## Disentangling Vehicle Technology \& Self-Selection Effects on Household Alternative Fuel Vehicle Use -

A Tri-variate Copula Based Endogenous Regime Switching Framework

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## Travel Behavior


"Zones don't travel; people travel!" Slogan, Travel Demand
Forecasting Project, 1972

## Conceptual Framework



## Conceptual Framework



## Emerging Transportation Paths (SECAV)

| Owned Automated |  |
| :---: | :---: |
| Does Not Meet City Goals Owned Conventional |  |
| Ownership Model | Shared Model |
| 1.0 Internal Combustion Engine/Pedal Power | 1.0 Shared Vehicles |
| 2.0 Electric Vehicles | 2.0 Electric Shared Vehicles |
| 3.0 Electric Driverless Vehicles | 3.0 Shared, Electric, Connected, Automated Vehicles (SECAV) |

## Bigger Picture - The Green Mobility of Future



Greene, Khattak, \& Wali (2017)

## Advancement of fuel tech - Trends in the U.S.




## Advancement of fuel tech - Trends in the U.S.

## Advancement of fuel tech - Global Trends



## Key Questions

- Mechanisms/factors leading to households purchasing AFVs (plug-in electric /plug-in hybrid vehicles)?
- Vehicle use patterns of AFV households, compared to nonAFV counterparts?


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- Mechanisms/factors leading to households purchasing AFVs (plug-in electric /plug-in hybrid vehicles)?
- Vehicle use patterns of AFV households, compared to nonAFV counterparts?
- Role of "self-selection" \& "true" vehicle technology effects?


## Developing Intuition



Orange Line: Mean Daily Distance by AFV HH
Green Line: Mean Daily Distance by Non-AFV HH

## Developing Intuition



## Feature of the Data (example)

- Avg. AFV Distance $=4$ log-miles
- Avg. Non-AFV Distance $=3.58$ log-miles

Question: Can we conclude that AFV Households travel more?

Orange Line: Mean Daily Distance by AFV HH
Green Line: Mean Daily Distance by Non-AFV HH

## Having counterfactuals?



## Feature of the Data (example)

- Avg. AFV Distance $=17.63$ log-miles
- Avg. Non-AFV Distance $=17.16$ log-miles

We could have concluded if we had countermeasures...

## Methodological Challenges

- Observational Data (AFV/Non-AFV Households)
- Defining characteristic: Not randomized
- Self-selection bias (Khatak \& Rodriguez, 2005; Fan \& Khattak, 2009)
- Endogeneity bias (Bhat, 1997; Bhat \& Koppelman, 1993; Bhat \& Eluru, 2009)


## Methodological Challenges

- Observational Data (AFV/Non-AFV Households)
- Defining characteristic: Not randomized
- Self-selection bias (Khattak \& Rodriguez, 2005; Fan \& Khattak, 2009)
- Endogeneity bias (Bhat, 1997; Bhat \& Koppelman, 1993; Bhat \& Eluru, 2009)

Quantify the true "causal effect" when the selection into being an AFV vs Non-AFV HH is presumably endogenous?

## Empirical Context

- 2017 National Household Travel Survey

National Household Travel Survey

Understanding How People Get from Place to Place

## Empirical Context

## National Household Travel Survey

Understanding How People Get from Place to Place

- 2017 National Household Travel Survey

For Each Person:

- Age
- Sex
- Driver status
- Worker status
- Annual miles

Daily Travel Data:

- Origin and destination
- Time trip started and ended
- Distance
- Means of transportation:

1. vehicle type
2. if household vehicle, which one
3. if transit, wait time
4. if transit, access and egress mode*

For Each Vehicle:

- Make

Detailed purpose

- Number of passengers on trip
- Most recent trip for non-travelers (date)
- Age (year)
- Years owned
- Odometer Reading


## Data Structure

"vehpub" File
$\left.\begin{array}{|cccc|}\hline \text { Household ID } & \text { Veh ID } & \text { Fuel Type } & \text { Type } \\ 1 & 1 & \text { G } & \\ 1 & 2 & \mathrm{H} & \mathrm{EV} \\ 1 & 3 & \mathrm{D} & \\ 2 & 1 & \downarrow & \downarrow \\ \downarrow & \downarrow & \downarrow & \downarrow\end{array}\right)$

## Data Structure



## Data Structure



Sub_Master File


## Data Structure



Sub_Master File


$$
=\quad \text { Analysis File }
$$

## Definitions Used in this Study



Non Plug-in Hybrid Household


Household having "atleast" one non plug-in hybrid vehicle


Plug-in Hybrid/Electric Veh Household


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Non Plug-in Hybrid Household


Household having "atleast" one non plug-in hybrid vehicle


Plug-in Hybrid/Electric Veh Household
Household having "at-
least" one plug-in
hybrid/electric vehicle

Households that may own "both" non plug-in hybrid and plug-in hybrid not considered.

## Methodological Approach

- Avoiding "loss of consistency in a greed to gain efficiency"
- A Tri-variate Discrete-Continuous Endogenous Regime Switching Framework


## Methodological Approach



## Methodological Approach



## Methodological Approach



## Mathematical Exposition

- Selection Equation:

$$
S_{i}=\left\{\begin{array}{l}
0 \text { if } S_{i}^{*}=z_{i}^{\prime} \gamma+\varepsilon_{s i} \leq 0 \\
1 \text { if } S_{i}^{*}=z_{i}^{\prime} \gamma+\varepsilon_{s i}>0
\end{array}\right.
$$

- Endogenous switching model: Two outcomes

$$
\begin{array}{cc}
y_{1 i}=x_{1 i}^{\prime} \beta_{1}+\varepsilon_{1 i} & \text { if } S_{i}=1 \\
y_{0 i}=x_{0 i}^{\prime} \beta_{0}+\varepsilon_{0 i} & \text { if } S_{i}=0
\end{array}
$$

- Potential dependencies:
- $\left(\varepsilon_{s i}, \varepsilon_{1 i}\right)$ AND $\left(\varepsilon_{s i}, \varepsilon_{0 i}\right)$


## Copula Approach

$$
\aleph(x, y)=C_{\theta}(\{A(x), B(y)\}
$$

- Stochastic dependence governed by copula:
- Different marginal distributions


## Copula Families \& Marginal Distributions

## Table 1. Copula functions

| Copula name | $C\left(u_{1}, u_{2} ; \theta\right)$ |
| :--- | :--- |
| Product | $u_{1} u_{2}$ |
| Gaussian | $\Phi_{2}\left\{\Phi^{-1}\left(u_{1}\right), \Phi^{-1}\left(u_{2}\right) ; \theta\right\}$ |
| FGM | $u_{1} u_{2}\left\{1+\theta\left(1-u_{1}\right)\left(1-u_{2}\right)\right\}$ |
| Plackett | $\frac{r-\sqrt{r^{2}-4 u_{1} u_{2} \theta(\theta-1)}}{2(\theta-1)}$ |

Archimedean family
$\varphi(t)$

| AMH | $u_{1} u_{2}\left\{1-\theta\left(1-u_{1}\right)\left(1-u_{2}\right)\right\}^{-1}$ | $\log \left\{\frac{1-\theta(1-t)}{t}\right\}$ |
| :--- | :--- | :--- |
| Clayton | $\left(u_{1}^{-\theta}+u_{2}^{-\theta}-1\right)^{-1 / \theta}$ | $\theta^{-1}\left(t^{-\theta}-1\right)$ |
| Frank | $-\theta^{-1} \log \left\{1+\frac{\left(e^{-\theta u_{1}}-1\right)\left(e^{-\theta u_{2}}-1\right)}{\left(e^{-\theta}-1\right)}\right\}$ | $-\log \left(\frac{e^{-\theta t}-1}{e^{-\theta}-1}\right)$ |
| Gumbel | $\exp \left[-\left\{\left(-\log u_{1}\right)^{\theta}+\left(-\log u_{2}\right)^{\theta}\right\}^{1 / \theta}\right]$ | $\{-\log (t)\}^{\theta}$ |
| Joe | $1-\left\{\left(\widetilde{u}_{1}\right)^{\theta}+\left(\widetilde{u}_{2}\right)^{\theta}-\left(\widetilde{u}_{1} \widetilde{u}_{2}\right)^{\theta}\right\}^{1 / \theta}$ | $-\log \left\{1-(1-t)^{\theta}\right\}$ |

[^0]
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|  |  | $\varphi(t)$ |
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| Frank | $-\theta^{-1} \log \left\{1+\frac{\left(e^{-\theta u_{1}}-1\right)\left(e^{-\theta u_{2}}-1\right)}{\left(e^{-\theta}-1\right)}\right\}$ |  |
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## Marginal Distributions

|  | Probit | Logit | Student's t |
| :--- | :---: | :---: | :---: |
| Fs | $Y$ | $Y$ | $N A$ |
| Fo $_{0}$ | $Y$ | $Y$ | $Y$ |
| F $_{1}$ | $Y$ | $Y$ | $Y$ |

Flexibility:
63 Unique Model Specifications

## Illustration

Source: Wali, Greene, Khattak, \& Liu (2018)






## Illustration



## Results - Key Distributions





## Results - Key Distributions





- $\mathrm{N}=5231$ households
- $\mathrm{N}=839$ PHEV/EV households
- $N=4,389$ Non-plug in hybrid households
- 79 households removed that owned both

|  | Variables | Not Plug-in Hybrid Vehicles ( $\mathrm{N}=4389$ ) |  |  | Plug-in Hybrid/Electric ( $\mathrm{N}=\mathbf{8 4 2 \text { ) }}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| tatistics |  | Mean | SD | Min/Max | Mean | SD | Min/Max |
|  | Daily HH Distance (Log-form) | 3.61 | 1.12 | -1.93/6.93 | 3.57 | 1.10 | -3.86/6.47 |
|  | Household Distance | 63.71 | 78.01 | 0.14/1024.53 | 59.27 | 73.15 | 0.021/651.68 |
|  | HH Total Trip Travel Time | 133.65 | 106.25 | 2/1093 | 134.18 | 101.13 | 2/739 |

Descriptive

|  | Variables | Not Plug-in Hybrid Vehicles ( $\mathrm{N}=4389$ ) |  |  | Plug-in Hybrid/Electric ( $\mathrm{N}=\mathbf{8 4 2 \text { ) }}$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TתTSES |  | Mean | SD | Min/Max | Mean | SD | Min/Max |
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|  | HH Total Trip Travel Time | 133.65 | 106.25 | 2/1093 | 134.18 | 101.13 | 2/739 |
|  | Household Income |  |  |  |  |  |  |
|  | Less than \$10,000 | 0.01 | 0.09 | 0/1 | 0.01 | 0.08 | 0/1 |
|  | \$10,000 to \$14,999 | 0.01 | 0.09 | 0/1 | 0.00 | 0.06 | 0/1 |
|  | \$15,000 to \$24,999 | 0.03 | 0.16 | 0/1 | 0.02 | 0.12 | 0/1 |
|  | \$25,000 to \$34,999 | 0.04 | 0.20 | 0/1 | 0.02 | 0.13 | 0/1 |
|  | \$35,000 to \$49,999 | 0.07 | 0.26 | 0/1 | 0.04 | 0.20 | 0/1 |
|  | \$50,000 to \$74,999 | 0.15 | 0.36 | 0/1 | 0.09 | 0.29 | 0/1 |
|  | \$75,000 to \$99,999 | 0.17 | 0.38 | 0/1 | 0.11 | 0.31 | 0/1 |
|  | \$100,000 to \$124,999 | 0.15 | 0.36 | 0/1 | 0.16 | 0.36 | 0/1 |
|  | \$125,000 to \$149,999 | 0.10 | 0.30 | 0/1 | 0.10 | 0.30 | 0/1 |
|  | \$150,000 to \$199,999 | 0.11 | 0.31 | 0/1 | 0.15 | 0.36 | 0/1 |
|  | \$200,000 or more | 0.13 | 0.34 | 0/1 | 0.28 | 0.45 | 0/1 |

Descriptive Statistics

## Descriptive Statistics

| Variables | Not Plug-in Hybrid Vehicles ( $\mathrm{N}=\mathbf{4 3 8 9}$ ) |  |  | Plug-in Hybrid/Electric ( $\mathrm{N}=842$ ) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mean | SD | Min/Max | Mean | SD | Min/Max |
| Daily HH Distance (Log-form) | 3.61 | 1.12 | -1.93/6.93 | 3.57 | 1.10 | -3.86/6.47 |
| Household Distance | 63.71 | 78.01 | 0.14/1024.53 | 59.27 | 73.15 | 0.021/651.68 |
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| \$125,000 to \$149,999 | 0.10 | 0.30 | 0/1 | 0.10 | 0.30 | 0/1 |
| \$150,000 to \$199,999 | 0.11 | 0.31 | 0/1 | 0.15 | 0.36 | 0/1 |
| \$200,000 or more | 0.13 | 0.34 | 0/1 | 0.28 | 0.45 | 0/1 |
| Housing Status |  |  |  |  |  |  |
| Own house | 0.87 | 0.34 | 0/1 | 0.91 | 0.29 | 0/1 |
| Rent | 0.13 | 0.33 | 0/1 | 0.09 | 0.28 | 0/1 |
| Number of employed members | 1.27 | 0.93 | 0/6 | 1.36 | 0.89 | 0/5 |
| Number of vehicles | 2.35 | 1.10 | 1/10 | 2.68 | 1.24 | 1/12 |
| Count of HH trips on travel day | 9.52 | 6.06 | 1/60 | 10.19 | 6.51 | 2/42 |

## Descriptive

 Statistics| Variables | Not Plug-in Hybrid Vehicles ( $\mathrm{N}=4389$ ) |  |  | Plug-in Hybrid/Electric ( $\mathrm{N}=842$ ) |  |  |
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| Housing Status |  |  |  |  |  |  |
| Own house | 0.87 | 0.34 | 0/1 | 0.91 | 0.29 | 0/1 |
| Rent | 0.13 | 0.33 | 0/1 | 0.09 | 0.28 | 0/1 |
| Number of employed members | 1.27 | 0.93 | 0/6 | 1.36 | 0.89 | 0/5 |
| Number of vehicles | 2.35 | 1.10 | 1/10 | 2.68 | 1.24 | 1/12 |
| Count of HH trips on travel day | 9.52 | 6.06 | 1/60 | 10.19 | 6.51 | 2/42 |
| Life cycle classification of HH |  |  |  |  |  |  |
| 2+ adults, retired, no children | 0.28 | 0.45 | 0/1 | 0.24 | 0.43 | 0/1 |
| Daily bike use | 0.02 | 0.13 | 0/1 | 0.03 | 0.17 | 0/1 |
| Daily bus use | 0.01 | 0.11 | 0/1 | 0.01 | 0.08 | 0/1 |
| Daily smartphone use to access internet | 0.81 | 0.40 | 0/1 | 0.88 | 0.33 | 0/1 |
| Daily internet use | 0.96 | 0.18 | 0/1 | 0.99 | 0.11 | 0/1 |
| Travel is NOT a financial burden | 0.09 | 0.28 | 0/1 | 0.16 | 0.36 | 0/1 |

## Model Selection (ICOMP)

|  | Marginal Distributions |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Copula Specification | Type 1 | Type 2 | Type 3 | Type 4 | Type 5 | Type 6 | Type 7 |  |
| Hybrid Copulas |  |  |  |  |  |  |  |  |
| Product | 19810.87 | 19726.34 | 19727.63 | 19570.75 | 19735.08 | 19727.36 | 19733.52 |  |
| Gaussian | $\mathbf{1 9 8 2 0 . 2}$ | 19734.93 | 19736.18 | 19565.34 | 19743.81 | 19734.89 | 19741.29 |  |
| FGM | 19782.04 | 19733.04 | 19734.2 | 19559.4 | 19741.61 | 19729.17 | 19735.43 |  |
| Plackett | 19741.8 | 19735.41 | 19736.6 | $\mathbf{1 9 5 5 1 . 2}$ | 19736.73 | 19728.42 | 19727.42 |  |
| Archimedian Copulas |  |  |  |  |  |  |  |  |
| Ali-Mikhael-Haq | 19788.04 | 19733.01 | 19734.24 | 19560.87 | 19741.67 | 19730.62 | 19736.82 |  |
| Clayton | 19827.99 | 19743.47 | --- | 19574.73 | --- | --- | -- |  |
| Frank | --- | -- | 19736.27 | 19554.91 | 19742.05 | 19726.63 | 19731.09 |  |
| Gumbel | 19786.98 | 19736.97 | 19738.08 | 19563.35 | 19735.63 | 19742.95 | 19739.46 |  |
| Joe | 19788.28 | 19716.21 | 19717.3 | 19551.72 | 19722.83 | 19723.36 | 19727.82 |  |

## Model Selection (ICOMP)

|  | Marginal Distributions |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Copula Specification | Type 1 | Type 2 | Type 3 | Type 4 | Type 5 | Type 6 | Type 7 |
| Hybrid Copulas |  |  |  |  |  |  |  |
| Product | 19810.87 | 19726.34 | 19727.63 | 19570.75 | 19735.08 | 19727.36 | 19733.52 |
| Gaussian | $\mathbf{1 9 8 2 0 . 2}$ | 19734.93 | 19736.18 | 19565.34 | 19743.81 | 19734.89 | 19741.29 |
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## Model Selection (ICOMP)

|  | Marginal Distributions |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Copula Specification | Type 1 | Type 2 | Type 3 | Type 4 | Type 5 | Type 6 | Type 7 |
| Hybrid Copulas |  |  |  |  |  |  |  |
| Product | 19810.87 | 19726.34 | 19727.63 | 19570.75 | 19735.08 | 19727.36 | 19733.52 |
| Gaussian | 19820.2 | 19734.93 | 19736.18 | 19565.34 | 19743.81 | 19734.89 | 19741.29 |
| FGM | 19782.04 | 19733.04 | 19734.2 | 19559.4 | 19741.61 | 19729.17 | 19735.43 |
| Plackett | 19741.8 | 19735.41 | 19736.6 | 19551.2 | 19736.73 | 19728.42 | 19727.42 |
| Archimedian Copulas |  |  |  |  |  |  |  |
| Ali-Mikhael-Haq | 19788.04 | 19733.01 | 19734.24 | 19560.87 | 19741.67 | 19730.62 | 19736.82 |
| Clayton | 19827.99 | 19743.47 | --- | 19574.73 | --- | --- | --- |
| Frank | --- | --- | 19736.27 | 19554.91 | 19742.05 | 19726.63 | 19731.09 |
| Gumbel | 19786.98 | 19736.97 | 19738.08 | 19563.35 | 19735.63 | 19742.95 | 19739.46 |
| Joe | 19788.28 | 19716.21 | 19717.3 | 19551.72 | 19722.83 | 19723.36 | 19727.82 |

- Red indicates the ICOMP statistic for traditional Gaussion copula model with normal margins
- Green indicates the best-fit Plackett copula model with Type 4 marginal distributions


## DIFFERENT MARGINAL DISTRIBUTIONS ARE:

l. normal/normal/normal
2. logistic/logistic/logistic
3. normal/logsitic/logistic
4. normal/t-dist/t-dist
5. normal/logistic/t-dist
6. normal/t-dist/logistic
7. logistic/t-dist/t-dist

## Model Selection (ICOMP)

|  | Type 4 Margins |  |
| :--- | :---: | :---: |
| Regime 0: Plackett | AIC | ICOMP |
| Regime 1: Plackett | 19551.22 | 19728.4 |
| Regime 1: Product | 19558.02 | 19728.64 |
| Regime 1: Gaussian | 19552.03 | 19729.21 |
| Regime 1: FGM | 19559.91 | 19737.09 |
| Regime 1: AMH | 19559.91 | 19737.09 |
| Regime 1: Clayton | 19560.02 | 19737.21 |
| Regime 1: Frank | 19560.02 | 19737.2 |
| Regime 1: Gumbel | 19554.76 | 19731.94 |
| Regime 1: Joe | 19547.8 | 19724.98 |
| Regime 1: Plackett |  |  |
| Regime 1: Plackett | 19551.22 | 19728.4 |
| Regime 0: Product | 19564.54 | 19735.16 |
| Regime 0: Gaussian | 19565.02 | 19742.2 |
| Regime 0: FGM | 19550.77 | 19727.96 |
| Regime 0: AMH | 19552.38 | 19729.57 |
| Regime 0: Clayton | 19566.54 | 19743.72 |
| Regime 0: Frank | 19547.87 | 19725.05 |
| Regime 0: Gumbel | 19559.2 | 19736.38 |
| Regime 0: Joe | 19554.54 | 19731.72 |

## Estimation Results

| Variables | Selection Equation (1/0) |  |
| :---: | :---: | :---: |
|  | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 |
| Household Income |  |  |
| Less than \$10,000 | --- | --- |
| \$15,000 to \$24,999 | --- | --- |
| \$25,000 to \$34,999 | --- | --- |
| High income ( 1 if income > 100,000) | 0.41 | 9.40 |
| Housing Status |  |  |
| Own house | 0.14 | 2.28 |
| Rent | --- | --- |
| Life cycle classification of HH |  |  |
| 2+ adults, retired, no children | --- | --- |
| Number of employed members | --- | --- |
| Count of HH trips on travel day | --- | --- |
| Three or more vehicles | --- | --- |
| Daily bike use | 0.28 | 2.01 |
| Daily smartphone use to access internet | 0.18 | 3.16 |
| Daily internet use | 0.33 | 2.31 |
| Travel is NOT a financial burden | 0.20 | 3.38 |
| Identification/Copula Parameters |  |  |
| Copula device | --- |  |
| Marginal distribution | Normal/Probit |  |
| Sigma (Regimes Specific) | --- | --- |
| Dependence (Regime Specific) | --- | --- |
| Kendall Tau | --- | --- |
| DOF-t marginal distributions | --- | --- |

## Estimation Results

| Variables | Selection <br> Equation (1/0) |  | Regime 0 (Not Plug-inHybrid) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | - | t-stat | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 | 3.04 | 77.69 |
| Household Income |  |  |  |  |
| Less than \$10,000 | --- | --- | -0.41 | -2.37 |
| \$15,000 to \$24,999 | --- | --- | -0.44 | -4.51 |
| \$25,000 to \$34,999 | --- | --- | -0.26 | -3.26 |
| High income (1 if income > 100,000) | 0.41 | 9.40 | --- | --- |
| Housing Status |  |  |  |  |
| Own house | 0.14 | 2.28 | --- | --- |
| Rent | --- | --- | -0.22 | -4.47 |
| Life cycle classification of HH |  |  |  |  |
| 2+ adults, retired, no children | --- | --- | -0.14 | -3.97 |
| Number of employed members | --- | --- |  |  |
| Count of HH trips on travel day | --- | --- | 0.06 | 23.50 |
| Three or more vehicles | --- | --- |  |  |
| Daily bike use | 0.28 | 2.01 | -0.59 | -4.79 |
| Daily smartphone use to access internet | 0.18 | 3.16 | --- | --- |
| Daily internet use | 0.33 | 2.31 | --- | --- |
| Travel is NOT a financial burden | 0.20 | 3.38 | --- | --- |
| Identification/Copula Parameters |  |  |  |  |
| Copula device | --- |  | Plackett copula |  |
| Marginal distribution | Normal/Probit |  | t-distribution |  |
| Sigma (Regimes Specific) | --- | --- | 0.98 | 43.60 |
| Dependence (Regime Specific) | --- | --- | 0.30 | 4.14 |
| Kendall Tau | --- | --- |  |  |
| DOF-t marginal distributions | --- | --- |  |  |

## Estimation Results

| Variables | Selection <br> Equation (1/0) |  | Regime 0 (Not Plug-inHybrid) |  |
| :---: | :---: | :---: | :---: | :---: |
|  | - | t-stat | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 | 3.04 | 77.69 |
| Household Income |  |  |  |  |
| Less than \$10,000 | --- | --- | -0.41 | -2.37 |
| \$15,000 to \$24,999 | --- | --- | -0.44 | -4.51 |
| \$25,000 to \$34,999 | --- | --- | -0.26 | -3.26 |
| High income (1 if income > 100,000) | 0.41 | 9.40 | --- | --- |
| Housing Status |  |  |  |  |
| Own house | 0.14 | 2.28 | --- | --- |
| Rent | --- | --- | -0.22 | -4.47 |
| Life cycle classification of HH |  |  |  |  |
| 2+ adults, retired, no children | --- | --- | -0.14 | -3.97 |
| Number of employed members | --- | --- |  |  |
| Count of HH trips on travel day | --- | --- | 0.06 | 23.50 |
| Three or more vehicles | --- | --- |  |  |
| Daily bike use | 0.28 | 2.01 | -0.59 | -4.79 |
| Daily smartphone use to access internet | 0.18 | 3.16 | --- | --- |
| Daily internet use | 0.33 | 2.31 | --- | --- |
| Travel is NOT a financial burden | 0.20 | 3.38 | --- | --- |
| Identification/Copula Parameters |  |  |  |  |
| Copula device | --- |  | Plackett copula |  |
| Marginal distribution | Normal/Probit |  | t-distribution |  |
| Sigma (Regimes Specific) | --- | --- | 0.98 | 43.60 |
| Dependence (Regime Specific) | --- | --- | 0.30 | 4.14 |
| Kendall Tau | --- | --- |  |  |
| DOF-t marginal distributions | --- | --- |  |  |

Estimation Results

| Variables | SelectionEquation (1/0) |  | Regime 0 (Not Plug-in Hybrid) |  | Regime 1 (Plug-in Hybrid/Electric) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\beta$ | t-stat | $\beta$ | t-stat | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 | 3.04 | 77.69 | 1.75 | 11.45 |
| Household Income |  |  |  |  |  |  |
| Less than \$10,000 | --- | --- | -0.41 | -2.37 | --- | --- |
| \$15,000 to \$24,999 | --- | --- | -0.44 | -4.51 | --- | --- |
| \$25,000 to \$34,999 | --- | --- | -0.26 | -3.26 |  |  |
| High income ( 1 if income > 100,000) | 0.41 | 9.40 | --- | --- | 0.53 | 5.96 |
| Housing Status |  |  |  |  |  |  |
| Own house | 0.14 | 2.28 | --- | --- | --- | --- |
| Rent | --- | --- | -0.22 | -4.47 | --- | --- |
| Life cycle classification of HH |  |  |  |  |  |  |
| 2+ adults, retired, no children | --- | --- | -0.14 | -3.97 | --- | --- |
| Number of employed members | --- | --- |  |  | 0.14 | 3.30 |
| Count of HH trips on travel day | --- | --- | 0.06 | 23.50 | 0.04 | 6.86 |
| Three or more vehicles | --- | --- |  |  | 0.32 | 3.50 |
| Daily bike use | 0.28 | 2.01 | -0.59 | -4.79 | -0.29 | -1.83 |
| Daily smartphone use to access internet | 0.18 | 3.16 | --- | --- | --- | --- |
| Daily internet use | 0.33 | 2.31 | --- | --- | --- | --- |
| Travel is NOT a financial burden | 0.20 | 3.38 | --- | --- | --- | --- |
| Identification/Copula Parameters |  |  |  |  |  |  |
| Copula device | --- |  | Plackett copula |  | Joe copula |  |
| Marginal distribution | Normal/Probit |  | t-distribution |  | t-distribution |  |
| Sigma (Regimes Specific) | --- | --- | 0.98 | 43.60 | 0.89 | 15.05 |
| Dependence (Regime Specific) | --- | --- | 0.30 | 4.14 | 1.81 | 14.57 |
| Kendall Tau | --- | --- | -0.26 |  | 0.31 |  |
| DOF-t marginal distributions | --- | --- | 14.93 |  | 10.38 |  |

Estimation Results

| Variables | Selection <br> Equation (1/0) |  | Regime 0 (Not Plug-in Hybrid) |  | Regime 1 (Plug-in Hybrid/Electric) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\beta$ | t-stat | $\beta$ | t-stat | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 | 3.04 | 77.69 | 1.75 | 11.45 |
| Household Income |  |  |  |  |  |  |
| Less than \$10,000 | --- | --- | -0.41 | -2.37 | --- | --- |
| \$15,000 to \$24,999 | --- | --- | -0.44 | -4.51 | --- | --- |
| \$25,000 to \$34,999 | --- | --- | -0.26 | -3.26 |  |  |
| High income ( 1 if income > 100,000) | 0.41 | 9.40 | --- | --- | 0.53 | 5.96 |
| Housing Status |  |  |  |  |  |  |
| Own house | 0.14 | 2.28 | --- | --- | --- | --- |
| Rent | --- | --- | -0.22 | -4.47 | --- | --- |
| Life cycle classification of HH |  |  |  |  |  |  |
| 2+ adults, retired, no children | --- | --- | -0.14 | -3.97 | --- | --- |
| Number of employed members | --- | --- |  |  | 0.14 | 3.30 |
| Count of HH trips on travel day | --- | --- | 0.06 | 23.50 | 0.04 | 6.86 |
| Three or more vehicles | --- | --- |  |  | 0.32 | 3.50 |
| Daily bike use | 0.28 | 2.01 | -0.59 | -4.79 | -0.29 | -1.83 |
| Daily smartphone use to access internet | 0.18 | 3.16 | --- | --- | --- | --- |
| Daily internet use | 0.33 | 2.31 | --- | --- | --- | --- |
| Travel is NOT a financial burden | 0.20 | 3.38 | --- | --- | --- | --- |
| Identification/Copula Parameters |  |  |  |  |  |  |
| Copula device | --- |  | Plackett copula |  | Joe copula |  |
| Marginal distribution | Normal/Probit |  | t-distribution |  | t-distribution |  |
| Sigma (Regimes Specific) | --- | --- | 0.98 | 43.60 | 0.89 | 15.05 |
| Dependence (Regime Specific) | --- | --- | 0.30 | 4.14 | 1.81 | 14.57 |
| Kendall Tau | --- | --- | -0.26 |  | 0.31 |  |
| DOF-t marginal distributions | --- | --- | 14.93 |  | 10.38 |  |

Estimation Results

| Variables | SelectionEquation (1/0) |  | Regime 0 (Not Plug-in Hybrid) |  | Regime 1 (Plug-in Hybrid/Electric) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\beta$ | t-stat | $\beta$ | t-stat | $\beta$ | t-stat |
| Constant | -1.84 | -12.96 | 3.04 | 77.69 | 1.75 | 11.45 |
| Household Income |  |  |  |  |  |  |
| Less than \$10,000 | --- | --- | -0.41 | -2.37 | --- | --- |
| \$15,000 to \$24,999 | --- | --- | -0.44 | -4.51 | --- | --- |
| \$25,000 to \$34,999 | --- | --- | -0.26 | -3.26 |  |  |
| High income ( 1 if income > 100,000) | 0.41 | 9.40 | --- | --- | 0.53 | 5.96 |
| Housing Status |  |  |  |  |  |  |
| Own house | 0.14 | 2.28 | --- | --- | --- | --- |
| Rent | --- | --- | -0.22 | -4.47 | --- | --- |
| Life cycle classification of HH |  |  |  |  |  |  |
| 2+ adults, retired, no children | --- | --- | -0.14 | -3.97 | --- | --- |
| Number of employed members | --- | --- |  |  | 0.14 | 3.30 |
| Count of HH trips on travel day | --- | --- | 0.06 | 23.50 | 0.04 | 6.86 |
| Three or more vehicles | --- | --- |  |  | 0.32 | 3.50 |
| Daily bike use | 0.28 | 2.01 | -0.59 | -4.79 | -0.29 | -1.83 |
| Daily smartphone use to access internet | 0.18 | 3.16 | --- | --- | --- | --- |
| Daily internet use | 0.33 | 2.31 | --- | --- | --- | --- |
| Travel is NOT a financial burden | 0.20 | 3.38 | --- | --- | --- | --- |
| Identification/Copula Parameters |  |  |  |  |  |  |
| Copula device | --- |  | Plackett copula |  | Joe copula |  |
| Marginal distribution | Normal/Probit |  | t-distribution |  | t-distribution |  |
| Sigma (Regimes Specific) | --- | --- | 0.98 | 43.60 | 0.89 | 15.05 |
| Dependence (Regime Specific) | --- | --- | 0.30 | 4.14 | 1.81 | 14.57 |
| Kendall Tau | --- | --- | -0.26 |  | 0.31 |  |
| DOF-t marginal distributions | --- | --- | 14.93 |  | 10.38 |  |

## Treatment Effects

| Treatment Effects | Trivariate-Joint <br> Normality | Trivariate-Joint <br> Switching | Trivariate-Joint <br> Switching |
| :--- | :---: | :---: | :---: |
|  | Gaussian copulas | Plackett-Joe Copulas | Plackett-Joe Copulas |
|  | Normal margins | Normal margins | Normal/t-distribution/t- <br> distribution |
|  | -0.384 | -1.38 |  |

## Closure

- .... Plug-in Hybrid/EV households travel on-average significantly less distance than their counterparts.
- Presence of self-selection effects.
- Standard approaches (if assumptions violated): provide misleading effects.
- Joint estimation of the behavioral system: Better than standard approaches.
- Given joint estimation, not only different marginal distributions, but also dependence structures yield much different effects.
- Future Work:

Analyze households that have both HEVs and PHEVs (Extend methodological framework)
$>$ Link HEV- and PHEV-VMT to each of the vehicle type
$>$ Look into vehicle use of conventional vehicles vis-à-vis AFVs


## Thank YOU

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Collaborative Sciences Center for CRUAD SAFETY

(3) ENERGY


卷OAK RIDGE
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[^0]:    Notes: For Plackett, $r=1+(\theta-1)\left(u_{1}+u_{2}\right)$. For Joe, $\widetilde{u}_{j}=1-u_{j}$.

