered by the MLs
- A temporal variation is also expected by TOD, as peak periods may have higher variation of travel time compared with off-peak

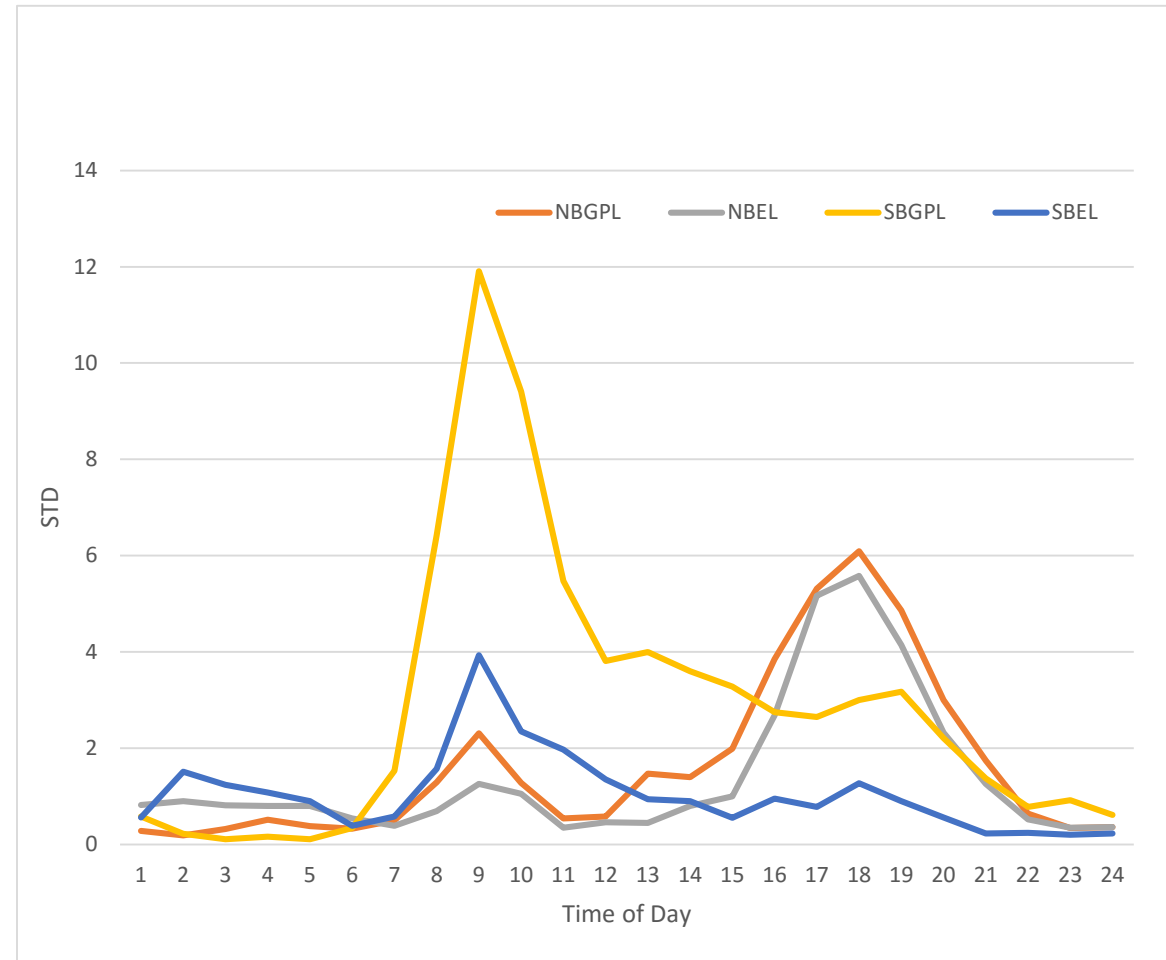


Figure: Standard deviation comparison by time of day



Descriptive Statistics – Combined RPSP Data

Introduction

Data

Methodology

Results Analysis

Conclusions

- SP data
 - Generally respondents selected GP alternative over ML alternatives, except for high income respondents
- RP data
 - Respondents who were male, employed, young or medium age people, from medium and high income households selected MLs mostly
 - Mandatory trips, medium and very frequent trips, weekday trips, drive alone trips, medium and long distance trips were conducted mainly in MLs

	Category	RP Alternatives (%)		SP Alternatives (%)					
		GP	ML	GP	ML	ML Before Peak	ML After Peak	ML Additional Passenger	
Personal Attributes	Age	16-34	40%	60%	51%	24%	3%	6%	16%
		35-54	48%	52%	60%	22%	4%	4%	11%
		55-75+	51%	49%	60%	21%	2%	4%	13%
	Gender	Male	45%	55%	57%	23%	3%	4%	13%
		Female	51%	49%	59%	21%	3%	4%	13%
	Household Income	Low (<50k)	54%	46%	62%	16%	3%	4%	15%
		Med (50k-150k)	48%	52%	59%	23%	3%	4%	11%
		High (>150k)	29%	71%	45%	37%	2%	5%	11%
	Employment	Employed	45%	55%	56%	24%	3%	4%	12%
		Unemployed	63%	37%	64%	14%	2%	4%	16%
	Arrival Flexibility	With Flexibility	44%	56%	59%	21%	4%	4%	12%
		No Flexibility	56%	44%	57%	22%	3%	4%	13%
	Sun Pass	User	45%	55%	57%	23%	3%	4%	12%
		Not User	76%	24%	65%	10%	5%	5%	15%
Trip Attributes	Trip Urgency	Urgent	46%	54%	53%	24%	5%	5%	14%
		Not Urgent	48%	52%	60%	21%	2%	4%	12%
	Trip Purpose	Mandatory	39%	61%	55%	26%	4%	5%	10%
		Non Mandatory	59%	41%	60%	18%	3%	4%	15%
	Trip Frequency (per month)	Less Freq (<4)	51%	49%	58%	22%	3%	4%	14%
		Med Freq (4-12)	39%	61%	53%	25%	5%	5%	12%
		Very Freq (>12)	37%	63%	60%	22%	3%	5%	9%
	Day of Week	Week Day	42%	58%	57%	24%	3%	5%	12%
		Weekend	64%	36%	61%	18%	3%	3%	14%
	Trip Occupancy	Drive Alone	42%	58%	58%	25%	3%	4%	9%
		Drive Another	56%	44%	50%	14%	2%	3%	31%
		HOV3	55%	45%	66%	23%	4%	7%	0%
	Trip Length (miles)	Short (<20)	57%	43%	62%	18%	3%	4%	13%
		Med (20-40)	44%	56%	55%	26%	3%	4%	12%
Long (>40)		44%	56%	53%	22%	4%	6%	15%	
Delay Experience	Have Experience	53%	47%	55%	23%	4%	5%	12%	
	No Experience	43%	57%	60%	22%	2%	4%	13%	
Total Sample N		47%	53%	58%	22%	3%	4%	13%	
		513		16327					

- GP alternative was selected more in SP and ML alternatives were more chosen in RP
 - Experience of RP respondents on managed lanes
 - Benefits of managed lanes were not well represented in the SP survey design

- Interestingly, ML alternatives were less chosen by the respondents when traveling with additional passengers
 - I-95 express lane requires pre-registration in order to receive a toll charge waiver

- Multinomial Logit (MNL)

- Utility Function: $U_{i,n} = \beta_i' X_{i,n} + \epsilon_{i,n}$
- Probability Equation: $P(i) = \frac{e^{U_i}}{\sum e^{U_j}}$

Where, $P(i)$ is the probability that any particular alternative (i) will be chosen and U_i is the utility of that alternative

- Limitations of MNL

- Identical and Independently Distributed (IID)
- Independence from Irrelevant alternatives (IIA)

■ Mixed Logit (ML)

- Utility Function: $U_{itn} = \beta'_n X_{itn} + [\eta_{itn} + \varepsilon_{itn}]$
- Probability Equation:

$$P_{iq} = \int_{\eta_{in}} L_{in}(\beta_n | \phi) f(\beta_n | \phi) \eta_{in}$$

Where $f(\beta_n | \phi)$ represents the density function of the coefficient vector β

■ Advantages of ML

- Coefficients are randomly distributed with a mean and a standard deviation across individuals and scenarios
- Include inter-alternative correlation error term

- Interaction Effects of random parameters

$$U_{in} = \beta X_{in} + \beta_{TT} TT_{in} + \beta_{TTR} TTR_{in} + \beta_{TC} TC_{in} + \gamma_{TT} (S_{in} * TT_{in}) + \gamma_{TTR} (S_{in} * TTR_{in}) + \gamma_{TC} (S_{in} * TC_{in}) + \varepsilon_{in} + \eta_{in}$$

Where, β	Coefficient vector of non-random parameters
X_{in}	Vector of non-random explanatory variables
β_{TT}	Coefficient of Travel Time
TT_{in}	Vector of Travel Time
β_{TTR}	Coefficient of Travel Time Unreliability
TTR_{in}	Vector of Travel Time Unreliability
β_{TC}	Coefficient of Travel Cost
TC_{in}	Vector of Travel Cost
S_{in}	Segmentation dummy variable
γ_{TT}	Interaction coefficient for travel time
γ_{TTR}	Interaction coefficient for travel time unreliability
γ_{TC}	Interaction coefficient for travel cost

■ Dependent Variables

- SP Alternatives (5): GP, ML Peak, ML Before Peak, ML After Peak, and ML Additional Passengers
- RP Alternatives (2) : GP and ML

■ Independent Variables

- Generic Attributes: time, reliability, and cost
- Alternative Specific Attributes: age, gender, household income, employment status, arrival flexibility, sunpass user, previous delay experience, trip purpose, trip length, trip frequency, trip urgency, day of the week, vehicle occupancy

<i>Generic Attributes in utility functions</i>					
Independent Variables	Parameter				
Time	-0.085 (-24.20)				
Reliability	-0.158 (-14.97)				
Cost	-0.588 (-41.16)				
<i>Alternative Specific Attributes in utility functions</i>					
Independent Variables	SP – ML Peak	SP – ML Before Peak	SP – ML After Peak	SP-ML Ad. Passenger	RP-ML
ASC	-3.23 (-23.5)	-2.37 (-11.1)	-2.91 (-19.1)	-2.43 (-26.8)	-2.42 (-5.13)
Male	-0.11 (-2.63)	-	-	-	-
Young People (16-34)	0.67 (12.85)	0.30 (2.70)	0.94 (10.18)	0.54 (9.35)	0.56 (2.20)
Med Income (50 ~ 150K)	0.30 (5.35)	-	-	-0.19 (-3.69)	-
High Income (>150k)	1.23 (18.25)	-	0.52 (4.85)	-	0.96 (3.71)
Employed	0.42 (6.30)	-	-	-	-
Sunpass User	0.72 (7.96)	-0.60 (-4.54)	-	-	1.21 (2.77)
Delay Experienced	-	-	-0.32 (-3.76)	-	-
Mandatory	0.50 (10.06)	-	-	-	-
Flexible Trip	-	-0.20 (-1.99)	-	0.10 (1.85)	-
Less Freq. (<4/month)	0.38 (6.49)	0.63 (5.14)	0.49 (4.78)	0.62 (8.90)	-
Med. Freq. (<12/month)	0.47 (6.06)	1.11 (7.41)	0.55 (3.88)	0.42 (4.24)	-
Weekday Trip	0.34 (8.90)	-0.38 (-3.32)	0.28 (2.60)	-	0.88 (3.72)
Urgent Trip	0.21 (4.40)	0.41 (4.19)	-	0.21 (3.71)	-
Short Trip (<20 miles)	-0.40 (-9.19)	-	-0.35 (-4.13)	-	-
Drive Another	0.57 (13.76)	-	-	-	-
VOT	\$8.67				
VOR	\$16.12				

All variables shown are significant at 5% significance level

Model Specifications

- Time, reliability, and cost
- Normally distributed random parameters
- 1000 Halton draws
- $\frac{\sigma}{\mu} < 0.33$ constraints imposed

Model Results

- Average VOT \$10.68 per hour
- Average VOR \$13.91 per hour

Independent Variables	Parameter		Standard Deviation		
<i>Random parameters in utility functions</i>					
Time	-0.20 (-109.31)		0.07 (109.31)		
Reliability	-0.26 (-26.22)		0.09 (26.22)		
Cost	-1.13 (-65.63)		0.37 (65.63)		
<i>Non-Random parameters in utility functions</i>					
Independent Variables	SP – ML Peak	SP – ML Before Peak	SP – ML After Peak	SP-ML Additional Passenger	RP-ML
ASC	-3.7 (-36.20)	-3.6 (-27.17)	-3.9 (-39.09)	-2.8 (-47.82)	-2.82 (-4.52)
Male	-0.13 (-4.20)	-	-	-	-
Young People (16-34)	0.83 (19.65)	0.43 (5.59)	1.06 (17.02)	0.62 (15.91)	0.56 (1.91)
Med Income (50~150K)	0.34 (8.13)	-	-	-0.21 (-6.47)	-
High Income (>150k)	1.45 (28.54)	-	0.57 (8.54)	-	1.03 (3.41)
Employed	0.47 (8.59)	-	-	-	-
Sunpass User	0.76 (11.19)	-0.55 (-7.06)	-	-	1.17 (2.01)
Delay Experienced	-	-	-0.50 (-9.10)	-	-
Mandatory Trip	0.41 (10.74)	-	-	-	-
Arrival Flexibility	-	-0.17 (-2.75)	-	0.07 (2.00)	-
Less Freq. (<4/month)	0.60 (12.62)	0.83 (9.82)	0.73 (10.62)	0.84 (18.43)	-
Med. Freq. (<12/month)	0.61 (9.99)	1.44 (14.02)	0.87 (9.07)	0.57 (8.61)	-
Weekday Trip	0.25 (5.94)	-0.36 (-4.49)	0.23 (3.45)	-	1.28 (4.49)
Urgent Trip	0.14 (3.82)	0.39 (6.09)	-	0.11 (3.24)	-
Short Trip (<20 miles)	-0.30 (-9.16)	-	-0.21 (-4.06)	-	-
Drive Another	-0.78 (-19.3)	-	-	-	-
VOT	\$10.68				
VOR	\$13.91				

*Model Performance: Log Likelihood Function = -16270.68, McFadden Pseudo R-squared = 0.546
All variables shown are significant at 5% significance level; t-statistics are shown in parentheses.*

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Independent Variables	Parameter	Standard Deviation
<i>Random parameters in utility functions</i>		
Time	-0.38 (-79.34)	0.13 (79.34)
Reliability	-1.94 (-36.94)	0.64 (36.94)
Cost	-2.74 (-70.42)	0.90 (70.42)

<i>Non-Random parameters in utility functions</i>					
Independent Variables	SP – ML Peak	SP – ML Before Peak	SP – ML After Peak	SP-ML Additional Passenger	RP-ML
ASC	-3.32 (-16.7)	-2.93 (-10.8)	-3.45 (-15.4)	-2.63 (-21.7)	-2.91 (-4.20)
Male	-0.18 (-2.46)	-	-	-	-
Young People (16-34)	-	-0.38 (-2.8)	0.29 (2.43)	0.22 (3.15)	-
Med Income (50~150K)	0.28 (3.00)	-	-	-0.17 (-2.65)	-
High Income (>150k)	1.09 (8.93)	-	0.45 (3.17)	-	-
Employed	0.56 (5.17)	-	-	-	-
Sunpass User	0.92 (6.89)	-0.39 (-2.43)	-	-	1.55 (2.35)
Mandatory Trip	0.59 (7.08)	-	-	-	-
Less Freq. (<4/month)	-	0.87 (4.36)	0.62 (3.32)	0.56 (5.11)	-
Med. Freq. (<12/month)	0.66 (3.03)	1.82 (6.59)	1.09 (4.05)	0.65 (4.08)	-
Weekday Trip	0.24 (2.32)	-0.48 (-2.97)	0.34 (2.23)	-	1.27 (3.84)
Urgent Trip	0.33 (3.62)	0.77 (6.15)	-	0.48 (6.49)	-
Short Trip (<20 miles)	-0.40 (-5.27)	-	-0.37 (-3.47)	-	-
Drive Alone	-	-	0.24 (2.24)	-	-
Drive Another	1.65 (19.80)	-	-	-	-

Cost Coefficient = -2.74 + 0.47(High income) + 0.13(Med income) + 0.23 (Urgent trip) + 0.26 (Employed) + 0.30 (Age<34) + 0.28(Age>54) + 0.22(Drive alone) - 0.18(Drive another) + 0.28(Freq. <4/month) + 0.19 (Freq. 4~12/month) + 0.21(Sunpass user) + 0.23 (Weekday) + 0.22 (Delay experienced)

Time Coefficient = -0.38 + 0.02(Urgent trip) + 0.04(Employed) - 0.05(Age<34) + 0.02(Age>54) + 0.07(Drive alone) + 0.14(Drive another) + 0.03(Freq.<4/month) + 0.06(Sunpass user) + 0.03(Delay experienced)

Reliability Coefficient = -1.94 - 0.19 (High Income) + 0.25(Urgent trip) + 0.80(Distance<20 miles) + 0.70(Distance<20~40 miles) + 0.24(Age<34) + 0.18(Age>54) + 0.18(male) - 0.27(Drive another) + 0.59(Freq. <4/month) + 0.33(Freq. 4~12/month) + 0.24(Delay experienced) - 0.16(Arrival Flexibility)

Heterogeneity	Time	Reliability	Cost
High Income (>150K)	-	-0.19 (-1.66)	0.47 (5.70)
Med Income (50~150K)	-	-	0.13 (2.09)
Urgent Trip	0.02 (2.21)	0.25 (3.07)	0.23 (4.16)
Employed	0.04 (3.01)	-	0.26 (3.42)
Short Trip (<20 miles)	-	0.80 (7.26)	-
Med. Trip (20~40 miles)	-	0.70 (6.52)	-
Young People (<34)	-0.05 (-4.46)	0.24 (2.57)	0.30 (4.78)
Old People (>54)	0.02 (2.31)	0.18 (2.27)	0.28 (5.00)
Male	-	0.18 (2.25)	-
Drive Alone	0.07 (6.06)	-	0.22 (3.08)
Drive Another	0.14 (9.95)	-0.27 (-2.25)	-0.18 (-2.27)
Mandatory Trip	-	-	-
Less Freq. (<4/month)	0.03 (2.19)	0.59 (6.40)	0.28 (4.65)
Med. Freq. (<12/month)	-	0.33 (2.18)	0.19 (2.26)
Sunpass User	0.06 (4.75)	-	0.21 (2.35)
Weekday Trip	-	-	0.23 (3.47)
Delay Experienced	0.03 (3.74)	0.24 (2.98)	0.22 (4.27)
Arrival Flexibility	-	-0.16 (-1.96)	-

Model Performance: Log Likelihood Function = -14021.82, *McFadden Pseudo R-squared* = 0.572
All variables shown are significant at 5% significance level; t-statistics are shown in parentheses.



Heterogeneity in VOT and VOR

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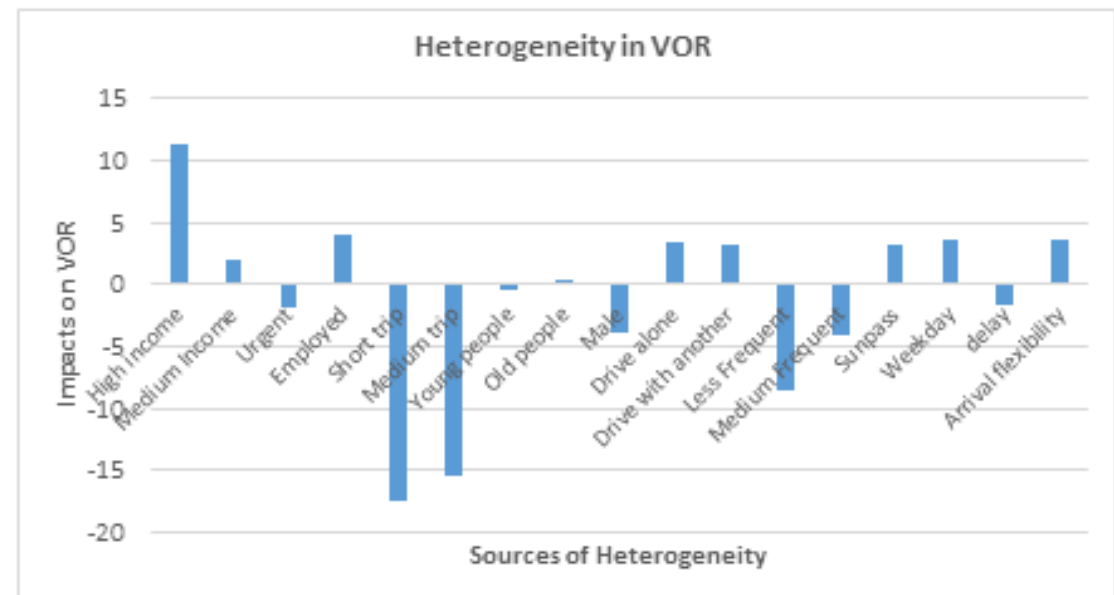
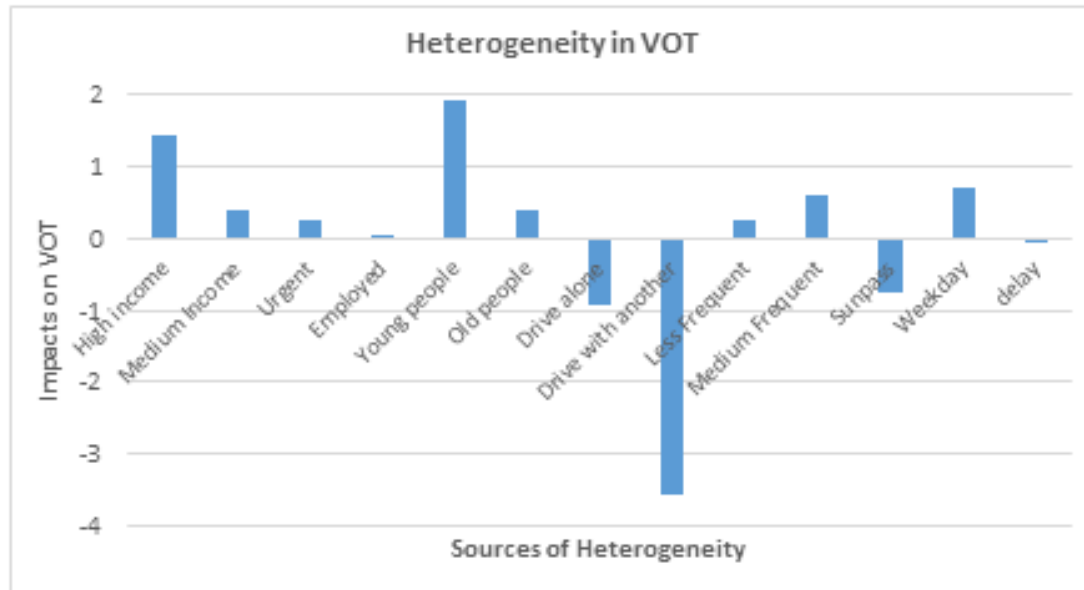
$$\frac{\partial VOT}{\partial S} = \frac{\left(\frac{\partial TT}{\partial S}\right) \times TC - \left(\frac{\partial TC}{\partial S}\right) \times TT}{TC^2} = \frac{\gamma_{TT} \times TC - \gamma_{TC} \times TT}{TC^2}$$

$$\frac{\partial VOR}{\partial S} = \frac{\left(\frac{\partial TR}{\partial S}\right) \times TC - \left(\frac{\partial TC}{\partial S}\right) \times TR}{TC^2} = \frac{\gamma_{TR} \times TC - \gamma_{TC} \times TR}{TC^2}$$

$$\frac{\partial VOT}{\partial(\text{High income})} = \left(\frac{0.00 \times (-2.74) + 0.47 \times 0.38}{(-2.74)^2} \right) \times 60 = 1.42 \text{ \$/hour}$$

$$\frac{\partial VOR}{\partial(\text{High income})} = \left(\frac{(-0.19) \times (-2.74) + 0.47 \times 1.94}{(-2.74)^2} \right) \times 60 = 11.34 \text{ \$/hour}$$

Heterogeneity Sources	ΔVOT	ΔVOR
High Income (>150K)	1.42	11.34
Med Income (50~150K)	0.40	2.05
Urgent Trip	0.25	-1.96
Employed	0.03	4.09
Short Trip (<20 miles)	0.00	-17.43
Med. Trip (20~40 miles)	0.00	-15.40
Young People (<34)	1.93	-0.54
Old People (>54)	0.38	0.34
Male	0.00	-3.86
Drive Alone	-0.92	3.47
Drive Another	-3.58	3.16
Less Freq. (<4/month)	0.26	-8.58
Med. Freq. (<12/month)	0.59	-4.19
Sumpass User	-0.75	3.24
Weekday Trip	0.71	3.60
Delay Experienced	-0.06	-1.76
Flexible Trip	0.00	3.50



- Mixed logit model results indicated an average value of \$10.68 per hour for VOT and \$13.91 per hour for VOR, with significant heterogeneity among the travelers

- In view of sensitivity to time, reliability, and cost
 - High and medium income groups, older individuals, and weekday trips lead to higher values for both VOT and VOR.
 - Urgent trips, less frequent trips, young individuals, and delay experienced travelers perceived higher VOT and lower VOR
 - Female travelers showed considerably higher VOR than males
 - Both driving alone and driving with one passenger reflected lower VOT
 - Short and medium trips only affected VOR, both of which had significantly lower VOR values compared to long trips
 - Less frequent and medium frequent trips resulted in lower VOR values compared with very frequent trips

- Lack of reliability data
- Reliability Measure
- Simple market segmentation

- Modal shifts for transit on managed lanes facility
- Impacts on automated/connected vehicle on VOT and VOR
- Robust market segmentation of managed lane users by latent class model (LCM)
- Joint impacts of heterogeneity and attitudes on choice behavior by hybrid choice model (HCM)

THANK YOU

QUESTIONS ?