

# Plowing the Streets of Pittsburgh

## A Dynamic Route Planning System

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# Motivation & Goals

*"Drivers have printed routing directions laying on the passenger seat. Most of them know the route (or an interpretation thereof) by heart."*

*"A lot of time is lost due to emergency plow requests."*

*"People complain that primary roads in their district are full of snow, while in other districts tertiary roads have already been serviced."*

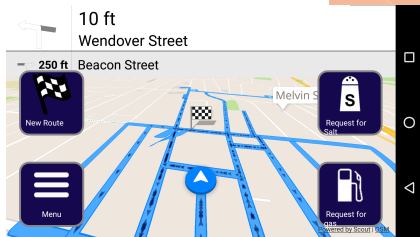
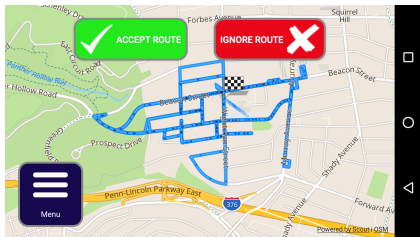
## Motivation (2)

- 1 Consumable resource costs: 4,3M\$ (2014/2015), 3.3M\$ (2013/2014)
  - 2 Labor costs: 3.3M\$ (2014/2015)
  - 3 Equipment costs: 800K\$ (2014/2015)
  - 4 Snow and ice control staff: 275
- safety
  - economy
  - environment
  - Generalizes to street sweeping, street maintenance, garbage collection, etc.



# Goal

*Design a route planning system that issues optimized turn-by-turn instructions to the vehicles as they execute routes, and dynamically revises these plans as unexpected events force changes.*



# Problem Description - Routes

Road segments:

- start/end
- # lanes
- priority class
- shape
- driving speed
- directionality



# Problem Description - Vehicles

## Vehicles:

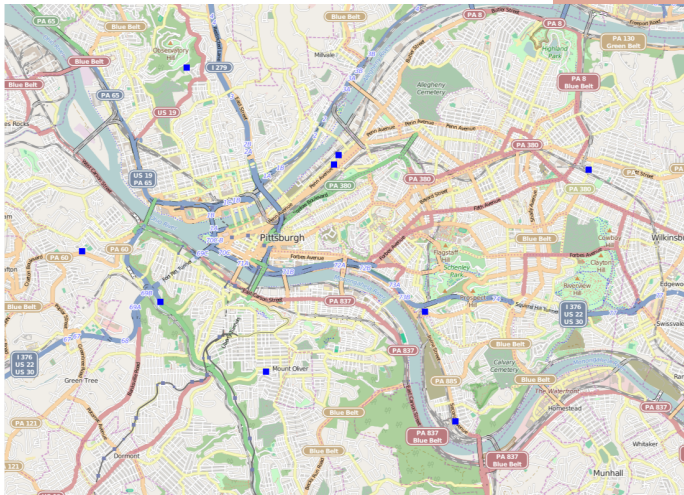
- Location
- Salt Capacity
- Fuel Capacity
- Salt economy
- Fuel economy



# Problem Description - Depots

Depots:

- Location
- Salt (y/n)
- Fuel (y/n)



## Related models

- Chinese postman problem
- Vehicle routing with resource constraints
- Resource-constrained project scheduling with renewable and non-renewable resources

For overview of Snow plowing literature, see N. Perrier, A. Langevin, et. al: [1, 2, 3, 4]

Synchronized arc routing for snow plowing operations [5]

- City of Dieppe: 24,000 inhabitants, 462 intersections, 1,234 road segments ( $\leq 20\%$  Downtown Pittsburgh)

# Model - Objective

## Objectives:

- 1 Makespan
- 2 Minimize deadheading
- 3 Weighted objective of Completion times per priority class

# Model - Constraints

## Constraints:

- 1 Vehicles start/end at depot
- 2 Every lane on a street segment must be covered, subject to traffic direction.
- 3 Renewable resource constraints: fuel, salt
- 4 Time constraints

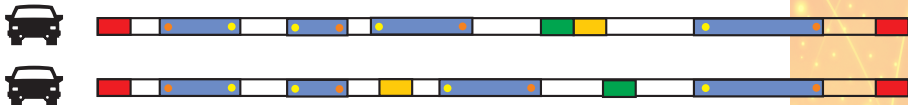
# Model

Job:

- 1 ID
- 2 start location
- 3 end location
- 4 duration
- 5 fuel & salt requirement

Job types:

- 1 source depot job
- 2 target depot job
- 3 plow job
- 4 refuel job
- 5 resupply salt job





# Mathematical models

- Mixed Integer Programming
- Constraint Programming

# Mixed Integer Programming Model - Outline

- Variables:
  - ▶ Three-index formulation: Vehicle  $k$  performs job  $j$  after job  $i$ .
  - ▶ Variables recording resource utilization: time, salt, fuel
- Constraints:
  - ▶ All plow jobs have to be performed, refuel/resupply jobs are optional
  - ▶ Decide on direction for bidirectional jobs
  - ▶ Resource constraints for fuel/salt/time

# Constraint Programming Model - Outline

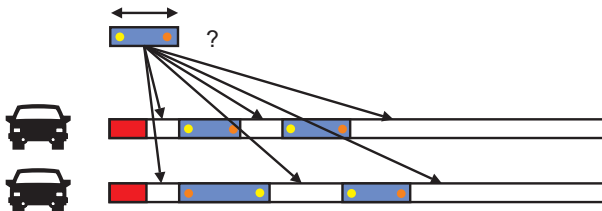
- Variables:
  - ▶ Job (interval) variables.
  - ▶ Job to vehicle assignment variables
- Constraints (outline):
  - ▶ Job sequencing constraints for each vehicle
  - ▶ Alternative constraint for job to vehicle assignment
  - ▶ Cumulative functions to manage resources

# Heuristic

- Constructive Heuristic
- Late Acceptance improvement heuristic

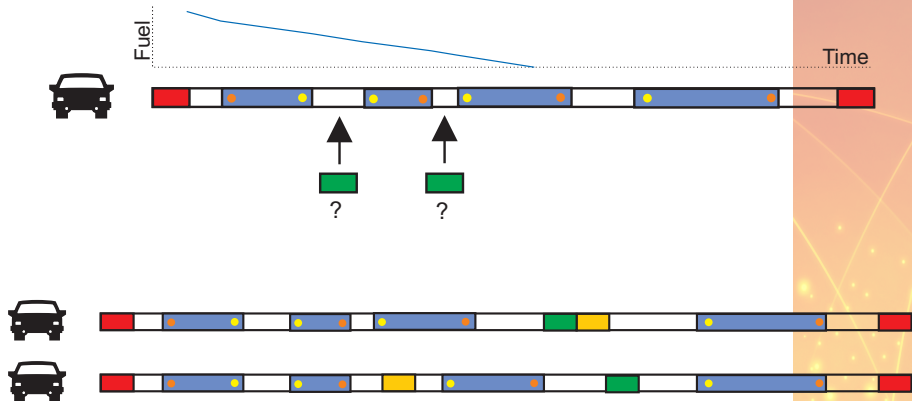
# Constructive Heuristic - Phase 1

- 1 Order jobs based on their priority
- 2 Constructively build schedules - Insert jobs 1 by 1

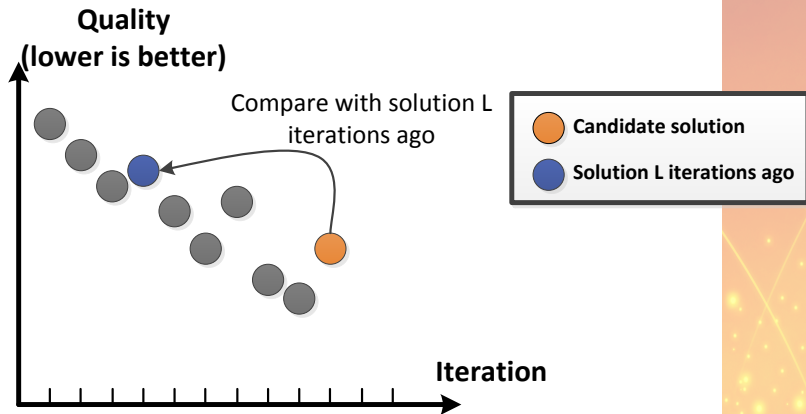


# Constructive Heuristic - Phase 2

## 1 Insert Refuel and Resupply salt jobs



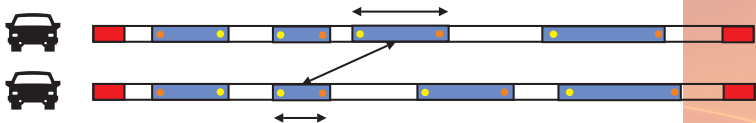
# Late acceptance improvement heuristic



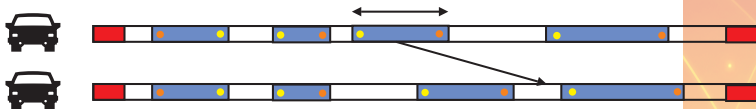
# Late acceptance heuristic

Moves:

1 Swap



2 Remove/insert



Termination:

1 Time limit

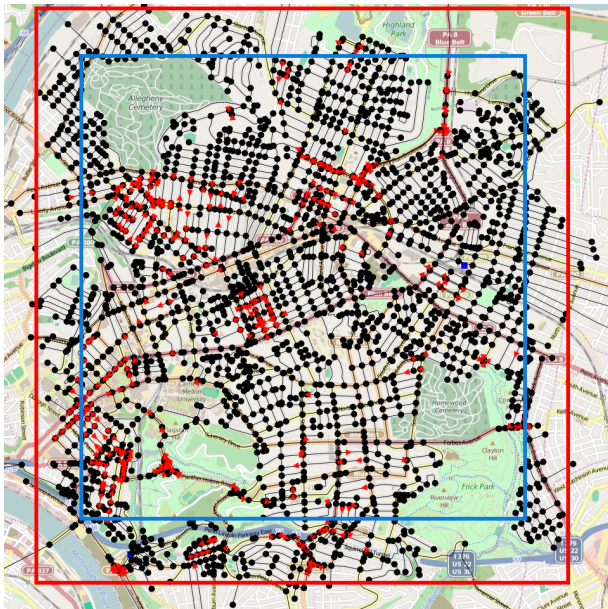
2 Max number of non-improvements



# Experiments - Setup

- 1 Take 2 snapshots from OSM
- 2 Extract graph, pre-process and ensure Strong Connectivity
- 3 Execute routing algorithm

# Routing and Plowing Graph



# Experiments (4/22 instances)

## Kamin St:

- 1 28 intersections
- 2 45 plow jobs
- 3 plowing: 4mi
- 4 bidirectional: 38%

## Residential:

- 1 2441 intersections
- 2 4073 plow jobs
- 3 plowing: 316mi
- 4 bidirectional: 64%

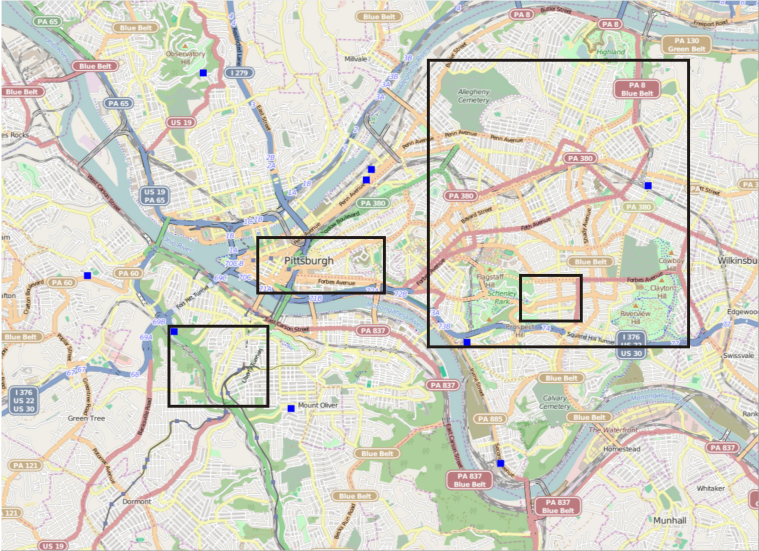
## mt Washington:

- 1 406 intersections
- 2 577 plow jobs
- 3 plowing: 52mi
- 4 bidirectional: 81%

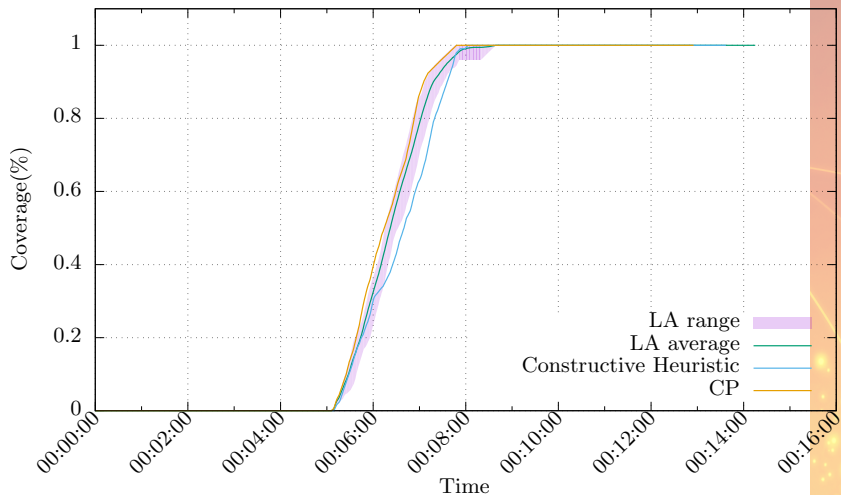
## Downtown:

- 1 345 intersections
- 2 724 plow jobs
- 3 plowing: 38mi
- 4 bidirectional: 38%

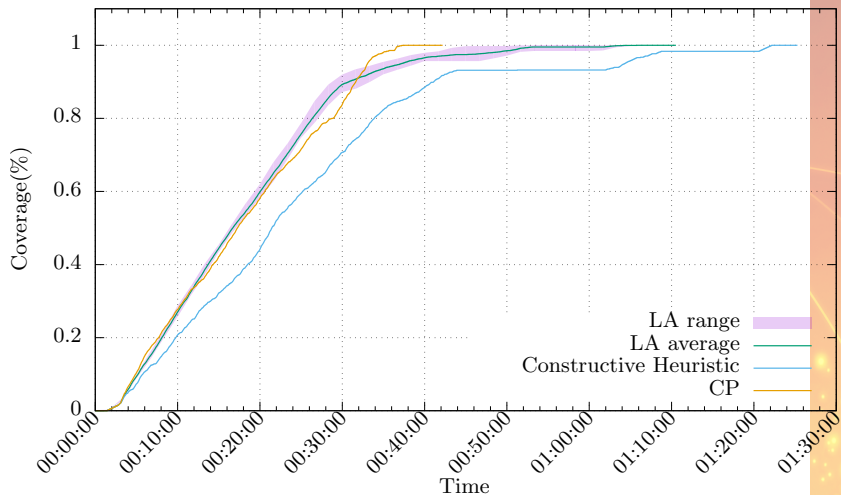
# Experiments



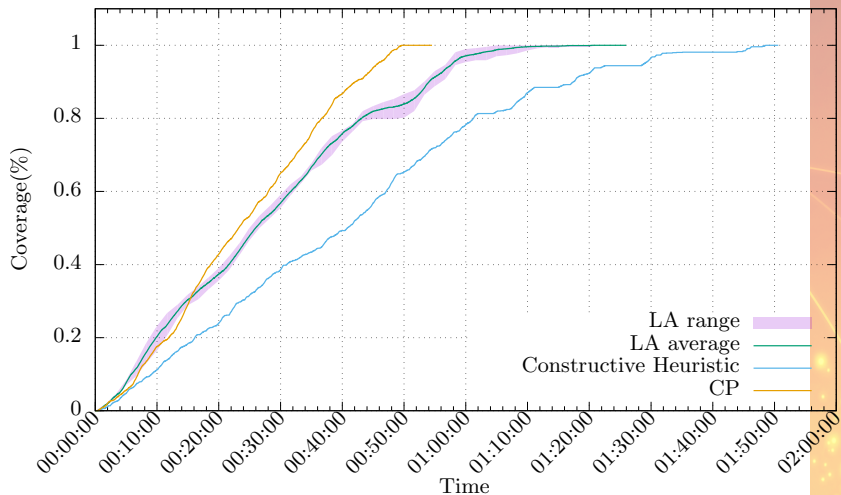
# Experiments - Kamin



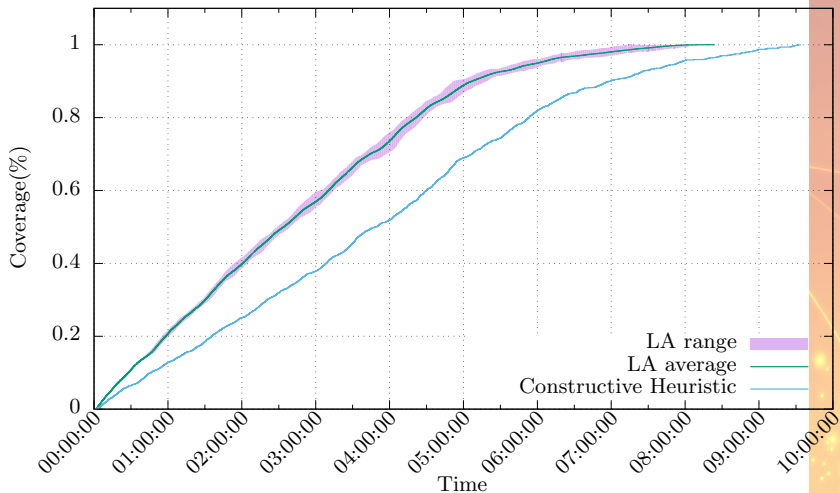
# Experiments - Downtown



# Experiments - Mnt Washington



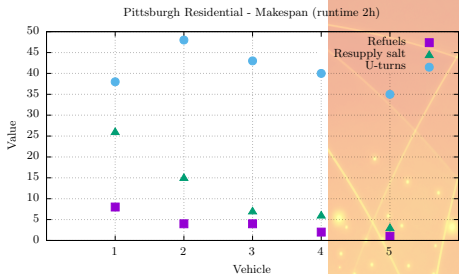
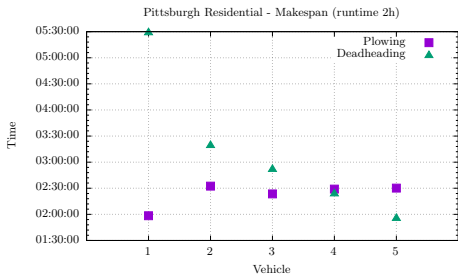
# Experiments - Residential





# Experiments - Residential Pittsburgh solution

- Schedule completion time: 07:38:33



# Summary of preliminary results

- MIP not suitable: bounds are too weak
- CP works well for small instances
- Constructive heuristic finds reasonable solutions in ms.
- LA heuristic produces solutions of consistent quality
- Idea: Improve LA solutions with a CP-Large Neighborhood Search

# Future requirements

- 1 Road priorities
- 2 U-turns
- 3 Vehicle weight/width restrictions on roads
- 4 Efficient construction/updating of distance matrix
- 5 Adaptive system

# Bibliography I

- [1] N. Perrier, A. Langevin, and J. F. Campbell, “A survey of models and algorithms for winter road maintenance. part i: system design for spreading and plowing.” *Computers & Operations Research*, vol. 33, pp. 209–238, 2006.
- [2] ———, “A survey of models and algorithms for winter road maintenance. part ii: system design for snow disposal,” *Computers & Operations Research*, vol. 33, no. 1, pp. 239 – 262, 2006.
- [3] ———, “A survey of models and algorithms for winter road maintenance. part iii: Vehicle routing and depot location for spreading,” *Computers & Operations Research*, vol. 34, no. 1, pp. 211 – 257, 2007.

# Bibliography II

- [4] ———, “A survey of models and algorithms for winter road maintenance. part iv: Vehicle routing and fleet sizing for plowing and snow disposal,” *Computers & Operations Research*, vol. 34, no. 1, pp. 258 – 294, 2007.
- [5] M. A. Salazar-Aguilar, A. Langevin, and G. Laporte, “Synchronized arc routing for snow plowing operations.” *Computers & Operations Research*, vol. 39, no. 7, pp. 1432–1440, 2012.