### Disentangling Vehicle Technology & Self-Selection Effects on Household Alternative Fuel Vehicle Use –

A Tri-variate Copula Based Endogenous Regime Switching Framework

#### **Presenter**:

Behram Wali, Graduate Research Assistant, University of Tennessee, Knoxville

#### **Mentors/Authors**:

Behram Wali, Ph.D. Asad J. Khattak, Ph.D. David L. Greene, Ph.D. Numan Ahmad

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## **Travel Behavior**



"Zones don't travel; people travel!" Slogan, Travel Demand Forecasting Project, 1972

## Conceptual Framework



## Conceptual Framework



## Emerging Transportation Paths (SECAV)



#### **Ownership Model**

1.0 Internal Combustion Engine/Pedal Power

2.0 Electric Vehicles

3.0 Electric Driverless Vehicles

#### **Shared Model**

 1.0 Shared Vehicles
 2.0 Electric Shared Vehicles
 3.0 Shared, Electric, Connected, Automated Vehicles (SECAV)

## Bigger Picture – The Green Mobility of Future



Greene, Khattak, & Wali (2017)

## Advancement of fuel tech - Trends in the U.S.



Source: https://www.hybridcars.com/may-2018-sales-dashboard/

## Advancement of fuel tech - Trends in the U.S.





Source: https://www.afdc.energy.gov/data/10301

## Advancement of fuel tech – Global Trends



## Key Questions

• Mechanisms/factors leading to households purchasing AFVs (plug-in electric /plug-in hybrid vehicles)?

• Vehicle use patterns of AFV households, compared to non-AFV counterparts?



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• Mechanisms/factors leading to households purchasing AFVs (plug-in electric /plug-in hybrid vehicles)?

 Vehicle use patterns of AFV households, compared to non-AFV counterparts?

 Role of "self-selection" & "true" vehicle technology effects?



## **Developing Intuition**



Orange Line: Mean Daily Distance by AFV HH

Green Line: Mean Daily Distance by Non-AFV HH

## **Developing Intuition**



Orange Line: Mean Daily Distance by AFV HH

Green Line: Mean Daily Distance by Non-AFV HH

#### **Feature of the Data (example)**

- Avg. AFV Distance = 4 log-miles
- Avg. Non-AFV Distance = 3.58 log-miles

*Question: Can we conclude that AFV Households travel more?* 

## Having counterfactuals?



Orange Line: AFV (Treated) Mean Green Line: Non-AFV (Untreated) Mean

#### **Feature of the Data (example)**

- Avg. AFV Distance = 17.63 log-miles
- Avg. Non-AFV Distance = 17.16 log-miles

We could have concluded if we had countermeasures...

## Methodological Challenges

- Observational Data (AFV/Non-AFV Households)
- Defining characteristic: Not randomized
- Self-selection bias (Khattak & Rodriguez, 2005; Fan & Khattak, 2009)
- Endogeneity bias (Bhat, 1997; Bhat & Koppelman, 1993; Bhat & Eluru, 2009)

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Quantify the true *"causal effect"* when the selection into being an AFV vs Non-AFV HH is presumably endogenous?

## **Empirical Context**

• 2017 National Household Travel Survey

### National Household Travel Survey

Understanding How People Get from Place to Place



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• 2017 National Household Travel Survey

### National Household Travel Survey

Understanding How People Get from Place to Place





#### Source: NHTS 2017 User Guide







#### Sub\_Master File

Househ old ID	H_Size	Insured	Resid	AFV Dummy	
1	1	1	2	0	
2	2	7	1	1	+
3	1	6	4	0	
Ļ	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	

#### "trippub" File

	Househ	Per_no	Pla_no	travday	Distance	
	1	1	1	2	2	
+	1	2	1	1	3.47	
	2	1	6	4	4	
	Ļ	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	



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	1	2	1	1	3.47
	2	1	6	4	4
	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$	$\downarrow$

#### **Analysis File**

=

## Definitions Used in this Study



Non Plug-in Hybrid Household

Household having "atleast" one non plug-in hybrid vehicle



#### Plug-in Hybrid/Electric Veh Household



## Definitions Used in this Study



Non Plug-in Hybrid Household

Household having "atleast" one non plug-in hybrid vehicle



#### **Plug-in Hybrid/Electric Veh Household**



Households that may own "both" non plug-in hybrid and plug-in hybrid not considered.

- Avoiding "loss of consistency in a greed to gain efficiency"
- A Tri-variate Discrete-Continuous Endogenous Regime Switching Framework







## Mathematical Exposition

• Selection Equation:

$$S_{i} = \begin{cases} 0 \ if \ S_{i}^{*} = z_{i}^{\prime} \gamma + \varepsilon_{si} \leq 0\\ 1 \ if \ S_{i}^{*} = z_{i}^{\prime} \gamma + \varepsilon_{si} > 0 \end{cases}$$

• Endogenous switching model: Two outcomes

$$y_{1i} = x'_{1i}\beta_1 + \varepsilon_{1i} \quad \text{if } S_i = 1$$
$$y_{0i} = x'_{0i}\beta_0 + \varepsilon_{0i} \quad \text{if } S_i = 0$$

- Potential dependencies:
  - $(\varepsilon_{si}, \varepsilon_{1i})$  AND  $(\varepsilon_{si}, \varepsilon_{0i})$

## Copula Approach

$$\aleph(x, y) = C_{\theta}(\{A(x), B(y)\}\)$$

- Stochastic dependence governed by copula:
- Different marginal distributions

## Copula Families & Marginal Distributions

Table 1. Copula functions

Copula name	$C(u_1, u_2; \theta)$	
Product	$u_1 u_2$	
Gaussian	$\Phi_2\{\Phi^{-1}(u_1), \Phi^{-1}(u_2); \theta\}$	
FGM	$u_1u_2\{1+\theta(1-u_1)(1-u_2)\}$	
Plackett	$\frac{r - \sqrt{r^2 - 4u_1 u_2 \theta(\theta - 1)}}{2(\theta - 1)}$	
Archimedean f	family	arphi(t)

AMH	$u_1u_2\left\{1-\theta(1-u_1)(1-u_2)\right\}^{-1}$	$\log\left\{\frac{1-\theta(1-t)}{t}\right\}$
Clayton	$\left(u_1^{-\theta}+u_2^{-\theta}-1\right)^{-1/\theta}$	$ heta^{-1}\left(t^{- heta}-1 ight)$
Frank	$-\theta^{-1}\log\left\{1+\frac{(e^{-\theta u_1}-1)(e^{-\theta u_2}-1)}{(e^{-\theta}-1)}\right\}$	$-\log\left(\frac{e^{-\theta t}-1}{e^{-\theta}-1}\right)$
Gumbel	$\exp\left[-\left\{(-\log u_1)^{\theta} + (-\log u_2)^{\theta}\right\}^{1/\theta}\right]$	$\{-\log(t)\}^{\theta}$
Joe	$1 - \left\{ (\widetilde{u}_1)^{\theta} + (\widetilde{u}_2)^{\theta} - (\widetilde{u}_1\widetilde{u}_2)^{\theta} \right\}^{1/\theta}$	$-\log\left\{1-(1-t)^\theta\right\}$

Notes: For Plackett,  $r = 1 + (\theta - 1)(u_1 + u_2)$ . For Joe,  $\tilde{u}_j = 1 - u_j$ .

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#### **Marginal Distributions**

	Probit	Logit	Student's t
Fs	Y	Y	NA
Fo	Y	Y	Y
F1	Y	Y	Y

**Flexibility:** 63 Unique Model Specifications

## Illustration



Source: Wali, Greene, Khattak, & Liu (2018)

## Illustration



**Clayton Copula** 

Gumbel Copula

Source: Wali, Greene, Khattak, & Liu (2018)

## Results – Key Distributions



## Results – Key Distributions



- N = 5231 households
  - N = 839 PHEV/EV households
  - N = 4,389 Non-plug in hybrid households
- 79 households removed that owned both

## Descriptive Statistics

Not Plug-in Hybrid Vehicles (N = 4389)			Plug-in Hybrid/Electric (N = 842)		
Mean	SD	Min/Max	Mean	SD	Min/Max
3.61	1.12	-1.93/6.93	3.57	1.10	-3.86/6.47
63.71	78.01	0.14/1024.53	59.27	73.15	0.021/651.68
133.65	106.25	2/1093	134.18	101.13	2/739
	Not Plug Mean <b>3.61</b> 63.71 <b>133.65</b>	Not Plug-in Hybrid Ve           Mean         SD <b>3.61</b> 1.12           63.71         78.01 <b>133.65</b> 106.25	Not Plug-in Hybrid Vehicles (N = 4389)MeanSDMin/Max3.611.12-1.93/6.9363.7178.010.14/1024.53133.65106.252/1093	Not Plug-in Hybrid Vehicles (N = 4389)         Plug-in	Not Plug-in Hybrid Vehicles (N = 4389)         Plug-in Hybrid/Elect           Mean         SD         Min/Max         Mean         SD           3.61         1.12         -1.93/6.93         3.57         1.10           63.71         78.01         0.14/1024.53         59.27         73.15           133.65         106.25         2/1093         134.18         101.13

# Descriptive $\frac{1}{\frac{v_{ar}}{Dai}}$

Variables	Not Plug-in Hybrid Vehicles (N = 4389)			Plug-in Hybrid/Electric (N = 842)		
	Mean	SD	Min/Max	Mean	SD	Min/Max
Daily HH Distance (Log-form)	3.61	1.12	-1.93/6.93	3.57	1.10	-3.86/6.47
Household Distance	63.71	78.01	0.14/1024.53	59.27	73.15	0.021/651.68
HH Total Trip Travel Time	133.65	106.25	2/1093	134.18	101.13	2/739
Household Income						
Less than \$10,000	0.01	0.09	0/1	0.01	0.08	0/1
\$10,000 to \$14,999	0.01	0.09	0/1	0.00	0.06	0/1
\$15,000 to \$24,999	0.03	0.16	0/1	0.02	0.12	0/1
\$25,000 to \$34,999	0.04	0.20	0/1	0.02	0.13	0/1
\$35,000 to \$49,999	0.07	0.26	0/1	0.04	0.20	0/1
\$50,000 to \$74,999	0.15	0.36	0/1	0.09	0.29	0/1
\$75,000 to \$99,999	0.17	0.38	0/1	0.11	0.31	0/1
\$100,000 to \$124,999	0.15	0.36	0/1	0.16	0.36	0/1
\$125,000 to \$149,999	0.10	0.30	0/1	0.10	0.30	0/1
\$150,000 to \$199,999	0.11	0.31	0/1	0.15	0.36	0/1
\$200,000 or more	0.13	0.34	0/1	0.28	0.45	0/1

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\$200,000 or more	0.13	0.34	0/1	0.28	0.45	0/1
Housing Status						
Own house	0.87	0.34	0/1	0.91	0.29	0/1
Rent	0.13	0.33	0/1	0.09	0.28	0/1
Number of employed members	1.27	0.93	0/6	1.36	0.89	0/5
Number of vehicles	2.35	1.10	1/10	2.68	1.24	1/12
Count of HH trips on travel day	9.52	6.06	1/60	10.19	6.51	2/42

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Number of vehicles	2.35	1.10	1/10	2.68	1.24	1/12
Count of HH trips on travel day	9.52	6.06	1/60	10.19	6.51	2/42
Life cycle classification of HH						
2+ adults, retired, no children	0.28	0.45	0/1	0.24	0.43	0/1
Daily bike use	0.02	0.13	0/1	0.03	0.17	0/1
Daily bus use	0.01	0.11	0/1	0.01	0.08	0/1
Daily smartphone use to access internet	0.81	0.40	0/1	0.88	0.33	0/1
Daily internet use	0.96	0.18	0/1	0.99	0.11	0/1
Travel is NOT a financial burden	0.09	0.28	0/1	0.16	0.36	0/1

	Marginal Distributions							
Copula Specification	Type 1	Type 2	Type 3	Type 4	Type 5	Туре б	Type 7	
Hybrid Copulas								
Product	19810.87	19726.34	19727.63	19570.75	19735.08	19727.36	19733.52	
Gaussian	19820.2	19734.93	19736.18	19565.34	19743.81	19734.89	19741.29	
FGM	19782.04	19733.04	19734.2	19559.4	19741.61	19729.17	19735.43	
Plackett	19741.8	19735.41	19736.6	19551.2	19736.73	19728.42	19727.42	
Archimedian Copulas								
Ali-Mikhael-Haq	19788.04	19733.01	19734.24	19560.87	19741.67	19730.62	19736.82	
Clayton	19827.99	19743.47		19574.73				
Frank			19736.27	19554.91	19742.05	19726.63	19731.09	
Gumbel	19786.98	19736.97	19738.08	19563.35	19735.63	19742.95	19739.46	
Joe	19788.28	19716.21	19717.3	19551.72	19722.83	19723.36	19727.82	

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#### DIFFERENT MARGINAL DISTRIBUTIONS ARE:

- normal/normal/normal
- 2. logistic/logistic/logistic
- 3. normal/logsitic/logistic
- 4. normal/t-dist/t-dist
- normal/logistic/t-dist
- 6. normal/t-dist/logistic
- logistic/t-dist/t-dist

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- Red indicates the ICOMP statistic for traditional Gaussion copula model with normal margins
- Green indicates the best-fit Plackett copula model with Type 4 marginal distributions

1 — /\* 2 — 3 — 4 — 5 — 6 — 7 — 8 — 9 —

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• Green indicates the best-fit Plackett-Joe copula model with Type 4 marginal distributions

	Type 4 Margins				
Regime 0: Plackett	AIC	ICOMP			
Regime 1: Plackett	19551.22	19728.4			
Regime 1: Product	19558.02	19728.64			
Regime 1: Gaussian	19552.03	19729.21			
Regime 1: FGM	19559.91	19737.09			
Regime 1: AMH	19559.91	19737.09			
Regime 1: Clayton	19560.02	19737.21			
Regime 1: Frank	19560.02	19737.2			
Regime 1: Gumbel	19554.76	19731.94			
Regime 1: Joe	19547.8	19724.98			
Regime 1: Plackett					
Regime 1: Plackett	19551.22	19728.4			
Regime 0: Product	19564.54	19735.16			
Regime 0: Gaussian	19565.02	19742.2			
Regime 0: FGM	19550.77	19727.96			
Regime 0: AMH	19552.38	19729.57			
Regime 0: Clayton	19566.54	19743.72			
Regime 0: Frank	19547.87	19725.05			
Regime 0: Gumbel	19559.2	19736.38			
Regime 0: Joe	19554.54	19731.72			

Variables	Sele Equati	Selection Equation (1/0)		
Constant	<b>p</b>	12.0C		
Constant	-1.84	-12.96		
Household Income				
Less than \$10,000				
\$15,000 to \$24,999				
\$25,000 to \$34,999				
High income (1 if income > 100,000)	0.41	9.40		
Housing Status				
Own house	0.14	2.28		
Rent				
Life cycle classification of HH				
2+ adults, retired, no children				
Number of employed members				
Count of HH trips on travel day				
Three or more vehicles				
Daily bike use	0.28	2.01		
Daily smartphone use to access internet	0.18	3.16		
Daily internet use	0.33	2.31		
Travel is NOT a financial burden	0.20	3.38		
Identification/Copula Parameters				
Copula device	-			
Marginal distribution	Norma	l/Probit		
Sigma (Regimes Specific)				
Dependence (Regime Specific)				
Kendall Tau				
DOF - t marginal distributions				

Variables	Sele	ction	Regime 0 (Not Plug-in		
	Equati	on (1/0)	H	ybrid)	
	β	t-stat	β	t-stat	
Constant	-1.84	-12.96	3.04	77.69	
Household Income					
Less than \$10,000			-0.41	-2.37	
\$15,000 to \$24,999			-0.44	-4.51	
\$25,000 to \$34,999			-0.26	-3.26	
High income (1 if income $> 100,000$ )	0.41	9.40			
Housing Status					
Own house	0.14	2.28			
Rent			-0.22	-4.47	
Life cycle classification of HH					
2+ adults, retired, no children			-0.14	-3.97	
Number of employed members					
Count of HH trips on travel day			0.06	23.50	
Three or more vehicles					
Daily bike use	0.28	2.01	-0.59	-4.79	
Daily smartphone use to access internet	0.18	3.16			
Daily internet use	0.33	2.31			
Travel is NOT a financial burden	0.20	3.38			
Identification/Copula Parameters					
Copula device	-			ett copula	
Marginal distribution	Normal/Probit		t-dis	tribution	
Sigma (Regimes Specific)			0.98	43.60	
Dependence (Regime Specific)			0.30	4.14	
Kendall Tau			-	0.26	
DOF - t marginal distributions				14.93	

Variables	Sele	ection	<b>Regime 0 (Not Plug-in</b>		
	Equati	ion (1/0)	H	ybrid)	
	β	t-stat	β	t-stat	
Constant	-1.84	-12.96	3.04	77.69	
Household Income					
Less than \$10,000			-0.41	-2.37	
\$15,000 to \$24,999			-0.44	-4.51	
\$25,000 to \$34,999			-0.26	-3.26	
High income (1 if income $> 100,000$ )	0.41	9.40			
Housing Status					
Own house	0.14	2.28			
Rent			-0.22	-4.47	
Life cycle classification of HH					
2+ adults, retired, no children			-0.14	-3.97	
Number of employed members					
Count of HH trips on travel day			0.06	23.50	
Three or more vehicles					
Daily bike use	0.28	2.01	-0.59	-4.79	
Daily smartphone use to access internet	0.18	3.16			
Daily internet use	0.33	2.31			
Travel is NOT a financial burden	0.20	3.38			
Identification/Copula Parameters					
Copula device	-			ett copula	
Marginal distribution	Norma	Normal/Probit		tribution	
Sigma (Regimes Specific)			0.98	43.60	
Dependence (Regime Specific)			0.30	4.14	
Kendall Tau				·0.26	
DOF - t marginal distributions				14.93	

Variables	Selection Equation (1/0)		Regime 0 (Not Plug-in Hybrid)		Regime 1 (Plug-in Hybrid/Electric)	
	β	t-stat	β	t-stat	β	t-stat
Constant	-1.84	-12.96	3.04	77.69	1.75	11.45
Household Income						
Less than \$10,000			-0.41	-2.37		
\$15,000 to \$24,999			-0.44	-4.51		
\$25,000 to \$34,999			-0.26	-3.26		
High income (1 if income $> 100,000$ )	0.41	9.40			0.53	5.96
Housing Status						
Own house	0.14	2.28				
Rent			-0.22	-4.47		
Life cycle classification of HH						
2+ adults, retired, no children			-0.14	-3.97		
Number of employed members					0.14	3.30
Count of HH trips on travel day			0.06	23.50	0.04	6.86
Three or more vehicles					0.32	3.50
Daily bike use	0.28	2.01	-0.59	-4.79	-0.29	-1.83
Daily smartphone use to access internet	0.18	3.16				
Daily internet use	0.33	2.31				
Travel is NOT a financial burden	0.20	3.38				
Identification/Copula Parameters						
Copula device	-		Plack	ett copula	Joe co	pula
Marginal distribution	Normal/Probit		t-dis	tribution	t-distrib	oution
Sigma (Regimes Specific)			0.98	43.60	0.89	15.05
Dependence (Regime Specific)			0.30	4.14	1.81	14.57
Kendall Tau			-	·0.26	0.31	
DOF - t marginal distributions			1	14.93		38

Variables	Selection Equation (1/0)		Regime 0 (Not Plug-in Hybrid)		Regime 1 (Plug-in Hybrid/Electric)	
	β	t-stat	β	t-stat	β	t-stat
Constant	-1.84	-12.96	3.04	77.69	1.75	11.45
Household Income						
Less than \$10,000			-0.41	-2.37		
\$15,000 to \$24,999			-0.44	-4.51		
\$25,000 to \$34,999			-0.26	-3.26		
High income (1 if income $> 100,000$ )	0.41	9.40			0.53	5.96
Housing Status						
Own house	0.14	2.28				
Rent			-0.22	-4.47		
Life cycle classification of HH						
2+ adults, retired, no children			-0.14	-3.97		
Number of employed members					0.14	3.30
Count of HH trips on travel day			0.06	23.50	0.04	6.86
Three or more vehicles					0.32	3.50
Daily bike use	0.28	2.01	-0.59	-4.79	-0.29	-1.83
Daily smartphone use to access internet	0.18	3.16				
Daily internet use	0.33	2.31				
Travel is NOT a financial burden	0.20	3.38				
Identification/Copula Parameters						
Copula device	-		Plack	ett copula	Joe co	pula
Marginal distribution	Normal/Probit		t-dis	tribution	t-distrik	oution
Sigma (Regimes Specific)			0.98	43.60	0.89	15.05
Dependence (Regime Specific)			0.30	4.14	1.81	14.57
Kendall Tau			-	-0.26	0.31	
DOF - t marginal distributions			1	14.93	10.3	8

Variables	Selection Equation (1/0)		Regime 0 (Not Plug-in Hybrid)		Regime 1 (Plug-in Hybrid/Electric)		
	β	t-stat	β	t-stat	β	t-stat	
Constant	-1.84	-12.96	3.04	77.69	1.75	11.45	
Household Income							
Less than \$10,000			-0.41	-2.37			
\$15,000 to \$24,999			-0.44	-4.51			
\$25,000 to \$34,999			-0.26	-3.26			
High income (1 if income $> 100,000$ )	0.41	9.40			0.53	5.96	
Housing Status							
Own house	0.14	2.28					
Rent			-0.22	-4.47			
Life cycle classification of HH							
2+ adults, retired, no children			-0.14	-3.97			
Number of employed members					0.14	3.30	
Count of HH trips on travel day			0.06	23.50	0.04	6.86	
Three or more vehicles					0.32	3.50	
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Daily smartphone use to access internet	0.18	3.16					
Daily internet use	0.33	2.31					
Travel is NOT a financial burden	0.20	3.38					
Identification/Copula Parameters							
Copula device	-		Plack	ett copula	Joe co	pula	
Marginal distribution	Normal/Probit		t-dis	tribution	t-distrib	oution	
Sigma (Regimes Specific)			0.98	43.60	0.89	15.05	
Dependence (Regime Specific)			0.30	4.14	1.81	14.57	
Kendall Tau			-	0.26	0.31		
DOF - t marginal distributions			1	14.93		10.38	

## Treatment Effects

	Trivariate-Joint	Trivariate-Joint	Trivariate-Joint
	Normality	Switching	Switching
<b>Treatment Effects</b>	Gaussian copulas	Plackett-Joe Copulas	Plackett-Joe Copulas
			Normal/t-distribution/t-
	Normal margins	Normal margins	distribution
Average Treatment Effect			
(ATE) in log-miles	-0.384	-1.38	-0.929

## Closure

- .... Plug-in Hybrid/EV households travel on-average significantly less distance than their counterparts.
- Presence of self-selection effects.
- Standard approaches (if assumptions violated): provide misleading effects.
- Joint estimation of the behavioral system: Better than standard approaches.
- Given joint estimation, not only different marginal distributions, but also dependence structures yield much different effects.
- Future Work:
  - Analyze households that have both HEVs and PHEVs (Extend methodological framework)
  - ≻ Link HEV- and PHEV-VMT to each of the vehicle type
  - ≻ Look into vehicle use of conventional vehicles vis-à-vis AFVs



## Thank YOU

Behram Wali bwali@vols.utk.edu www.bwali.weebly.com













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